

ϕ and ω mesons in a nuclear
medium and the nuclear
photoproduction reaction

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Introduction

- The study of vector meson properties could be useful to find evidence of a possible partial restoration of chiral symmetry at finite ρ , T
- Particularly suited probes: electromagnetic decays (dileptons)



ρ meson has been extensively studied, dilepton spectrum from HIC's may indicate a lowering of M_ρ or large increase of Γ_ρ

R. Rapp, J. Wambach, Adv. Nucl Phys. 25 (2000) 1

- Narrow vector mesons (ω , ϕ) have received comparatively less attention



Interesting theoretical problems associated!

Introduction

- The ϕ meson is an appropriate probe for dynamics of vector mesons in nuclear matter
 - *Isolated* in the mass spectrum
 - Changes of properties comparatively *larger* than other mesons



Experimental observation in principle easier

- ϕ properties in nuclear medium strongly related to the renormalization of kaon properties



- *Kaon selfenergy*

Variety of models, predict different kaon potentials
Good reproduction of data (*K-atoms*, *HIC*)

- *Kaon condensation* → astrophysical implications

Experimental information from ϕ decay

→ *valuable info on kaon selfenergy*

Introduction

Proposed reactions to test ϕ , ω properties in nuclear medium

AA, pA collisions

$\pi p \rightarrow \phi n$ in nuclei

$\gamma N \rightarrow \phi N, \omega N$ in nuclei

Experiments

KEK-PS ☺

LEPS ☺

CB-TAPS@ELSA ☺

Near future...

HADES, CLAS (preliminary)

Very recent analysis from p-A reaction, presented in Chiral'05 and Quark Matter '05

Recent experimental data from nuclear inclusive ϕ photoproduction reaction

Very recent experimental data from nuclear ω photoproduction reaction

ϕ meson: Outline

ϕ meson mass and decay width in the nuclear medium – a selfenergy approach.

Experimental information: study of inclusive nuclear ϕ photoproduction.

D. Cabrera and M.J. Vicente Vacas, Phys. Rev C 67, 045203 (2003)

D. Cabrera, L. Roca, E. Oset, H. Toki and M.J. Vicente Vacas, Nucl. Phys. A 733 (2004) 130

Theoretical approaches to ϕ meson properties

ϕ mass

Effective Lagrangian approach

Weise et al.; Kuwabara and Hatsuda; Song; Bhattachayya et al.

QCD sum rules

Asakawa and Ko; Kampf et al.

ϕ decay width

Dropping of meson masses

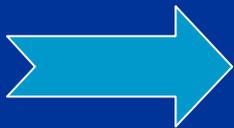
Bhattacharyya et al.; Ko et al.; Shuryak et al.; Panda et al.

Collisional broadening by ϕ -baryon and ϕ -meson interactions

Smith and Haglin; Alvarez-Ruso and Koch

Modification of ϕ decay channels (ϕ selfenergy approach, kaon selfenergies)

Weise et al.; Ramos et al.



Sizable renormalization of ϕ width
and small mass shift in nuclear medium

ϕ meson selfenergy in vacuum

* Interested in the ϕ to $\bar{K}K$ coupling \longrightarrow main ϕ decay channel in vacuum, BR 85% (ignore other contributions).

ϕ KK Lagrangian in a gauge vector representation

J. Schechter et al. 1988

W. Weise et al. 1998

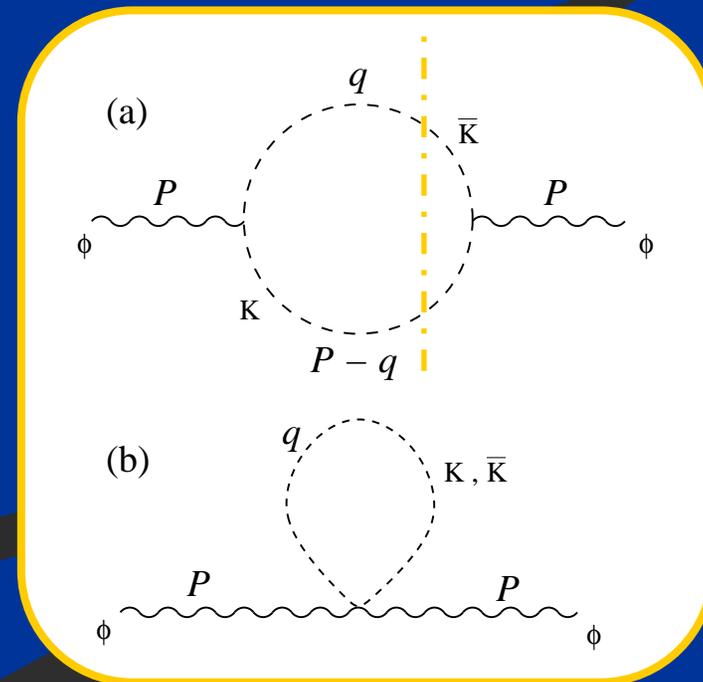
$$\mathcal{L}_{\phi,kaons} = -ig_{\phi}\phi_{\mu}(K^{-}\partial^{\mu}K^{+} - K^{+}\partial^{\mu}K^{-} + \bar{K}^0\partial^{\mu}K^0 - K^0\partial^{\mu}\bar{K}^0) + g_{\phi}^2\phi_{\mu}\phi^{\mu}(K^{-}K^{+} + \bar{K}^0K^0),$$

Gives rise to a ϕ selfenergy built from:

- $\bar{K}K$ loop diagram
- Kaon tadpole diagram

$$\text{Im}\Pi_{\phi} \rightarrow \Gamma_{\phi} = f(g_{\phi})$$

$$\Gamma_{\phi \rightarrow K^+K^-}^{\text{exp}} \rightarrow g_{\phi} = 4.57$$

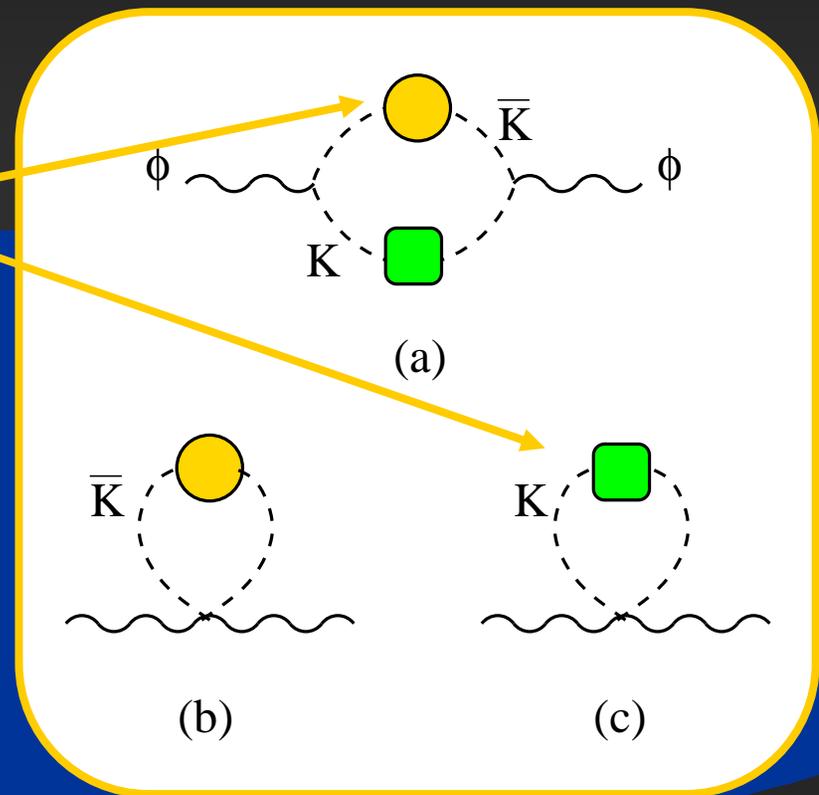


Nuclear medium effects

We modify the kaon propagators with selfenergy accounting for interactions with the nuclear medium

$$\Pi_{\bar{K}(K)}(q^0, \vec{q}; \rho)$$

$$\begin{aligned} \Pi_{\phi}^{ij}(P^0; \rho) = & \delta^{ij} i 2g_{\phi}^2 \frac{4}{3} \int \frac{d^4q}{(2\pi)^4} \vec{q}^2 D_K(P-q; \rho) D_{\bar{K}}(q; \rho) \\ & + \delta^{ij} i 2g_{\phi}^2 \left\{ \int \frac{d^4q}{(2\pi)^4} D_{\bar{K}}(q; \rho) + \int \frac{d^4q}{(2\pi)^4} D_K(q; \rho) \right\} \end{aligned}$$



$$D_{\bar{K}(K)}(q) \implies D_{\bar{K}(K)}(q^0, \vec{q}; \rho)$$

Kaon selfenergy: S-wave

Kaon and anti-kaon interactions with nucleons are rather different
 → we treat them separately

- KN : smooth at low energies, since there are not $S=1$ resonances (?)
 We use $t\rho$ approximation

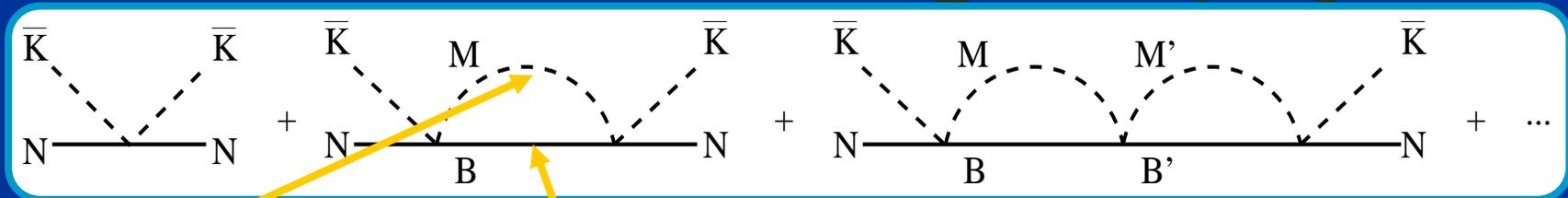
$$\Pi_{K^+} = \frac{1}{2}(t_{K^+p} + t_{K^+n})\rho = 0.13 m_K^2 \frac{\rho}{\rho_0}$$

N. Kaiser, P.B. Siegel and W. Weise, Nucl. Phys. A 594 (1995) 325

- $\bar{K}N$: strongly dominated by the excitation of *sub-threshold* $\Lambda(1405)$.

Chiral unitary model in coupled channels for *S-wave* $\bar{K}N$ scattering

E. Oset and A. Ramos, Nucl. Phys. A 635 (1998) 99



π and K selfenergies

Pauli blocking
 Mean-field potentials

Selfconsistent calculation of the S-wave selfenergy

A. Ramos and E. Oset, Nucl.Phys. A 671 (2000) 481

Kaon selfenergy: P-wave

$\Sigma^* = \Sigma^*$ (1385)

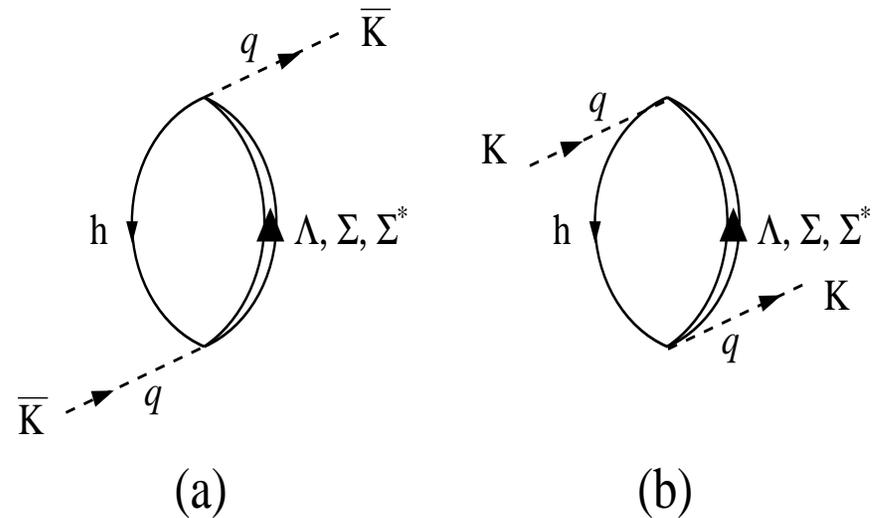
Built from Λh , Σh and $\Sigma^* h$ excitations, found to be an important source of ϕ renormalization in a nuclear medium.

Klingl, Waas and Weise 98; Oset and Ramos 01

KNY interaction from lowest order chiral Lagrangian coupling pseudoscalar meson and $1/2^+$ baryon octets.

$$\begin{aligned} \Pi_{\bar{K}}^P(q, \rho) = & \frac{1}{2} \tilde{V}_{K^p\Lambda}^2 f_{\Lambda}^2(q) \vec{q}^2 U_{\Lambda}(q, \rho) \\ & + \frac{3}{2} \tilde{V}_{K^p\Sigma^0}^2 f_{\Sigma}^2(q) \vec{q}^2 U_{\Sigma}(q, \rho) \\ & + \frac{1}{2} \tilde{V}_{K^p\Sigma^{*0}}^2 f_{\Sigma^*}^2(q) \vec{q}^2 U_{\Sigma^*}(q, \rho) \end{aligned}$$

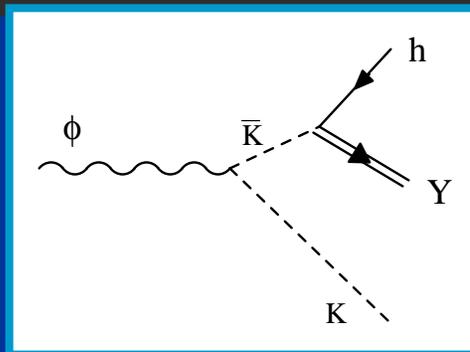
$$\Pi_K^P(q^0, \vec{q}; \rho) = \Pi_{\bar{K}}^P(-q^0, \vec{q}; \rho)$$



ϕ meson selfenergy in the medium

ϕ decay channels which open in the medium due to Π_K :

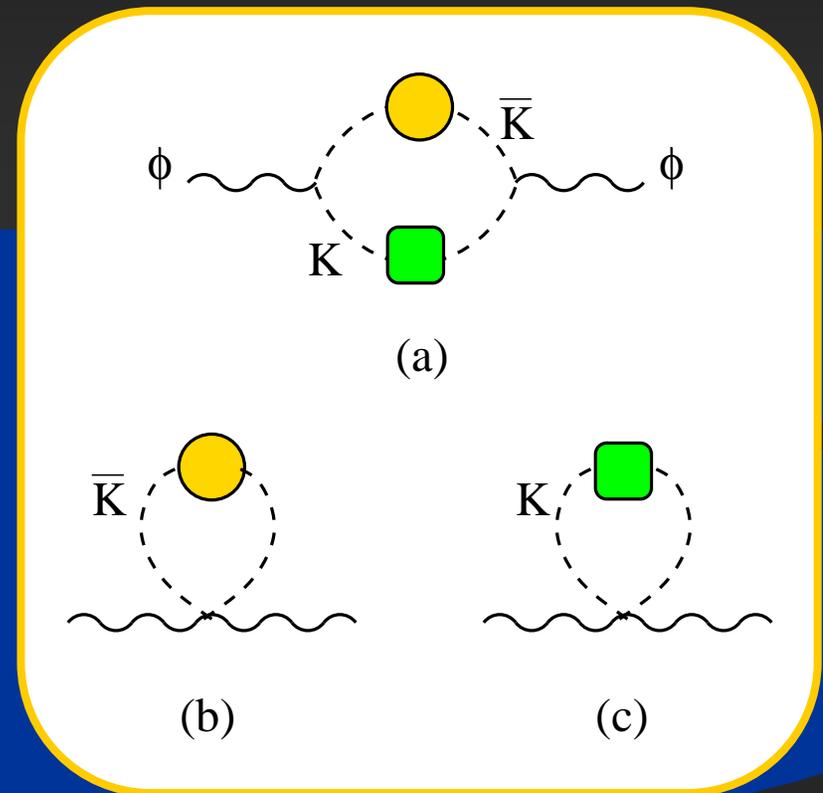
- S-wave: $\phi \rightarrow KM Yh$ ($\pi\Sigma, \pi\Lambda$)
- P-wave: $\phi \rightarrow K Yh$



Use of spectral (Lehmann) representation for kaon, anti-kaon propagator, guarantees *crossing*

$$D_{\bar{K}(K)}(-q^0, \vec{q}; \rho) = D_{K(\bar{K})}(q^0, \vec{q}; \rho)$$

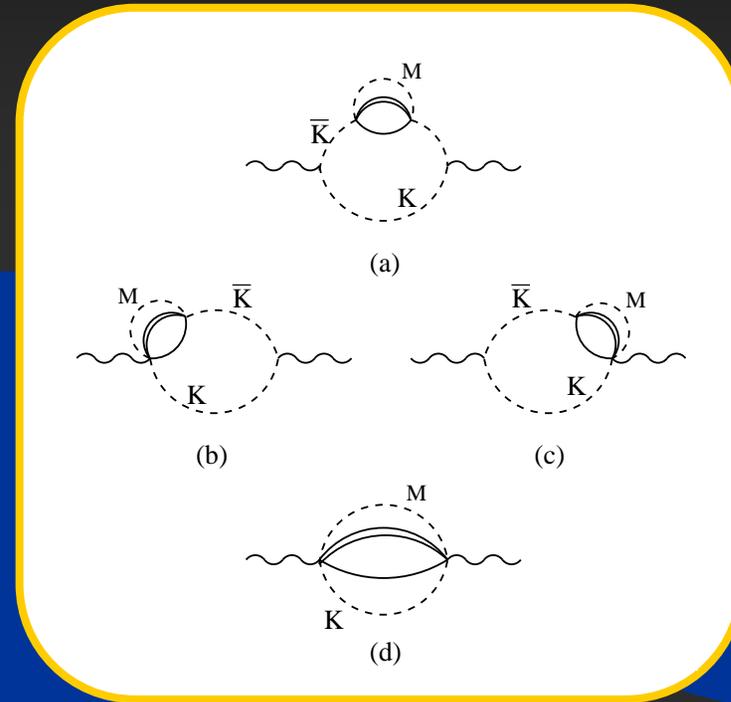
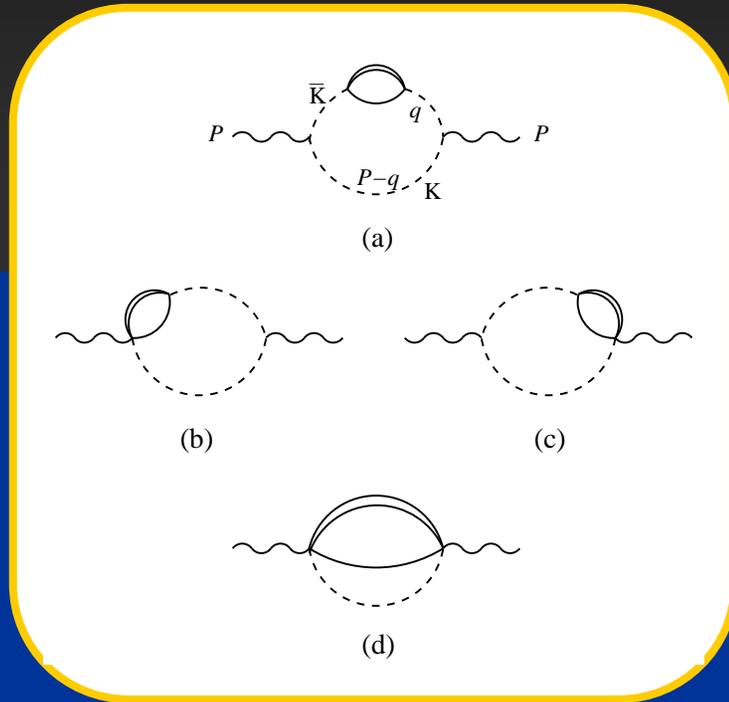
Kaon propagator:
$$D_{\bar{K}(K)}(q^0, \vec{q}; \rho) = \int_0^\infty d\omega \left\{ \frac{S_{\bar{K}(K)}(\omega, \vec{q}; \rho)}{q^0 - \omega + i\eta} - \frac{S_{K(\bar{K})}(\omega, \vec{q}; \rho)}{q^0 + \omega - i\eta} \right\}$$



Vertex corrections and gauge invariance

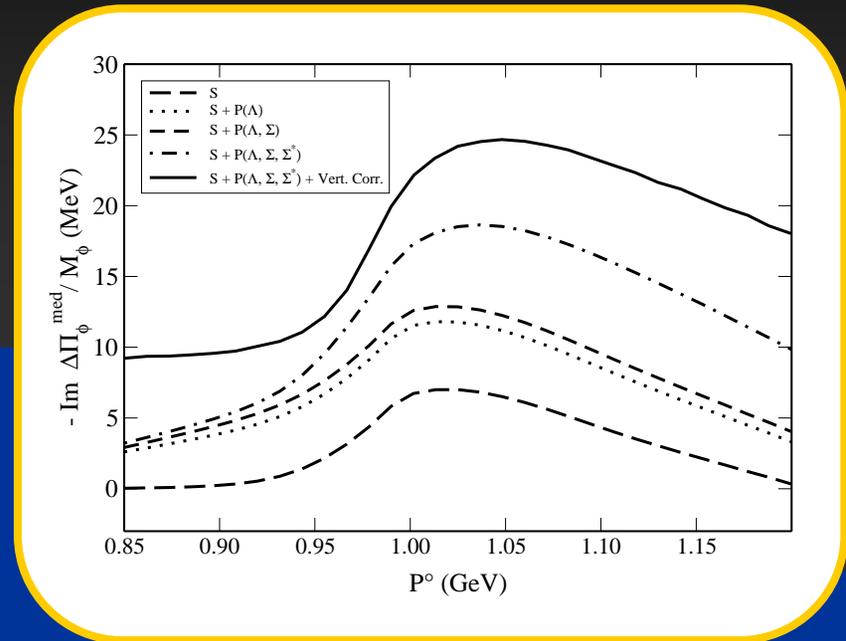
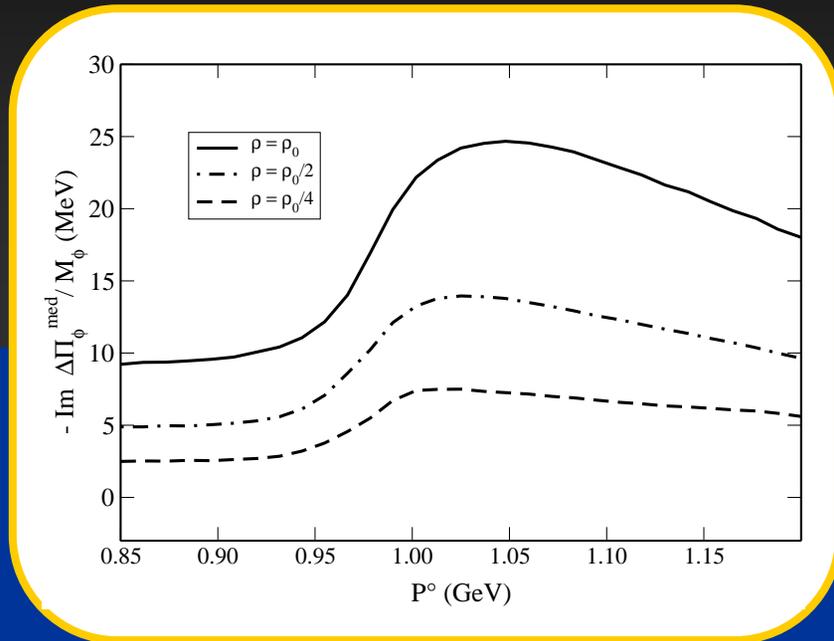
Herrmann, Friman and Noremborg 93; Chanfray and Schuck 93

P- and *S*-wave kaon selfenergy insertions and related vertex corrections:



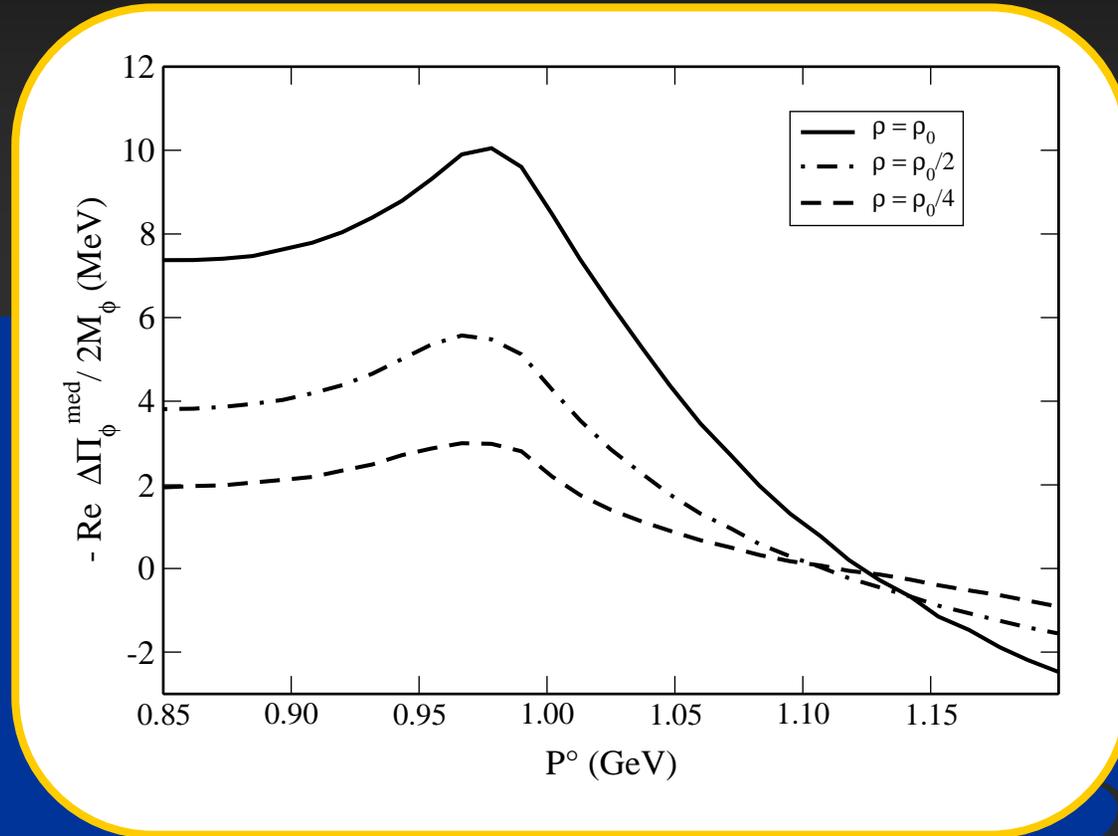
- (a) included by using the renormalized kaon & antikaon propagators
- (b-d) generated by vertex corrections
- Contact vertices: can be obtained by imposing W.I.

Results: ϕ mass and decay width in the nuclear medium



- ϕ width grows considerably with the density: $\Gamma_\phi \approx 30$ MeV, $\rho = \rho_0$
F. Klingl, T. Waas and W. Weise, Phys. Lett. B 431 (1998) 254;
E. Oset and A. Ramos, Nucl. Phys. A 679 (2001) 616
- Sizeable energy dependence due to the $\phi \rightarrow K \Sigma^* h$ channel (thres. ~ 940 MeV)
- K S-wave: mildly attractive contribution, compensates partly K repulsion
- K P-wave: small contribution from Σ , sizeable from Λ and Σ^* excitations
- Vertex corrections: further enhancement of the total width

Results: ϕ mass and decay width in the nuclear medium (II)

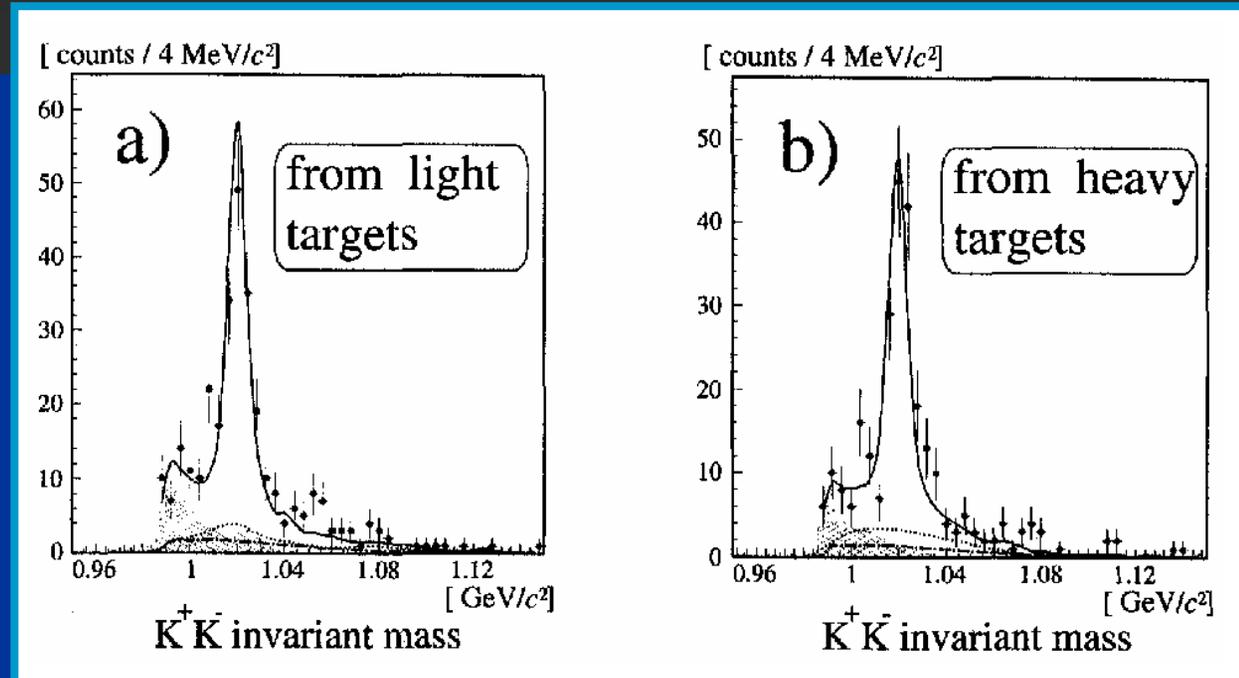


- Real part of ϕ selfenergy: very small, attractive up to 1.1 GeV
- ϕ mass change: $\sim(-8)$ MeV at $\rho=\rho_0$

Experimental information on ϕ properties in the nuclear medium

Several experimental proposals to observe changes in the ϕ properties in a nuclear medium:

- HIC's (p - A , A - A collisions)
- $\pi p \rightarrow \phi N$
- $\gamma N \rightarrow \phi N$



- Results from p - A reaction: *KEK-PS E325*, K. Ozawa et al., *Nucl. Phys. A* 698 (2002) 535c

Experimental information on ϕ properties in the nuclear medium

- Results from p - A reaction: *KEK-PS E325*, K. Ozawa et al., *Nucl. Phys. A* 698 (2002) 535c
- HIC's $^{28}\text{Si} + ^{196}\text{Au}$: *BNL-AGS E802*, Y. Akiba et al., *Phys. Rev. Lett.* 96 (1996) 2021
Au + Au: PHENIX Col., Adler et al., *nucl-ex/0410012*
- $\gamma A \rightarrow K^+K^-X$: *LEPS*, T. Ishikawa et al., *Phys. Lett. B* 608 (2005) 215



Medium effects on the mass or decay width of the ϕ meson are difficult to observe

Problems:

- Long ϕ lifetime: ϕ decays outside the nuclear medium
- ϕ is produced with high P_ϕ
- Kinematical cuts to isolate small- P_ϕ events
→ poor statistics
- Distortion in K^+K^- distribution (Coulomb interaction may bind K^- in nucleus)

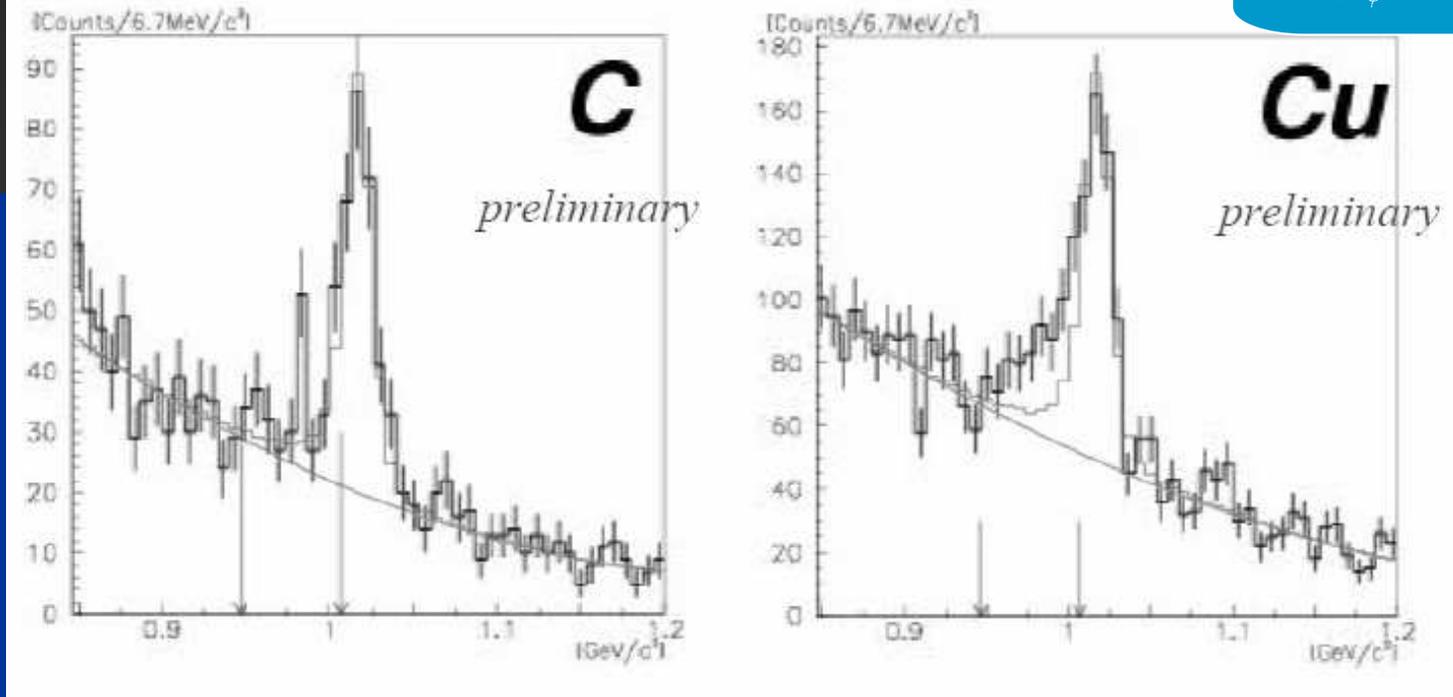
*P. Mühlich, T. Falter, C. Greiner, J. Lehr, M. Post and U. Mosel,
Phys. Rev. C 67 (2003) 024605*

Dilepton spectrum from p -A reaction: KEK-PS E325,

presented at Chiral'05, 16 Feb 2005, RIKEN, Japan

slowly moving ϕ ($\beta\gamma < 1.35$)

ϕ momentum cut
 $p_\phi = M_\phi \beta \gamma$



borrowed from S. Yokkaichi

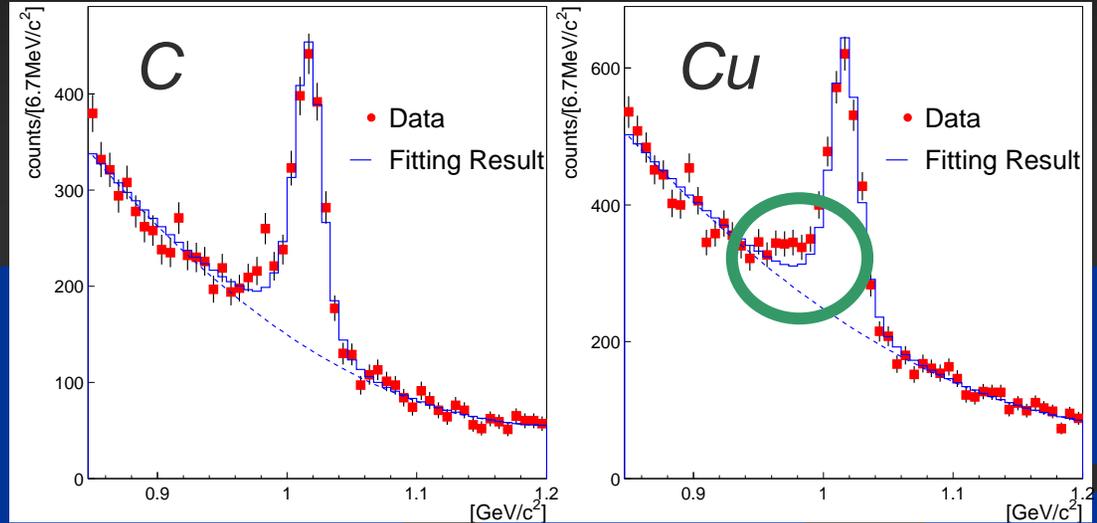
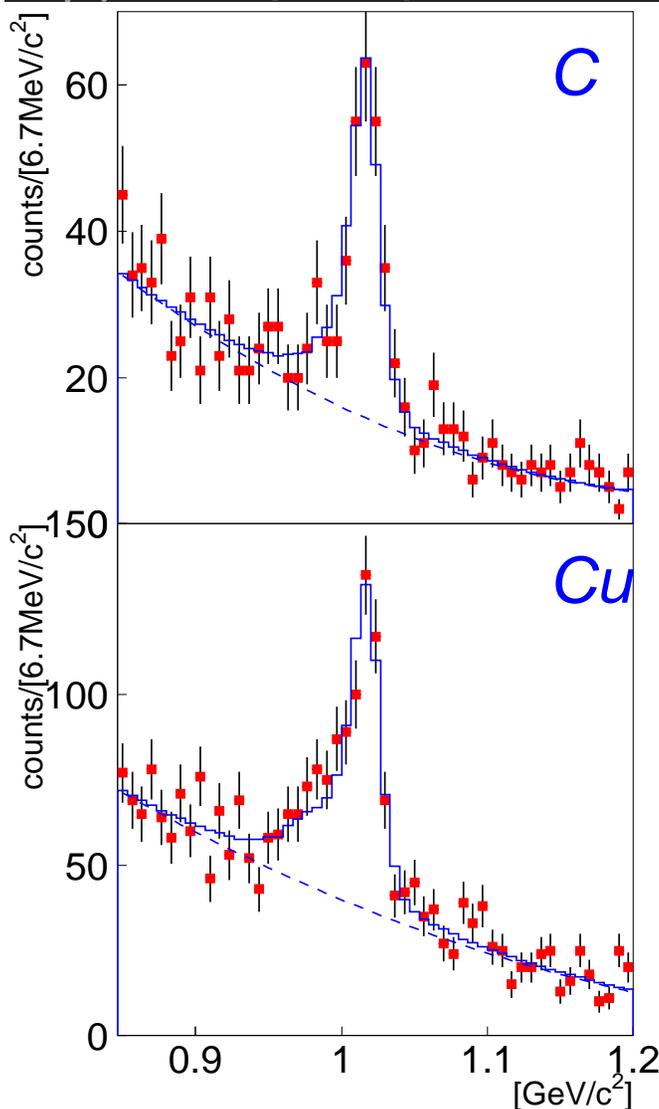
- Toy model with -16% mass shift at ρ_0 . Also $\Gamma_\phi(\rho) = (1 + 6 \rho/\rho_0) \Gamma_\phi^{\text{vac}}$ is used in analysis to understand *dilepton yield excess*
- If only $\Delta\Gamma_\phi$, *symmetric effect* expected

*K⁺K⁻ analysis
on going...*

Dilepton spectrum from p -A reaction: KEK-PS E325,

presented at QM '05, Aug 4-9, Budapest

$\beta\gamma < 1.25$ (Slow)



borrowed from R. Muto

- Low energy tail cannot be fit (bkgnd + BW)
- $M_\phi(\rho) = (1 - 0.04 \rho/\rho_0) M_\phi^{\text{vac}} \longrightarrow \Delta M_\phi(\rho_0) \approx -40 \text{ MeV}$
- $\Gamma_\phi(\rho) = (1 + 10 \rho/\rho_0) \Gamma_\phi^{\text{vac}} \longrightarrow \Gamma_\phi(\rho) \approx 44 \text{ MeV}$
- No momentum dependence ($p_\phi \sim 2 \text{ GeV}$)

$M_\phi(\rho)$ Hatsuda et al.; $\Gamma_\phi(\rho)$ Weise et al.

Study of inclusive nuclear ϕ photoproduction

Proposal: observation of **loss of ϕ flux** due to nuclear effects and its A dependence

- No need to cut ϕ phase space \longrightarrow better statistics
- A dependence of ϕ flux can be related to the ϕ decay width in the nuclear medium

But: Most of the produced ϕ 's carry a high momentum



Extension of our model for finite P_ϕ

Experiment:

Spring8/Osaka **LEPS**

(γ, ϕ) with $E_\gamma \in [1.5-2.4]$ GeV

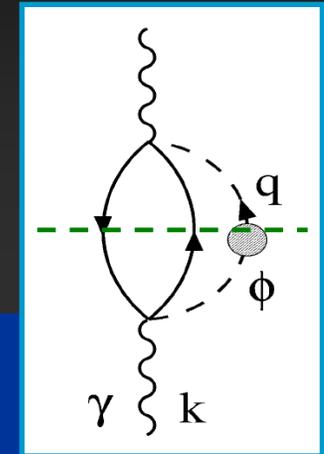
$P_\phi \sim 1.8$ GeV

Study of inclusive nuclear ϕ photoproduction

ϕ flux and ϕ decay width:

$$\frac{\Gamma_\phi}{2} = -\text{Im}V_{opt} = -\text{Im}\frac{\Pi_\phi}{2\omega} \Rightarrow \Gamma_\phi = -\frac{\text{Im}\Pi_\phi}{\omega} \equiv \frac{dP}{dt}$$

$$\frac{dP}{dl} \equiv \frac{dP}{v dt} = \frac{dP}{\frac{P_\phi}{\omega} dt} = -\frac{\text{Im}\Pi_\phi}{P_\phi}$$



Nuclear cross section for inclusive nuclear ϕ photoproduction:

$$\frac{d\sigma_A}{d\Omega} = \int d^3\vec{r}\rho(r) \frac{d\sigma}{d\Omega} e^{-\int_0^\infty dl \frac{1}{P} \text{Im}\Pi_\phi(P^0, P; \rho(r'))}$$

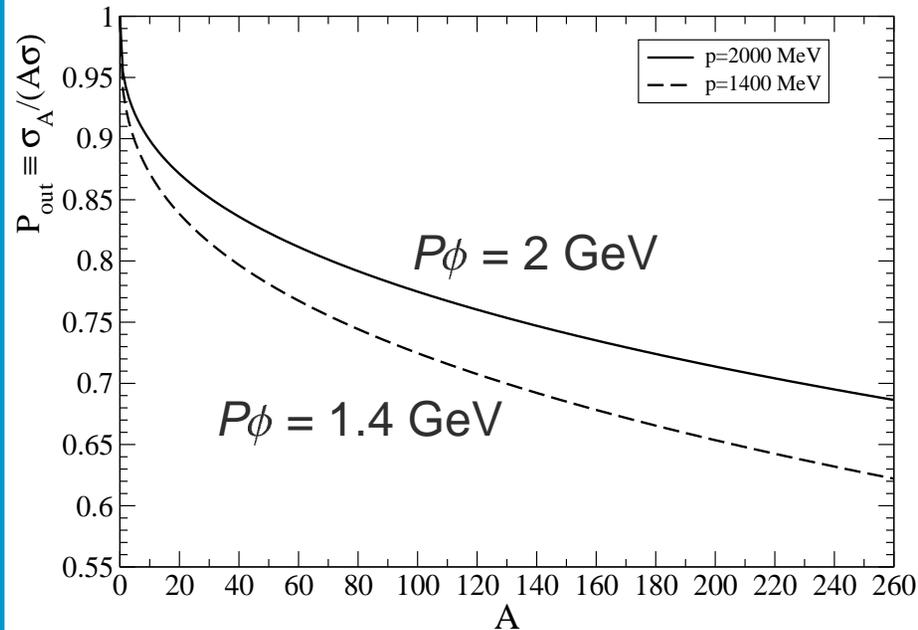
Absorption factor

ϕ survival probability:

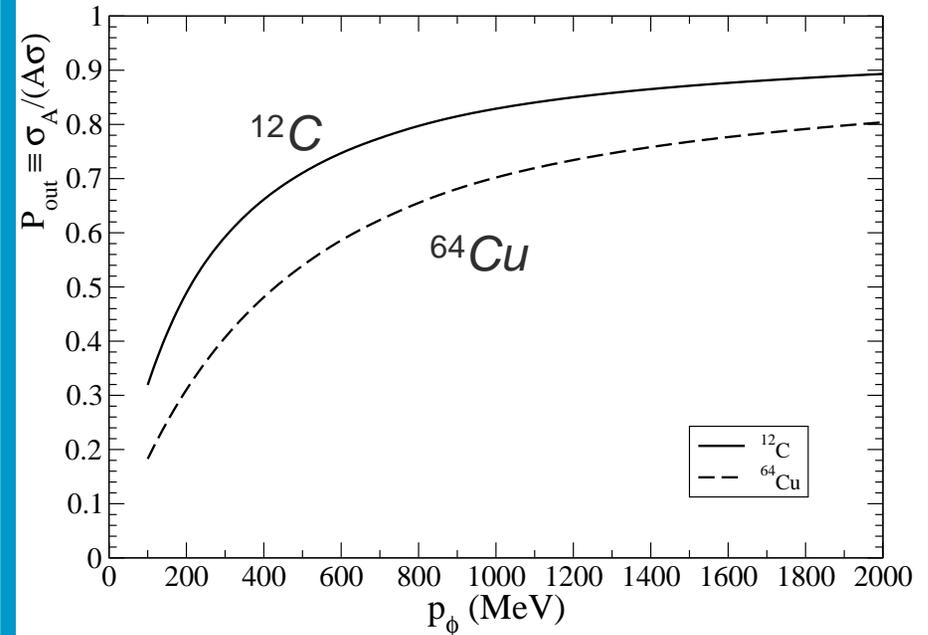
$$\mathcal{P}_{out} \equiv \frac{\sigma_A}{A\sigma} = \frac{1}{A} \int d^3\vec{r}\rho(r) e^{\int_0^\infty dl \frac{1}{P} \text{Im}\Pi_\phi(P^0, P; \rho(r'))}$$

Inclusive nuclear ϕ photoproduction: results

A dependence



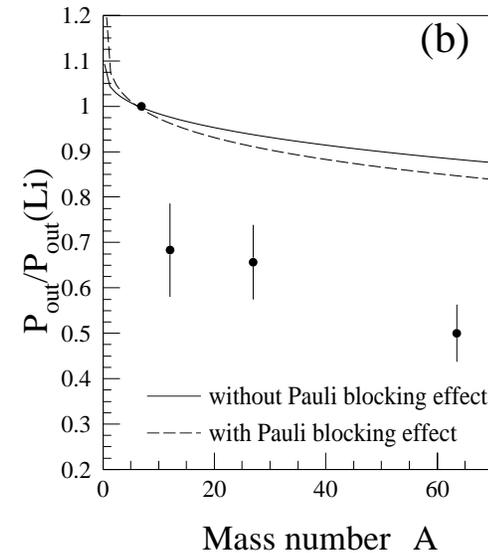
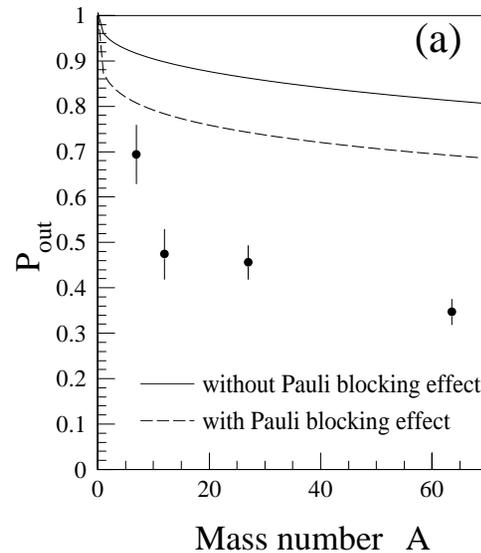
P_ϕ dependence



- Clear loss of ϕ flux: enhanced effect for small P_ϕ and heavy nuclei
- $E_\gamma = 1.6$ GeV $\rightarrow P_\phi \approx 1000$ MeV in fwd direction $\rightarrow P_{\text{out}} \sim 0.65$ for ^{64}Cu , and smaller for heavier nuclei

Inclusive nuclear ϕ photoproduction: experimental results

LEPS
Collaboration,
T. Ishikawa et al.,
Phys. Lett. B 608
(2005) 215,
[nucl-ex/0411016](#)



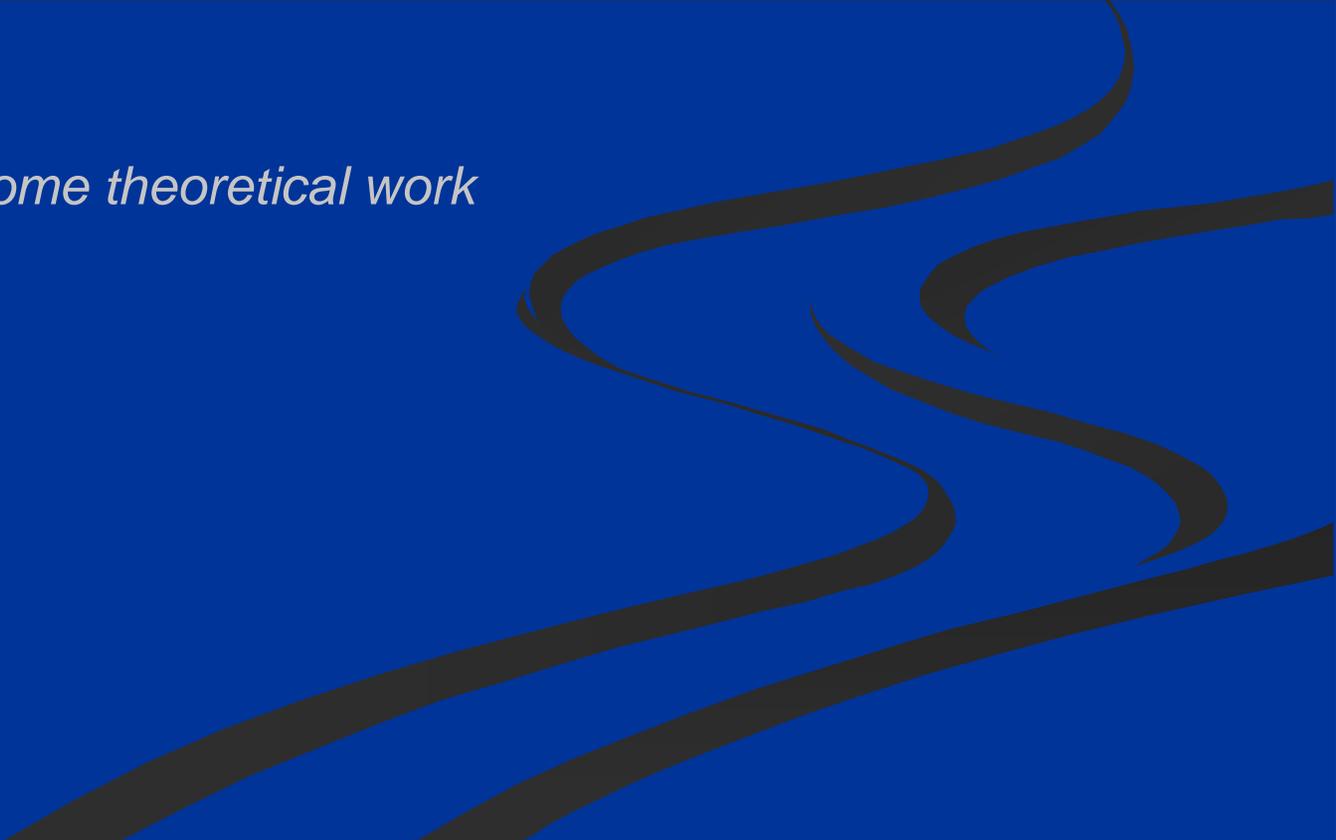
- Separation of the coherent ϕ photoproduction is important, particularly for light nuclei
- Stronger effect than theoretically predicted
- Calculation agrees with A -dependence (normalize to C)
- Other possible sources of ϕN interactions (further flux reduction)

Ex: $\phi \rightarrow 3\pi$ (pion selfenergy!), quasi-elastic collisions

ω meson: Outline

(Recent) experimental information on the ω meson in-medium decays

Overview of some theoretical work



ω meson in the medium: experimental information

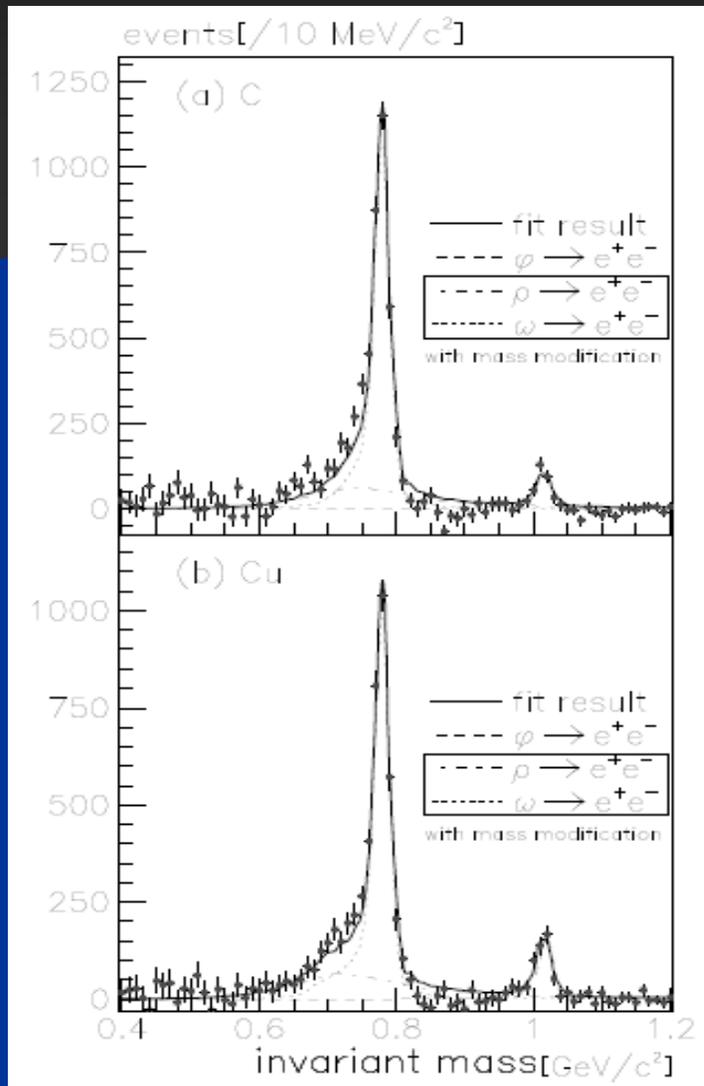
- Very small width in vacuum, mostly from 3π decay
- Appears overlapped with the ρ meson in the mass spectrum
- Several theoretical calculations predict *sizable changes* in mass / decay width at finite ρ or T
- Current experiments search for medium modifications in mass spectrum observable

Recent experimental results:

- KEK-PS E325: p -A reaction + $\rho/\omega \rightarrow e^+e^-$ decay
- CB-TAPS/ELSA Col. @ Bonn: nuclear ω photoproduction + $\omega \rightarrow \pi^0 \gamma$ decay

ω meson in the medium: experimental information

- KEK-PS E325: p -A reaction + $\omega \rightarrow e^+e^-$ decay *M. Naruki et al., nucl-ex/0504016*



- 50 times 2001 statistics
- e^+e^- mass resolution 8 MeV (ρ/ω) and 10 MeV (ϕ)
- Yield excess below ω mass:
 $M_V(\rho)/M_V = 1 - k \rho/\rho_0$, $k \approx 0.10$ from fit
($k = 0.10-0.22$, Hatsuda, Lee, Shiomi '95)
- No broadening is assumed
- Actually, no broadening is favoured in the analysis

ω meson in the medium: experimental information

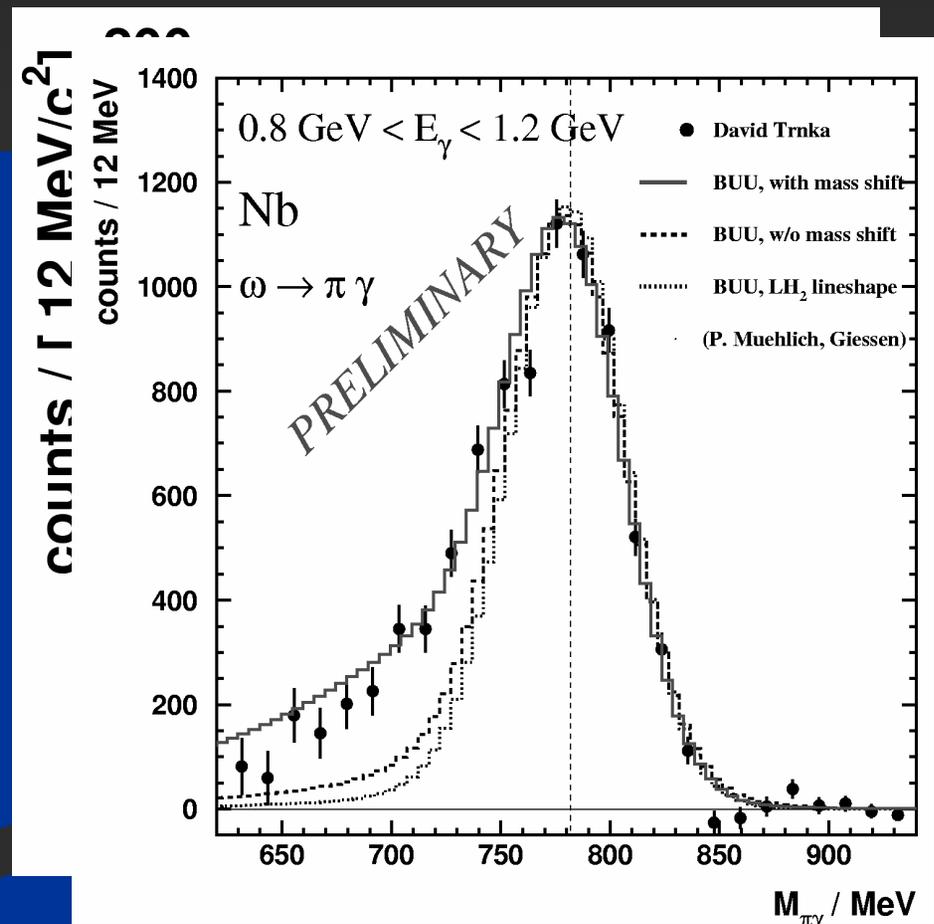
- CB-TAPS@ELSA Col.: nuclear ω photoproduction + $\omega \rightarrow \pi^0 \gamma$ decay

* $\pi^0 \gamma$ decay: much suppressed for ρ meson (10^{-2}) \longrightarrow no overlap

- Sizable enhancement of spectrum below M_ω
- Effect vanishes when increasing p_ω cuts
- Width dominated by exp. resolution ($\Gamma_\omega < 55$ MeV at estimated $\rho = 0.6\rho_0$)

BUU transport calculation incl. FSI, collisional broadening and explicit ΔM_ω proportional to density (-16% at ρ_0)

P. Mühlich et al., Eur. Phys. J. A20 (2004) 499



borrowed from V. Metag

ω meson in the medium: theoretical approaches

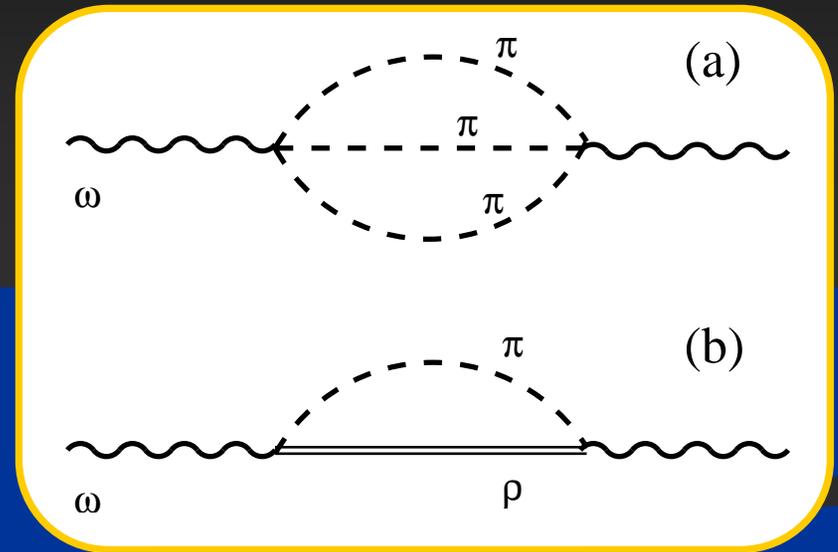
A simple calculation in a selfenergy approach

$$\mathcal{L}_{V\Phi}^{(3)} = \frac{i\hbar}{4f_\pi^3} \epsilon^{\mu\nu\alpha\beta} \text{tr}(V_\mu \partial_\nu \Phi \partial_\alpha \Phi \partial_\beta \Phi) + \frac{g_{VVP}}{4f_\pi} \epsilon^{\mu\nu\alpha\beta} \text{tr}(\partial_\mu V_\nu V_\alpha \partial_\beta \Phi),$$

$\rho\pi$ decay is about 90% of $\Gamma(\omega \rightarrow 3\pi)$

(from $\phi \rightarrow (\omega) \rightarrow 3\pi$ and radiative decays)

P. Jain et al., Phys. Rev. D37 (1988) 3252; F. Klingl et al., Z. Phys. A356 (1996) 193



Medium effects on intermediate mesons:

- 3π : plenty of phase space, pion attraction will not make a strong effect
- $\rho\pi$: not open at the physical ρ mass, only the *low energy ρ tail* is explored ($E \sim 500$ MeV, $\rho \sim 200$ MeV)



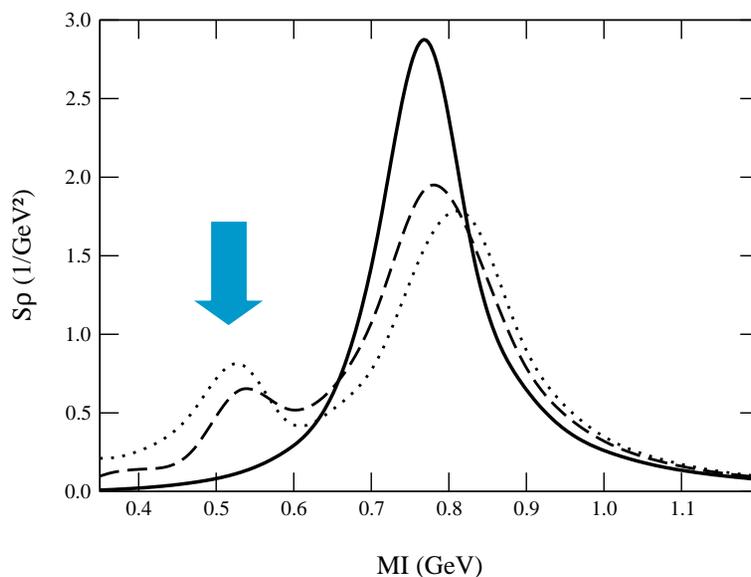
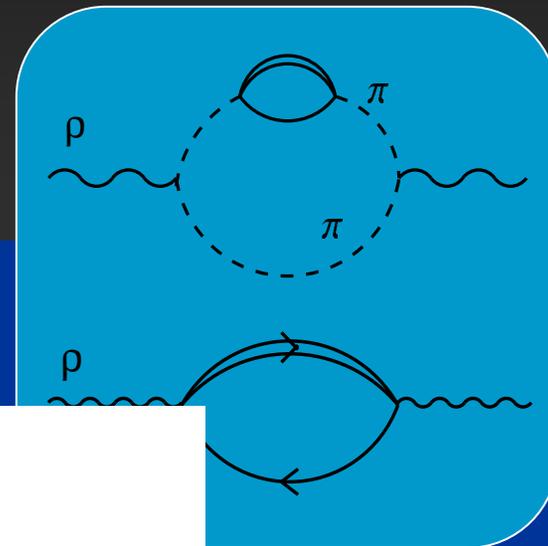
ρ spectral function enhanced in this region at finite nuclear density

ω meson in the medium: theoretical approaches

A simple calculation in a selfenergy approach

Several in-medium mechanisms could spread ρ spectral density to lower energies:

- π selfenergy ($ph, \Delta h$)
- ρ coupling to $ph, \Delta h$ states (for $p_\rho \neq 0$)
- Excitation of Rh states (ex. $N^*(1520), \dots$)



D.Cabrera et al., Nucl. Phys. A705 (2002) 90

at rest:

$$(\Gamma_\omega^{vac} = 8.49 \text{ MeV})$$

excitation!!)

ω meson in the medium: theoretical approaches

Many other mechanisms have been studied

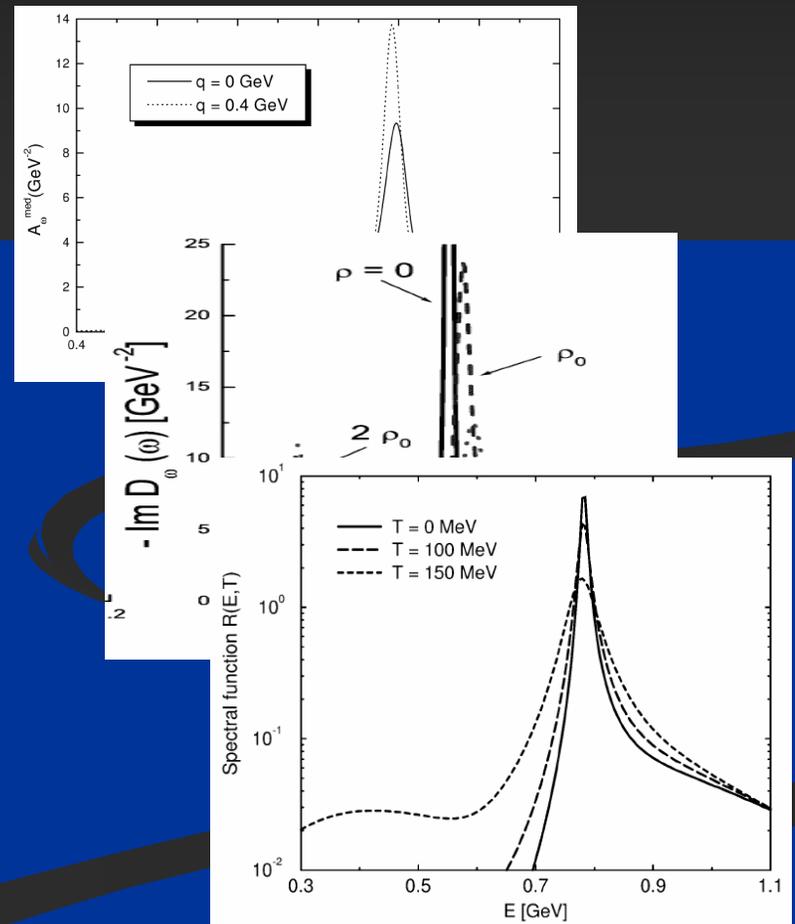
- $\omega N \rightarrow \pi N$, $\omega N \rightarrow \rho N \rightarrow [\pi\pi]N$ in a Chiral SU(3) Lagrangian approach: $\Delta\Gamma_\omega \approx 40$ MeV!
F. Klingl et al. Nucl. Phys. A624 (1997) 527; A650 (1999) 299

- ω coupling to several Rh states ($N^*(1520)h$, $N^*(1650)h$, ...) *M. Post et al. Nucl. Phys. A688 (2001)808; M. Lutz et al Nucl. Phys. A706 (2002) 431*

- Self-consistent determination of ρ and ω spectral functions *F. Riek et al., Nucl. Phys. A740 (2004) 287*

- Finite T effects (ex. $\omega\pi \rightarrow \pi\pi$, thermally excited pions) *R. Rapp, Phys. Rev. C63 (2001) 054907; R. Schneider et al., Phys. Lett. B515 (2001) 89; A. Martell et al., Phys. Rev. C69 (2004) 065206*

- QCD sum rules calculations *S. Zschocke et al., Phys. Lett. B562 (1993) 57*



ω meson in the medium: theo + exp

Γ_ω expected to increase \approx one order of magnitude, the ω still keeping its resonant shape as a quasiparticle in the nuclear medium



This should be observable as a (A-dependent) *clear loss of ω flux* in a nuclear photoproduction experiment...



...well suited to provide *COMPLEMENTARY* information to the measure of the mass spectrum observable in vector meson decays

What is needed (from ϕ experience) ?

- Good control of *coherent production*
- Reliable calculations of ω properties at finite p_ω

If some effect is observed...

- Clear evidence of medium effects on the ω meson (Γ_ω)
- Test of ρ and p dependence of calculated ω nuclear potentials

Conclusions

- Much work has been carried out regarding the properties of vector mesons in dense and hot matter
- Narrow vector mesons (particularly ϕ) have received less attention, but very exciting experimental results have been found recently in production reactions in nuclei

ϕ meson mass and decay width in a nuclear medium

- Model calculation based on (anti-)kaon selfenergies
- ϕ decay width increases considerably in nuclear matter (6-8 $\Gamma_{\phi}^{\text{free}}$ at ρ_0)
- Very small change in the ϕ mass
- Very recent analysis from p -A dilepton spectrum from KEK-PS shows some nuclear medium effect

Conclusions

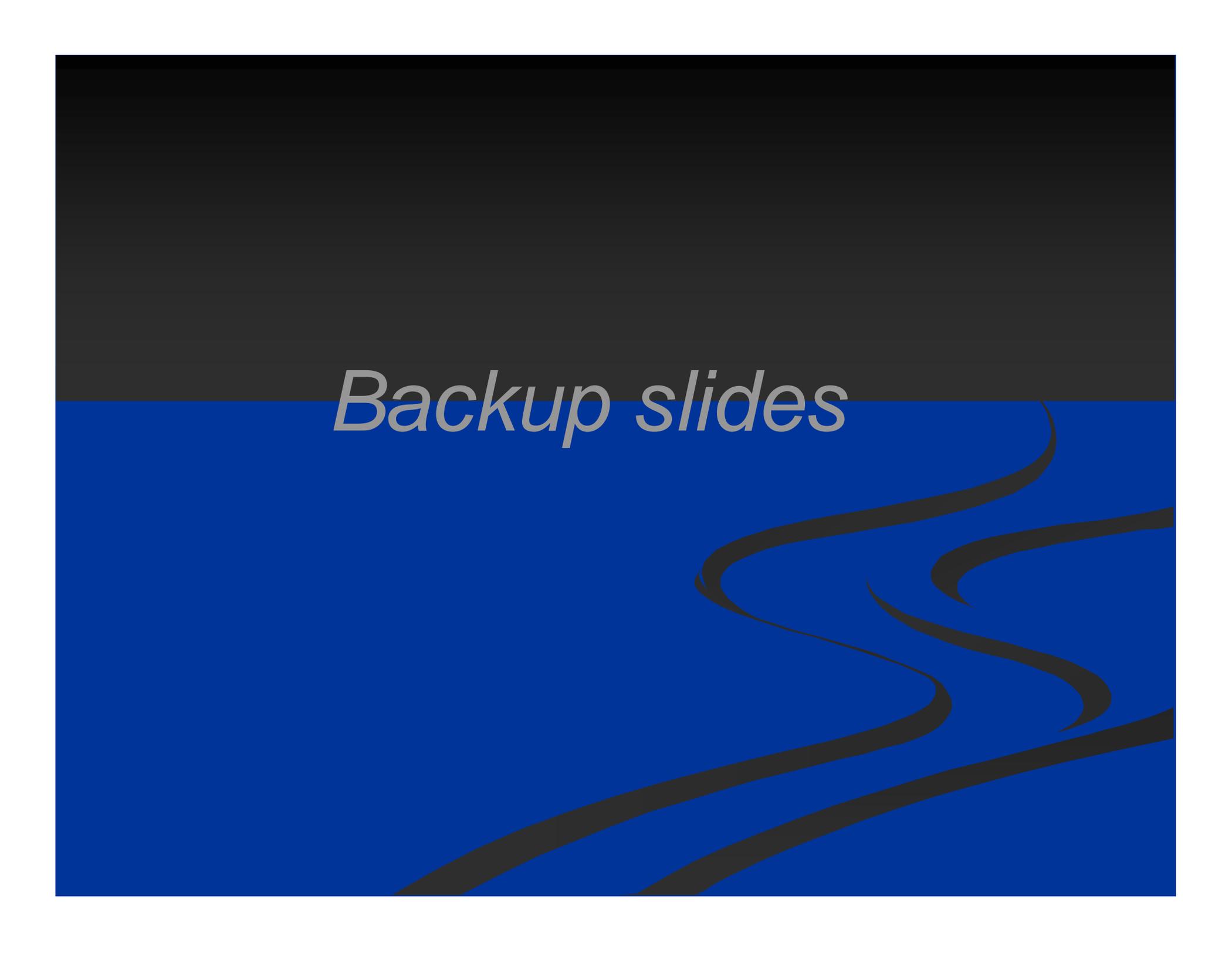
Inclusive nuclear ϕ photoproduction: A dependence

- A dependence of loss of ϕ flux can be related to the in-medium ϕ decay width
- Clear deviation from unity in the calculated ϕ survival probability indicates a loss of ϕ flux due to nuclear medium effects
- Experimental results from LEPS find a reduction in the survival probability, *stronger effect than calculated*

ω meson properties

- Sizable effects theoretically estimated
- Some effect experimentally observed in nuclear photoproduction + $\pi^0 \gamma$ decay by CB-TAPS/ELSA
- We suggest that measurement of loss of ω flux (and A -dependence) could provide complementary information (Γ_ω)

Backup slides

The image features a solid blue background. On the right side, there is a decorative graphic consisting of several thick, dark grey, wavy lines that curve and flow downwards, resembling a stylized wave or a series of connected loops.

Outlook and work in progress

Inclusive nuclear ϕ photoproduction: A dependence

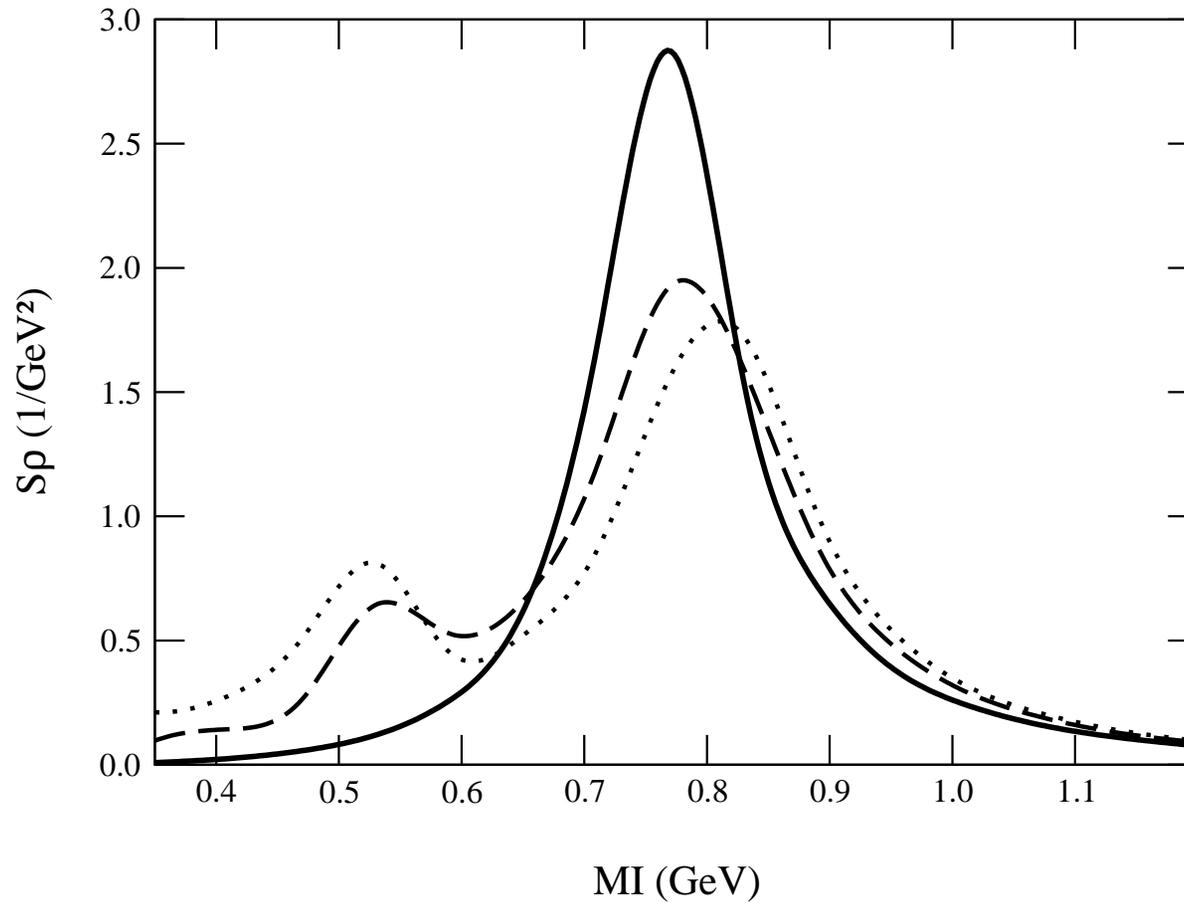
- Calculate A dependence of loss of ϕ flux for different kaon-antikaon potentials (shallow-deep) \longrightarrow study sensitivity of P_{out}
- Study other possible effects leading to a flux reduction: $\phi \rightarrow 3\pi$ (small), quasi-elastic ϕN collisions (forward acceptance)
- Extend the model for finite temperature (application to HIC)

ω meson selfenergy

- Complete selfenergy calculation including pion cloud modifications, ρ selfenergy and coupling of ρ, ω to baryonic resonances (and finite T)
- Subthreshold coupling to $\bar{K}K$ \longrightarrow *additional open channels in the nuclear medium (+ 5 MeV)*

ρ spectral function in nuclear matter (ρ at rest)

D. Cabrera, E. Oset and M.J. Vicente Vacas, Nucl Phys. A705 (2002) 90



$$\phi \rightarrow (\omega) \rightarrow 3\pi$$

$$\phi \rightarrow (\omega) \rightarrow \rho\pi$$

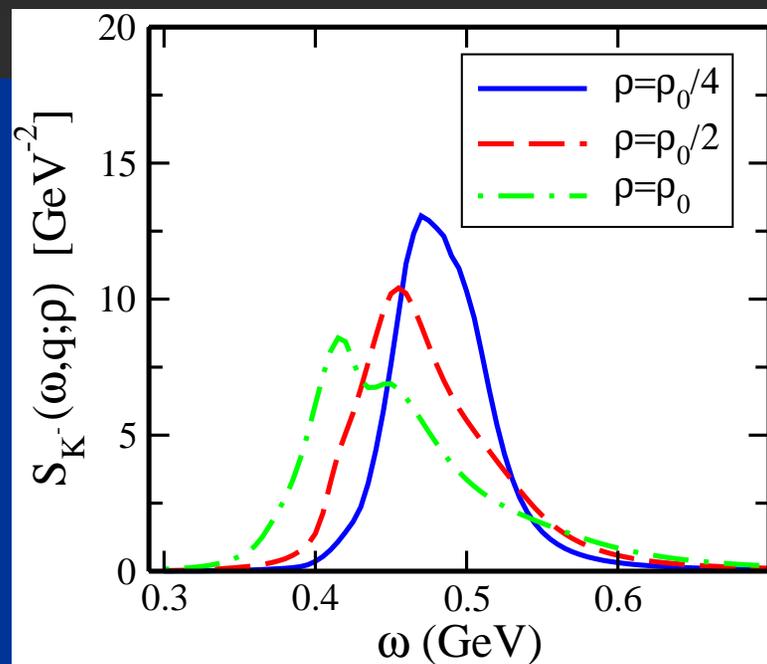
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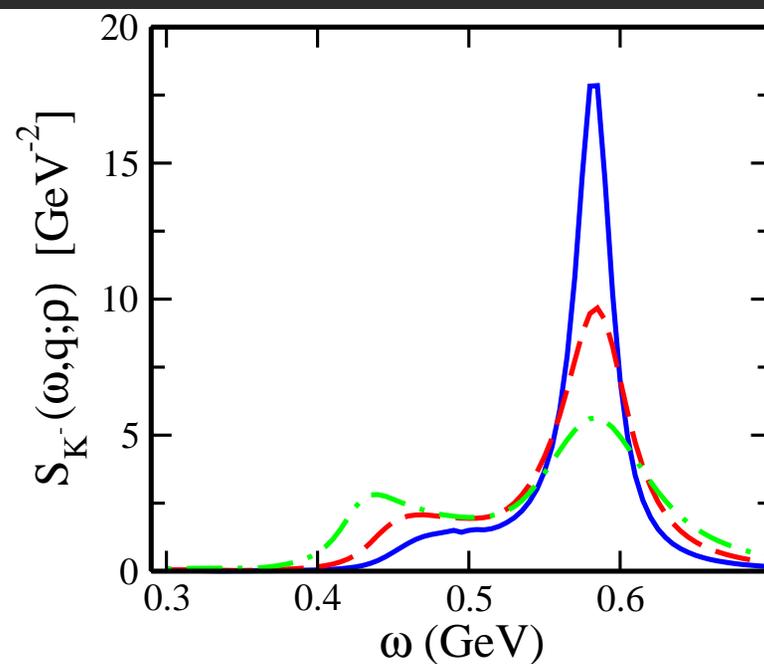
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Antikaon spectral function for several nuclear densities

A. Ramos and E. Oset, Nucl.Phys. A 671 (2000) 481



zero momentum

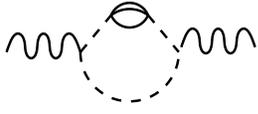
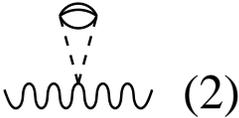
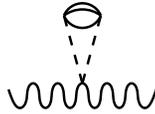
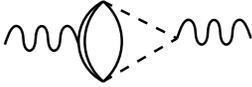
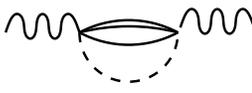


$q=300$ MeV

ϕ selfenergy from kaon loop and tadpole diagrams, in terms of the spectral functions of the kaon propagators

$$\begin{aligned}\Pi_\phi(P^0; \rho) &= 2g_\phi^2 \frac{1}{2\pi^2} \frac{4}{3} \int_0^\infty dq \vec{q}^2 \left\{ \frac{\vec{q}^2}{\tilde{\omega}(q)} \int_0^\infty d\omega \frac{S_{\bar{K}}(\omega, |\vec{q}|; \rho) (\omega + \tilde{\omega}(q))}{(P^0)^2 - (\omega + \tilde{\omega}(q))^2 + i\epsilon} \right. \\ &+ \left. \frac{3}{4} \left[\int_0^\infty d\omega S_{\bar{K}}(\omega, |\vec{q}|; \rho) + \frac{1}{2\tilde{\omega}(q)} \right] \right\}\end{aligned}$$

Vertex corrections and gauge invariance (II)

Π_ϕ^{00}	Π_ϕ^{0j}	Π_ϕ^{ij}
 (1)		
 (2)		
 (3)		
 (4)		

Detailed analysis of necessary diagrams to satisfy gauge invariance in a non-relativistic approximation of vertices involving baryons and baryon propagators

$$q_\mu \Pi_\phi^{\mu\nu} = 0$$

↔
(ϕ at rest in n.m.)

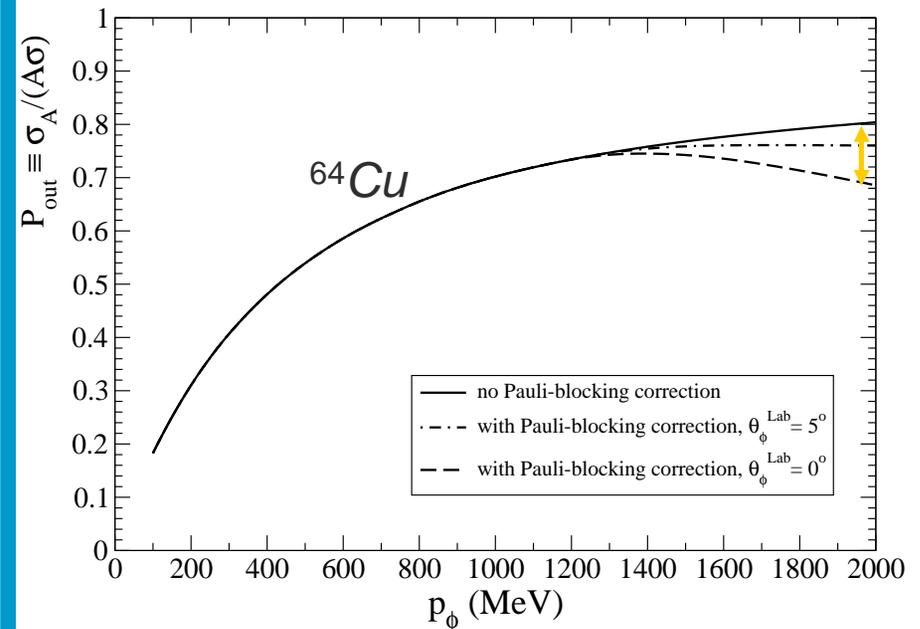
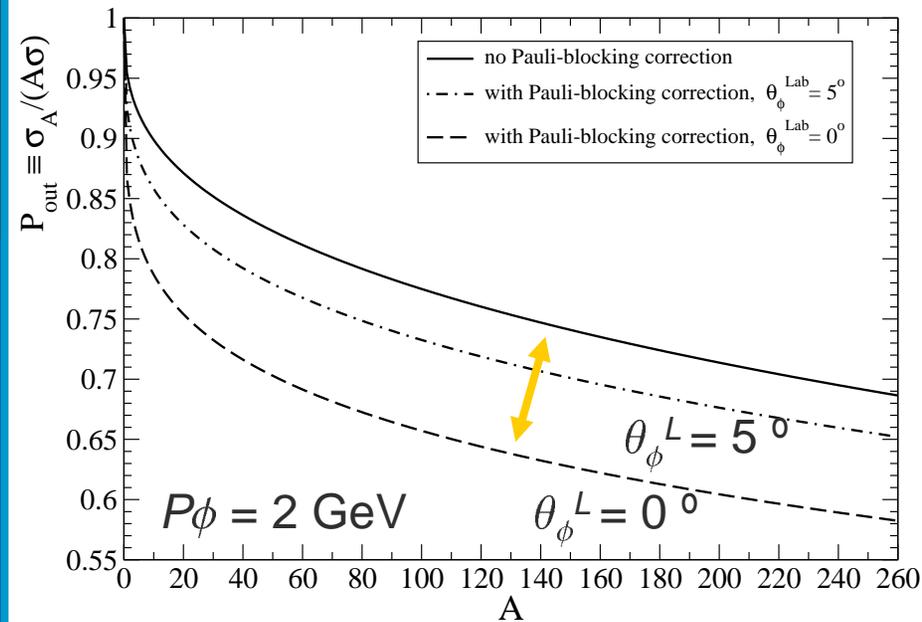
$$q^0 \Pi_\phi^{00} = 0 \leftrightarrow \Pi_\phi^{00}$$

$$q^0 \Pi_\phi^{i0} = 0 \leftrightarrow \Pi_\phi^{i0} = 0$$

$$q^0 \Pi_\phi^{0j} = 0 \leftrightarrow \Pi_\phi^{0j} = 0$$

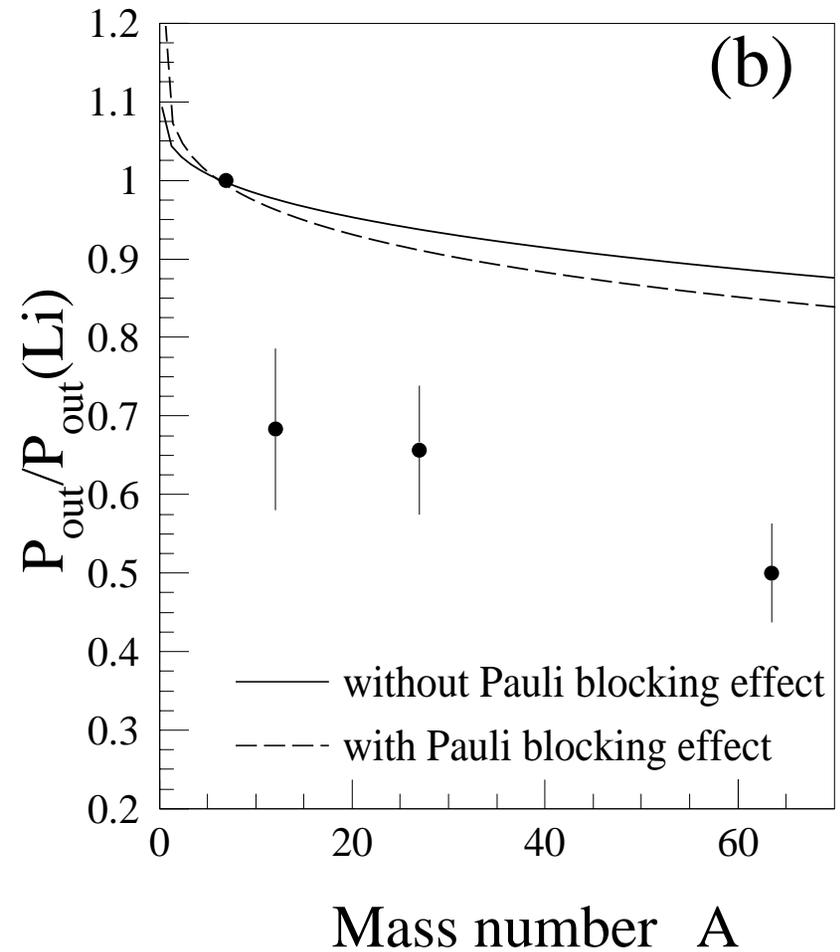
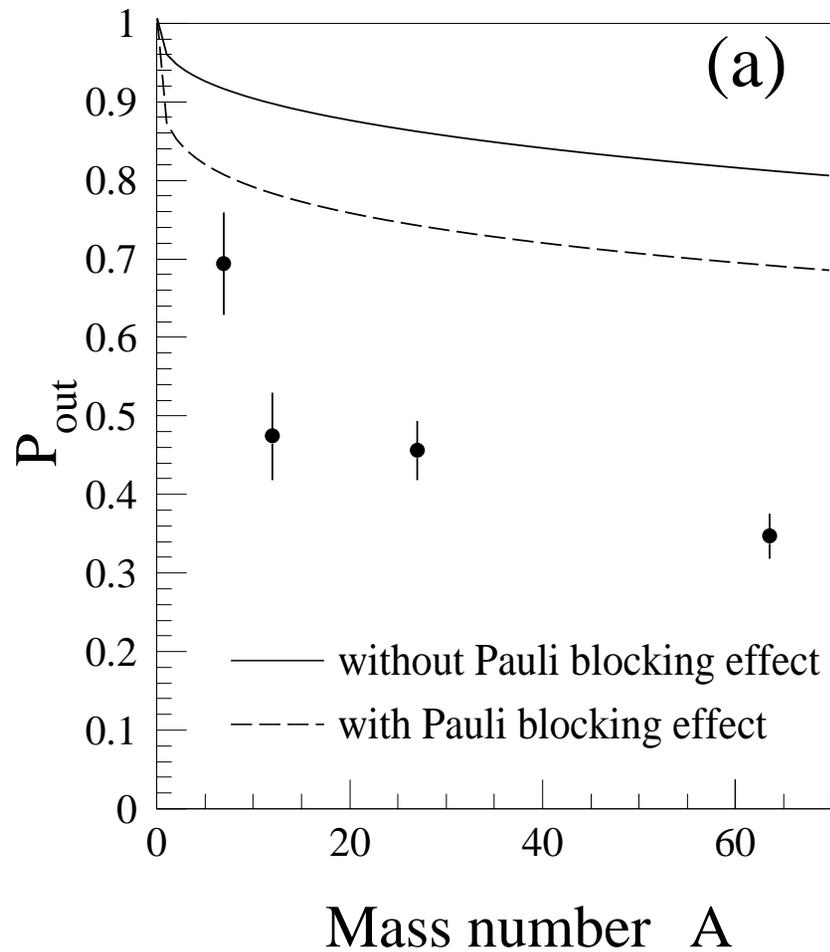
Inclusive nuclear ϕ photoproduction: results

Other nuclear effects: Pauli blocking and Fermi motion



- Pauli blocking of the final nucleon is important for high P_ϕ (small momentum transfer)
- ϕ photoproduction is forward peaked, thus actual effect is to be found somewhere in $\theta_\phi^L < \text{a few degrees}$

Inclusive nuclear ϕ photoproduction: experimental results



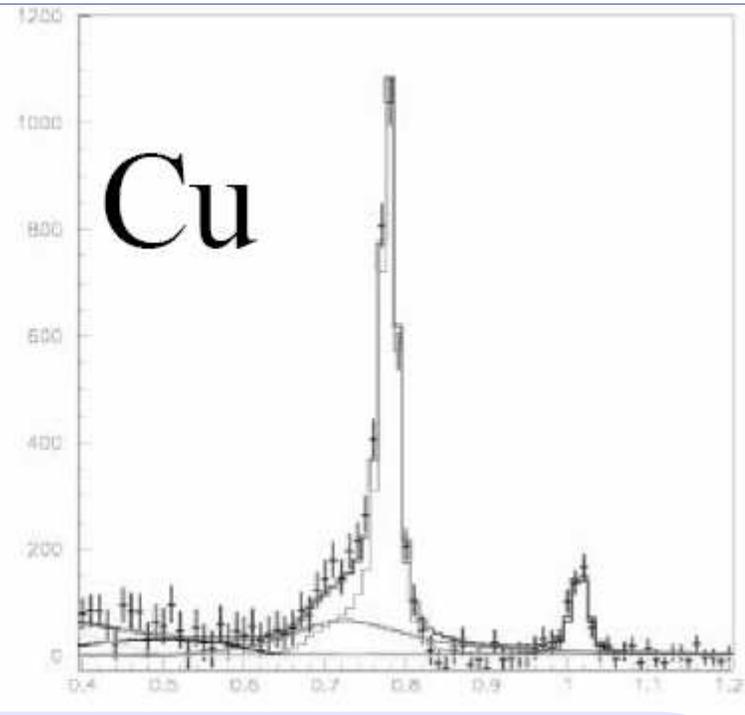
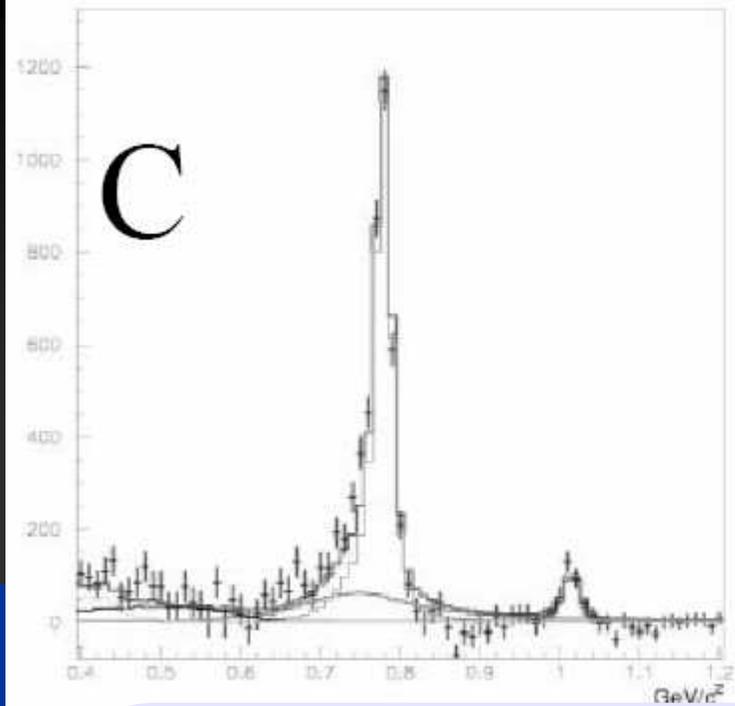
Toy model again : Width broadning of ϕ ?

- Many theoretical predeictions ...
 - $\Gamma=22\text{MeV}$, $\Delta m=0$ at $\rho=\rho_0$ (Oset et.al,2001)
 - $\Gamma=30\text{MeV}$, $\Delta m=8\text{MeV}$ at $\rho=\rho_0$ (Cabrera et.al, 2003)
- Toy model like ρ & ω , including width (=decay prob.) change
- Inside-nucleus decay (=at $\rho > 0.5 \rho_0$) probability for ϕ

- natural width ($\Gamma=4.4\text{MeV}$)	C	Cu
• all our acceptances	1 %	3%
• slow ($\beta\gamma < 1.35$)	2 %	6%
- $\Gamma=30\text{MeV}$ at $\rho=\rho_0$		
• all	5 %	18%
• slow	9 %	32%

- Observation : $N(\text{excess})/(N(\text{excess})+N(\phi))$		
• all	(9+-7) %	(13+-7)%
• slow	(15+-15) %	(25+-12)%

- $\Gamma^*/\Gamma_0 = 1 + 6 \rho^*/\rho_0$
 $4.4 * 7 \sim 30\text{MeV}$ at $\rho=\rho_0$)
- no theoretical basis



Results from experiments measuring mass spectrum observable show *some medium effects are there*, BUT interpretation in terms of ΔM_V and / or $\Delta \Gamma_V$ still difficult



- Sizable modifications are predicted

- ϕ , ω stay as quasiparticles in the medium