Probing the Equation of State of Neutron-Rich Matter with Heavy-Ion Reactions

Bao-An Li

Arkansas State University

Collaborators:Lie-Wen Chen, Shanghai Jiao Tong University Champak B. Das, Subal Das Gupta and Charles Gale, McGill University Che Ming Ko, Texas A&M University Andrew W. Steiner, Los Alamos National Laboratory Gao-Chan Yong and Wei Zuo, Chinese Academy of Science

- 1. EOS and symmetry energy of neutron-rich matter
- Current status, importance for nuclear physics and astrophysics
- 2. Major physical issues in modeling nuclear reactions induced by neutron-rich nuclei
- Momentum dependence of the symmetry potential
- Neutron-proton effective mass splitting in neutron-rich matter
- Isospin dependence of in-medium nucleon-nucleon cross sections
- 3. Experimental probes of the symmetry energy
- An example: isospin diffusion/transport in heavy-ion reactions
- 4. Impacts of the symmetry energy constrained by available data on the isospin diffusion and the size of neutron-skin in ²⁰⁸Pb
- Nuclear effective interactions
- Cooling mechanisms of proto-neutron stars
- Radii of neutron stars



A.E. L. Dieperink, Y. Dewulf, D. Van Neck, M. Waroquier and V. Rodin, Phys. Rev. C68 (2003) 064307

Components of the symmetry energy



A.E. L. Dieperink, Y. Dewulf, D. Van Neck, M. Waroquier and V. Rodin, Phys. Rev. C68 (2003) 064307

E_{sym}(ρ) from Hartree-Fock approach using different effective interactions

B. Cochet, K. Bennaceur, P. Bonche, T. Duguet and J. Meyer, Nucl. Phys. **A731**, 34 (2004). J. Stone, J.C. Miller, R. Koncewicz, P.D. Stevenson and M.R. Strayer, PRC **68**, 034324 (2003). Bao-An Li, PRL **88**, 192701 (2002) (where paramaterizations of E^a_{sym} and E^b_{sym} are given)



- The major remaining uncertainty in determining the EOS of <u>symmetric</u> nuclear matter is due to the poor knowledge about $E_{sym}(\rho)$ Example 1: On extracting the incompressibility $K_{\infty}(\rho_0)$ from isoscalar giant monopole resonance,
- J. Piekarewicz, PRC 69, 041301 (2004); G. Colo, et al., PRC 70, 024307 (2004).

Liquid-drop formula for finite nuclei: $K_A = m \langle r^2 \rangle_0 E^2_{ISGMR} = K_{\infty} (1+cA^{-1/3}) + K_{asy} \delta^2 + K_{Coul} Z^2 A^{-4/3}$

Isobaric incompressibility of asymmetric matter: $K_{\infty}(\rho, \delta) = K_{\infty}(\rho) + K_{asy}(\rho)\delta^2$

 $K_{\infty}(\rho_0) \equiv 9\rho_0^2 (d^2 E / d\rho^2)_{\rho_0} \text{ and } K_{asy}(\rho_0) \equiv 9\rho_0^2 (d^2 E_{sym} / d\rho^2)_{\rho_0} - 18\rho_0 (dE_{sym} / d\rho)_{\rho_0}$





Expanding fireball and gamma-ray burst (GRB) from the superdene neutron star (magnetar) SGR 1806-20 on 12/27/2004. RAO/AUI/NSF

GRB and nucleosynthesis in the expanding fireball after an explosion of a supermassive object depends on the n/p ratio

In pre-supernova / explosion of massive stars $e^- + p \rightarrow n + v_e$ is easier with smaller symmetry energy

The multifaceted influence of symmetry energy in astrophysics and nuclear physics

J.M. Lattimer and M. Prakash, *Science Vol. 304 (2004) 536-542.* A.W. Steiner, M. Prakash, J.M. Lattimer and P.J. Ellis, *Phys. Rep. 411, 325 (05)*



The proton fraction x at ß-equilibrium in proto-neutron stars is determined by

$$x \approx 0.048 [E_{sym}(\rho) / E_{sym}(\rho_0)]^3 (\rho / \rho_0) (1 - 2x)^3$$

The critical proton fraction for direct URCA process to happen is $X_p=0.14$ for npeµ matter obtained from energy-momentum conservation on the proton Fermi surface

Slow cooling: modified URCA:

$$n + (n, p) \rightarrow p + (n, p) + e^{-} + v_{e}$$

$$p + (n, p) \rightarrow n + (n, p) + e + V_e$$

Consequence: long surface thermal emission up to a few million years

Faster cooling by 4 to 5 orders of magnitude: direct URCA $n \rightarrow p + e^{-} + \overline{v}_{e}$ $p \rightarrow n + e^{+} + v_{e}$

PSR J0205+6449 in 3C58 was suggested as a candidate



B.A. Li, Nucl. Phys. A708, 365 (2002).

Probing the EOS of neutron-rich matter in terrestrial labs



Bao-An Li, Phys. Rev. Lett. 88, 192701 (2002).

A road map towards determining the nature of neutron-rich nucleonic matter



Hadronic transport equations for the reaction dynamics of nucleus-nucleus collisions:

Baryons:
$$\frac{\partial f_b}{\partial t} + \frac{p}{E_b} \cdot \overline{\nabla}_r f_b - \overline{\nabla}_r U_b \cdot \overline{\nabla}_p f_b = I_{bb}^b + I_{bm}^b$$

Mesons: $\frac{\partial f_m}{\partial t} + \frac{\overline{k}}{E_m} \cdot \overline{\nabla}_r f_m = I_{mm}^m + I_{bm}^m$

An example:

Collision integral $I_{b\pi}^{\pi}$: changing rate of pion phase space distribution $f_{\pi}(\vec{r}, \vec{p}, t)$ due to baryon-pion scatterings



U_b is the mean-field potential for baryons

The phase space distribution functions, mean fields and collisions integrals are all isospin dependent

Simulate solutions of the coupled transport equations using test-particles and Monte Carlo:

$$f(\vec{r},\vec{p},t) \cong \frac{1}{N_t} \sum_i \delta(\vec{r}-\vec{r_i}) \delta(\vec{p}-\vec{p_i})$$

The evolution of $f(\vec{r}, \vec{p}, t)$ is followed on a 6D lattice

$$\begin{split} I_{b\pi}^{\pi}(xk) &= \\ \frac{\pi}{16} \sum_{\alpha\alpha'} \int \int \frac{M_{\alpha}M_{\alpha'}}{E_{\alpha}(p)E_{\alpha'}(p')} W_{b\pi}^{\pi}(\alpha p, \alpha'p', \pi k) \cdot \delta^{(4)}(p'-p-k) \frac{1}{(2\pi)^6} d\vec{p} d\vec{p} \\ [(1+f_{\pi}(xk))f_{\alpha'}(xp')(1-f_{\alpha}(xp)) \text{ (gain)} \\ -f_{\pi}(xk)f_{\alpha}(xp)(1-f_{\alpha'}(xp'))] \text{ (loss)} \end{split}$$

Bao-An Li and Wolfgang Bauer, Phys. Rev. C44, (1991) 450.

<u>Main features</u>:

Pauli bolcking $(1-f_{\alpha})$ for Fermions and Bose enhancement $(1+f_{\pi})$ for bosons are included.

Isospin splitting and momentum dependence of nucleon mean field in neutron-rich matter Predictions of Brueckner-Hartree-Fock including 3-body forces 0 -25 ρ =0.34fm⁻³ $\rho = 0.17 \text{ fm}^{-3}$ U_p(k)(MeV) -50 δ=0.2 -75 ρ=0.085fm⁻³ -100δ=0.8 -125 protons 0 neutrons -25 $U_n(k)(MeV)$ δ=0.8 -50 -75 $U_{n}(k)$ is shifted upwards δ=0.2 compared to $U_{p}(k)$ due to -100 the positive/negative $U_{n/p} = U_0 \pm U_{Lane} \cdot \delta$ symmetry potential for n/p -125 3 2 3 2 2 3 0 0 O $k(fm^{-1})$ $k(fm^{-1})$ $k(fm^{-1})$

The momentum dependence of the nucleon potential is a result of the non-locality of nuclear effective interactions and the Pauli exclusion principle

I. Bombaci and U. Lombardo, Phys. Rev. C44, 1892 (1991);

W. Zuo, L.G. Gao, B.A. Li, U. Lombardo and C.W. Shen, Phys. Rev. C72, 014005 (2005).

Symmetry energy and single nucleon potential used in the IBUU04 transport model



C.B. Das, S. Das Gupta, C. Gale and B.A. Li, PRC 67, 034611 (2003).

B.A. Li, C.B. Das, S. Das Gupta and C. Gale, PRC 69, 034614; NPA 735, 563 (2004).

Nucleon-nucleon cross section in free-space



Neutron-proton effective k-mass splitting in neutron-rich matter at zero temperature



With the modified Gogny effective interaction

Isospin-dependence of nucleon-nucleon cross sections in neutron-rich matter

The effective mass scaling model:

$$\sigma_{medium} / \sigma_{free} \approx \left(\frac{\mu_{NN}^{*}}{\mu_{NN}}\right)^{2}$$

...* is the reduced effective mass

 μ_{NN}^* is the reduced effective mass of the colliding nucleon pair NN

valid for $\rho \le 2\rho_0$ and relative momenta $\le 240 \text{ MeV/c}$ according to Dirac-Brueckner-Hatree-Fock calculations F. Sammarruca and P. Krastev, nucl-th/0506081 Phys. Rev. C (2005) in press.



Application in neutron-rich matter: nn and pp xsections are splitted due to the neutron-proton effective mass slitting

Bao-An Li and Lie-Wen Chen, nucl-th/0508024, Phys. Rev. C (2005) in press.



Nucleon effective masses during heavy-ion reactions

B.A. Li and L.W. Chen, nucl-th/0508024, Phys. Rev. C (2005) in press.



No. of potential colliding nucleon-nucleon pairs during heavy-ion collisions



Reduction factor of their corresponding cross sections in the medium

Promising Probes of the $E_{sym}(\rho)$ in Nuclear Reactions (an incomplete list !)

At sub-saturation densities

- Sizes of n-skins of unstable nuclei from total reaction cross sections
- Proton-nucleus elastic scattering in inverse kinematics
- Parity violating electron scattering studies of the n-skin in ²⁰⁸Pb
- n/p ratio of FAST, pre-equilibrium nucleons
- Isospin fractionation and isoscaling in nuclear multifragmentation
- Isospin diffusion/transport
- Neutron-proton differential flow
- Neutron-proton correlation functions at low relative momenta
- t/³He ratio

Towards high densities reachable at FAIR/GSI, RIA, RIKEN and CSR/China

- π^{-}/π^{+} ratio, K⁺/K⁰ ?
- Neutron-proton differential transverse flow
- n/p ratio at mid-rapidity
- Nucleon elliptical flow at high transverse momenta

(1) Multi-observable correlations are important

(2) Detecting neutrons simultaneously with charged particles is critical

Extract the $E_{sym}(\rho)$ at subnormal densities from isospin diffusion/transport



Nucleon flux:

 $\Gamma_i = \rho_i V_i$

Isospin transport/diffusion:

 $\Gamma_n - \Gamma_p \propto \rho D_I \nabla_r \delta$

A quantitative measure:

$$R_X^{A+B} \equiv \frac{2X^{A+B} - X^{A+A} - X^{B+B}}{X^{A+A} - X^{B+B}}$$

$$R_X^{A+A} = 1$$
 and $R_X^{B+B} = -1$

 $R_X^{A+B} \approx 0$ for complete isospin mixing

X is an isospin-sensitive obseravble, F. Rami et al. (FOPI/GSI), PRL, 84, 1120 (2000).

The degree of isospin transport/diffusion depends on both the symmetry potential and the in-medium neutron-proton scattering cross section.

For near-equilibrium systems, the mean-field contributes:

$$D_I^m \propto dt \bullet F_{np} \propto \frac{1}{\sigma_{np}} \bullet (\frac{\partial \mu_{np}}{\partial \delta} + \frac{4E_{sym}^{int}}{m})$$

During heavy-ion reactions, the collisional contribution to D_1 is expected to be proportional to σ_{np}

L. Shi and P. Danielewicz, Phys. Rev. C68, 017601 (2003).

Isospin transport/diffusion experiments at the NSCL/MSU

Isospin transport in ¹²⁴Sn+¹¹²Sn using ¹¹²Sn+¹¹²Sn and ¹²⁴Sn+¹²⁴Sn as references E_{beam}/A=50 MeV, use X=⁷Li/⁷Be or isospin-asymmetry of the projectile-like residue. *M.B. Tsang et al., Phys. Rev. Lett.* 92, 062701 (2004)



Strength of the symmetry potential at sub-normal densities



Impacts of the symmetry energy constrained by the isospin diffusion data

(2) Cooling mechanisms of proto-neutron stars



Direct URCA processes are possible for neutron stars with central densities ρ_c > 3.5 ρ_0 and masses M>1.39M_{\odot}

A. Akmal, V.R.Pandharipande and D.G. Ravenhall Phys. Rev. C58, 1804 (1998)

Mass-radius correlation of neutron stars and their EOS



J.M. Lattimer and M. Prakash, Science Vol. 304 (2004) 536-542.



Bao-An Li and Andrew W. Steiner, nucl-th/0511064

Masses of canonical neutron stars



S.E. Thorsett and D. Charkrabarty, Astrophysics J. 512, 288 (1999).

Measuring Neutron Star Radii

- Determine luminosity, temperature and deduce surface area. If black body $L=4\pi R_{\infty}^2 \sigma T^4$.
 - T from X-ray spectrum, such as those from Chandra satellite
 - Need distance to star from parallax to get L.
 - Deduce R from surface area (~30% corrections from curvature of spacetime).

The radiation radius for <u>an observer at infinity</u>:

 $R_{\infty} = R(1+z) = R / \sqrt{1 - 2GM} / Rc^{2}$

z is the gravitational redshift and R the matter radius where the pressure vanishes

Complications

– Spectrum peaks in UV and this is heavily absorbed by interstellar H.

- Not a black body: often black body fit to X-ray does not fit visible spectra.
- Model NS atmospheres (composition uncertain) to correct black body.
- Current status: available estimates give a wide range "Although accurate masses of several neutron stars are available, a precise measurement of the radius does not exist yet"..... Lattimer and Prakash, Science Vol. 304 (2004) 536

The Chandra X-Ray Observatory lunched on July 23, 1999

Latest status of the radiation radius R_∞ measured on space x-ray observatories (Chandra and XMM-Newton) --- Bob Rutledge, Oct. 2005

	5.93	22
-	145	
		A. A.

Chandra image of Cas A

The radii are estimated assuming the masses are all $1.4M_{\odot}$ without actually measuring the masses simultaneously because some of them are isolated neutron stars instead of being in a binary

Name	R _∞ (km/D)	D (kpc)	kT _{eff,□} (eV)	N _H (10 ²⁰ cm ⁻²)	Ref.
omega Cen (Chandra)	13.5 ± 2.1	5.36 ±6%	66 ⁺⁴ -5	(9)	Rutledge et al (2002)
omega Cen (XMM)	13.6 ± 0.3	5.36 ±6%	67 ±2	9 ± 2.5	Gendre et al (2002)
M13 (XMM)	12.6 ± 0.4	7.80 ±2%	76 ±3	(1.1)	Gendre et al (2002)
47 Tuc X7 (Chandra)	R=14.51.4 ^{+1.6} (M=1.4)	5.13 ±4%	kT=105 ±6	4.2 +1.8 -1.6	Rybicki et al (2005)
M28 (Chandra)	14.5 _{-3.8} +6.9	5.5 ±10%	90 ₋₁₀ +30	26 ± 4	Becker et al (2003)

The radii of neutron stars are primarily determined by $\frac{dE_{sym}(\rho)}{d\rho}|_{\rho_0}$ unlike other properties, such as the masses

unlike other properties, such as the masses

First found empirically then proven analytically by Prakash and Lattimer, Astro. Phys. Jour. 550, 426 (2001)

Why?

The radius and mass are determined by the Tolman-Oppenheimer-Volkoff eq. for the gravitational equilibrium

$$\frac{dP}{dr} = -\frac{G(e(r) + P(r)/c^2)(m(r) + 4\pi r^3 P(r)/c^2)}{r^2(1 - 2Gm(r)/rc^2)}, \ m(r) = \int_0^r 4\pi r'^2 e(r')dr', \ e(r) \text{ is the energy density at } r$$

the radius is determined by P(R)=0, the pressure P(ρ) at β -equilibrium is obtained from

$$P(\rho,\delta) = P_{\text{nuclear}} + P_{\text{electron}} = \rho_0^2 (\frac{\partial E}{\partial \rho})_{\delta} + \frac{1}{4} \rho_e \mu_e = \rho_0^2 (E_{\text{nuclear matter}}^{'}(\rho) + E_{\text{sym}}^{'}(\rho)\delta^2) + \frac{1}{2}\delta(1-\delta)\rho \cdot E_{\text{sym}}(\rho)$$

with δ determined by the chemical equilibrium condition $\mu_{e} = \mu_{n} - \mu_{p} = 4\delta E_{sym}(\rho)$ and the charge neutrality $\rho_{e} = \rho_{p}$

Example: at ρ_0 , $\delta \approx 0.86$ with $E_{sym}(\rho_0) = 32$ MeV, and $E'_{nuclear matter}(\rho_0) = 0$

thus $P(\rho_0) = \rho_0^2 \delta^2 E'_{sym}(\rho_0) + \frac{1}{2} \delta(1-\delta) \rho \cdot E_{sym}(\rho_0) \approx \rho_0^2 \delta^2 E'_{sym}(\rho_0)$ Most models predict $\mathbf{E}_{sym}^{'}(\rho) \sim E_{sym}^{'}(\rho_0)$ for $\rho \leq 5\rho$

Since the radius is determined by P(R)=0, the R is thus very sensitive to the

behavior of $P(\rho_0) \propto E'_{sym}(\rho_0)$ while the mass $m(r) = \int_{0}^{r} 4\pi r'^2 e(r') dr'$ is sensitive to the EOS at all densities



A.E. L. Dieperink, Y. Dewulf, D. Van Neck, M. Waroquier and V. Rodin, Phys. Rev. C68 (2003) 064307



Pressure forces neutrons out against surface tension. Large pressure gives large neutron skin. $dE_{sym}/d\rho$ determines the size of n-skin and pressure of neutron matter at ρ_0

$$E_{neutron} = E_{nuclear} + E_{sym}, R_n - R_p \propto \Delta p_{np} = dE_{nuclear} / d\rho |_{\rho_0} + dE_{sym} / d\rho |_{\rho_0} = 0 + dE_{sym} / d\rho |_{\rho_0}$$

For the same reason, it is harder for neutrons and protons to mix-up with a larger $dE_{sym}/d\rho$, thus a smaller/slower isospin diffusion \rightarrow correlation of neutron-skin and isospin diffusion *Andrew W. Steiner and Bao-An Li, Phys. Rev. C72, 041601 (2005).*

Constraining the $dE_{\text{sym}}/d\rho$ with data on both isospin diffusion and n-skin in ^{208}Pb





Neutron skin is calculated with Skyrme HF with interactions parameters adjusted such that the same EOS as used in calculating the isospin diffusion is obtained for a given x

Neutron-skin data: V.E. Starodubsky and N.M. Hintz, PRC 49, 2118 (1994);

B.C. Clark, L.J. Kerr and S. Hama, PRC 67, 054605 (2003)



Bao-An Li and Andrew W. Steiner, nucl-th/0511064

Summary

Intermediate energy heavy-ion collisions are a unique tool to study the isospin dependence of strong interactions, it is a fundamental quantity for understanding the nature of neutron-rich matter and has significant ramifications in astrophysics (Hope the director, Prof. E. Migneco will consider this in making the future plan for the INFN-LNS)



Looking forward and driving away from the valley of stability \rightarrow EOS of dense n-rich matter





- How supernovae explode
- How heavy elements are formed in the universe
- What are the properties of n-stars
- What is the critical M/R ratio of a neutron star before it becomes a black hole when the neutron degenerate pressure in the star can no longer support its gravity
- Isospin dependence of in-medium nuclear effective interactions