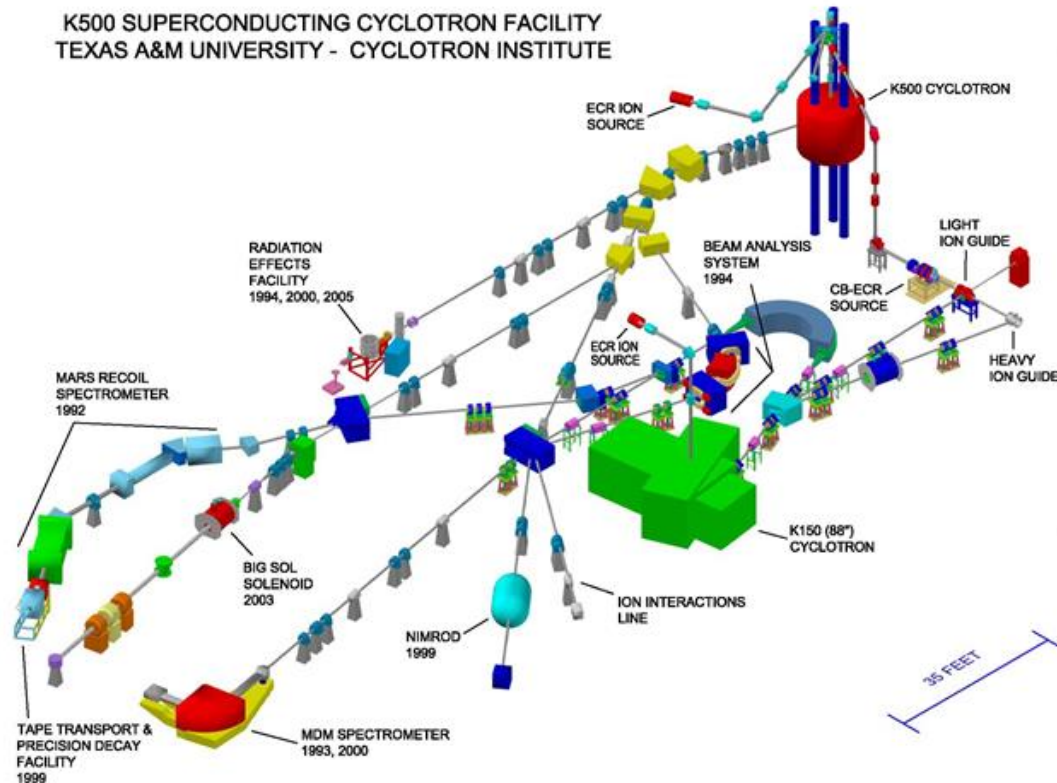


# Nuclear Reactions

## Where Would We Be Without Them?

J. Natowitz



**T-REX**  
[ TAMU  
Reaccelerated  
EXotics]

# Periodic Table of the Elements

1 1IA 11A	2 IIA 2A											13 IIIA 3A	14 IVA 4A	15 VA 5A	16 VIA 6A	17 VIIA 7A	18 VIIIA 8A
1 H Hydrogen 1.0079																	2 He Helium 4.0026
3 Li Lithium 6.941	4 Be Beryllium 9.01218											5 B Boron 10.811	6 C Carbon 12.011	7 N Nitrogen 14.00674	8 O Oxygen 15.9994	9 F Fluorine 18.998403	10 Ne Neon 20.1797
11 Na Sodium 22.989769	12 Mg Magnesium 24.305	3 IIIB 3B	4 IVB 4B	5 VB 5B	6 VIB 6B	7 VIIB 7B	8 VIII 8	9 VIII 8	10 VIII 8	11 IB 1B	12 IIB 2B	13 Al Aluminum 26.981539	14 Si Silicon 28.0855	15 P Phosphorus 30.973762	16 S Sulfur 32.066	17 Cl Chlorine 35.4527	18 Ar Argon 39.948
19 K Potassium 39.0983	20 Ca Calcium 40.078	21 Sc Scandium 44.95591	22 Ti Titanium 47.88	23 V Vanadium 50.9415	24 Cr Chromium 51.9961	25 Mn Manganese 54.938	26 Fe Iron 55.847	27 Co Cobalt 58.9332	28 Ni Nickel 58.6934	29 Cu Copper 63.546	30 Zn Zinc 65.39	31 Ga Gallium 69.723	32 Ge Germanium 72.64	33 As Arsenic 74.92159	34 Se Selenium 78.96	35 Br Bromine 79.904	36 Kr Krypton 83.80
37 Rb Rubidium 85.4678	38 Sr Strontium 87.62	39 Y Yttrium 88.90585	40 Zr Zirconium 91.224	41 Nb Niobium 92.90638	42 Mo Molybdenum 95.94	43 Tc Technetium 98.9062	44 Ru Ruthenium 101.07	45 Rh Rhodium 102.9055	46 Pd Palladium 106.42	47 Ag Silver 107.8682	48 Cd Cadmium 112.411	49 In Indium 114.818	50 Sn Tin 118.71	51 Sb Antimony 121.760	52 Te Tellurium 127.6	53 I Iodine 126.90447	54 Xe Xenon 131.29
55 Cs Cesium 132.90545	56 Ba Barium 137.327	57-71	72 Hf Hafnium 178.49	73 Ta Tantalum 180.9479	74 W Tungsten 183.85	75 Re Rhenium 186.207	76 Os Osmium 190.23	77 Ir Iridium 192.22	78 Pt Platinum 195.08	79 Au Gold 196.9666	80 Hg Mercury 200.59	81 Tl Thallium 204.3833	82 Pb Lead 207.2	83 Bi Bismuth 208.98039	84 Po Polonium [209]	85 At Astatine 208.9804	86 Rn Radon 222.0176
87 Fr Francium [223]	88 Ra Radium 226.0254	89-103	104 Rf Rutherfordium [261]	105 Db Dubnium [262]	106 Sg Seaborgium [266]	107 Bh Bohrium [264]	108 Hs Hassium [265]	109 Mt Meitnerium [268]	110 Ds Darmstadtium [281]	111 Rg Roentgenium [272]	112 Cn Copernicium [277]	113 Uut Ununtrium unknown	114 Uuq Ununquadium [286]	115 Uup Ununpentium unknown	116 Uuh Ununhexium [284]	117 Uus Ununseptium unknown	118 Uuo Ununoctium unknown

Lanthanide Series

57 La Lanthanum 138.9055	58 Ce Cerium 140.12	59 Pr Praseodymium 140.90766	60 Nd Neodymium 144.24	61 Pm Promethium 144.9127	62 Sm Samarium 150.36	63 Eu Europium 151.9654	64 Gd Gadolinium 157.25	65 Tb Terbium 158.92534	66 Dy Dysprosium 162.50	67 Ho Holmium 164.93033	68 Er Erbium 167.26	69 Tm Thulium 168.93421	70 Yb Ytterbium 173.04	71 Lu Lutetium 174.967
-----------------------------------	------------------------------	---------------------------------------	---------------------------------	------------------------------------	--------------------------------	----------------------------------	----------------------------------	----------------------------------	----------------------------------	----------------------------------	------------------------------	----------------------------------	---------------------------------	---------------------------------

Actinide Series

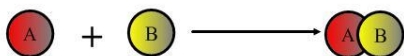
89 Ac Actinium 227.0277	90 Th Thorium 232.0377	91 Pa Protactinium 231.03626	92 U Uranium 238.02891	93 Np Neptunium 237.04817	94 Pu Plutonium 244.06422	95 Am Americium 243.06136	96 Cm Curium 247.07035	97 Bk Berkelium 247.07035	98 Cf Californium 251.07958	99 Es Einsteinium [252]	100 Fm Fermium [257]	101 Md Mendelevium [258]	102 No Nobelium [259]	103 Lr Lawrencium [260]
----------------------------------	---------------------------------	---------------------------------------	---------------------------------	------------------------------------	------------------------------------	------------------------------------	---------------------------------	------------------------------------	--------------------------------------	----------------------------------	-------------------------------	-----------------------------------	--------------------------------	----------------------------------

Akali Metal	Alkali Earth	Transition Metal	Basic Metal	Semimetals	Nonmetals	Halogens	Noble Gas	Lanthanides	Actinides
-------------	--------------	------------------	-------------	------------	-----------	----------	-----------	-------------	-----------

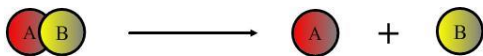


### Types of Chemical Reactions

**A) Synthesis Reactions:** two reactants combine to make a larger product

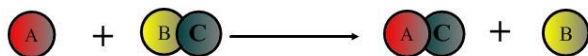


**B) Decomposition Reactions:** larger reactant breaks down to form 2 or more simple products



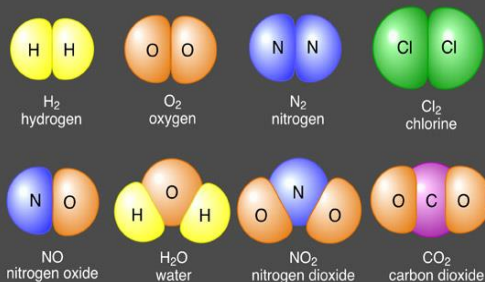
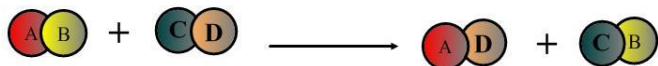
**C) Single Displacement Reactions:**

one element displaces or replaces an element in a compound

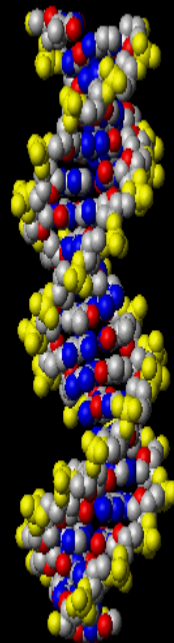
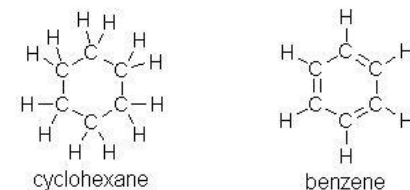
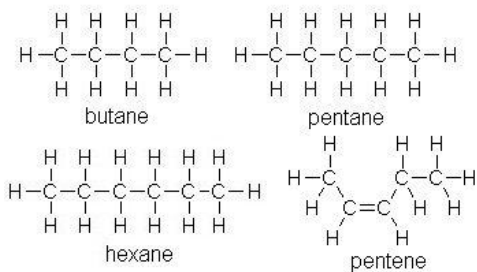
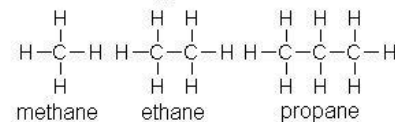


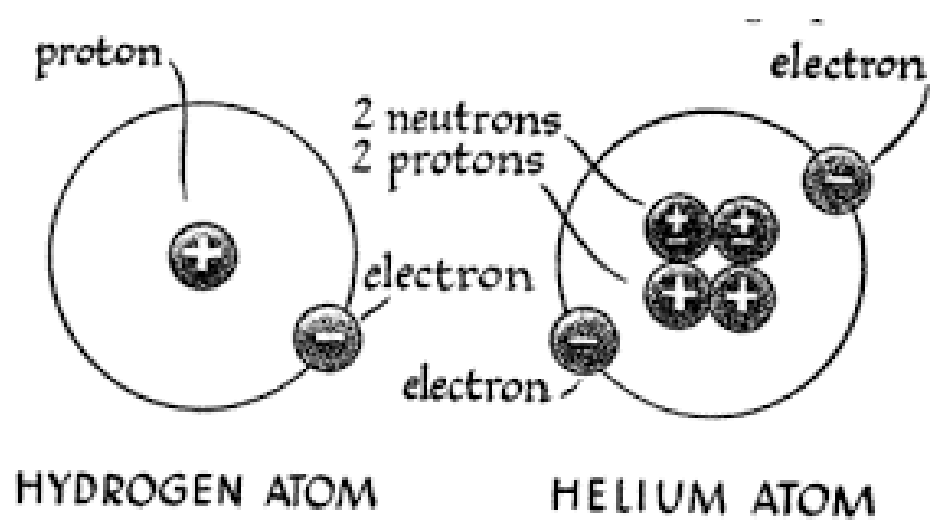
**D) Double Displacement Reactions:**

two elements in different compounds trade places



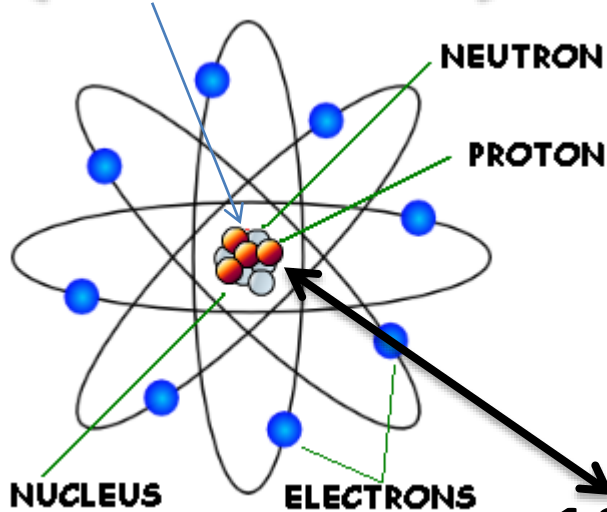
### Some Organic Molecules





# The Atom

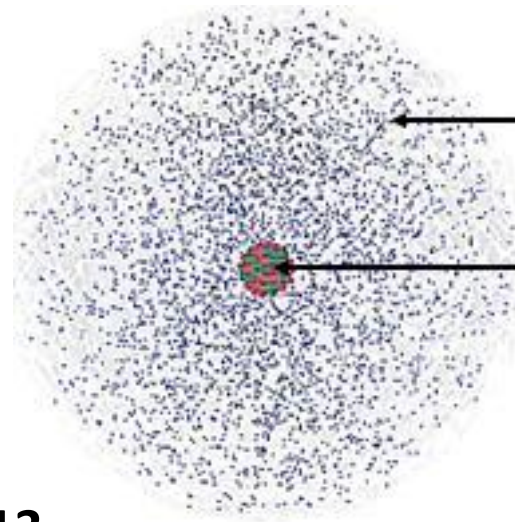
Classical  
 $10^{-8}$  cm



$10^{-13}$  cm

Quantum Mechanical

$10^{-13}$  cm

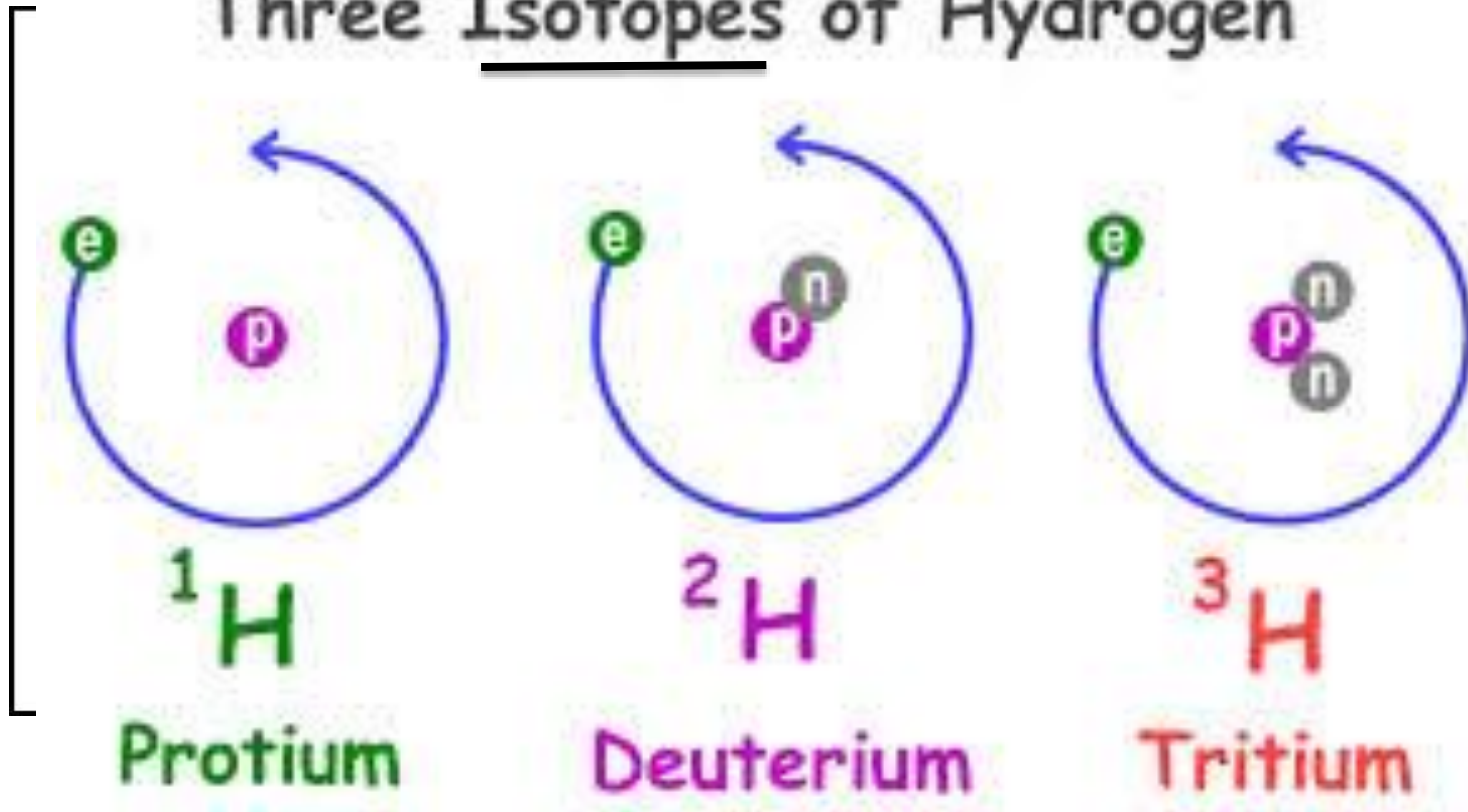


Electron cloud

Nucleus

# All Atoms With One Proton in the Nucleus are Hydrogen Atoms

## Three Isotopes of Hydrogen



There are many possible isotopes of each element.

# Periodic Table of the Elements

1 1IA 11A	2 IIA 2A											13 IIIA 3A	14 IVA 4A	15 VA 5A	16 VIA 6A	17 VIIA 7A	18 VIIIA 8A		
1 H Hydrogen 1.0079	2 He Helium 4.0026											3 Li Lithium 6.941	4 Be Beryllium 9.01218	5 B Boron 10.811	6 C Carbon 12.011	7 N Nitrogen 14.00674	8 O Oxygen 15.9994	9 F Fluorine 18.998403	10 Ne Neon 20.1797
11 Na Sodium 22.989769	12 Mg Magnesium 24.305	3 IIIB 3B	4 IVB 4B	5 VB 5B	6 VIB 6B	7 VIIB 7B	8 VIII 8	9 VIII 8	10 VIII 8	11 IB 1B	12 IIB 2B	13 Al Aluminum 26.981539	14 Si Silicon 28.0855	15 P Phosphorus 30.973762	16 S Sulfur 32.066	17 Cl Chlorine 35.4527	18 Ar Argon 39.948		
19 K Potassium 39.0983	20 Ca Calcium 40.078	21 Sc Scandium 44.95591	22 Ti Titanium 47.88	23 V Vanadium 50.9415	24 Cr Chromium 51.9961	25 Mn Manganese 54.938	26 Fe Iron 55.847	27 Co Cobalt 58.9332	28 Ni Nickel 58.6934	29 Cu Copper 63.546	30 Zn Zinc 65.39	31 Ga Gallium 69.723	32 Ge Germanium 72.64	33 As Arsenic 74.92159	34 Se Selenium 78.96	35 Br Bromine 79.904	36 Kr Krypton 83.80		
37 Rb Rubidium 85.4678	38 Sr Strontium 87.62	39 Y Yttrium 88.90585	40 Zr Zirconium 91.224	41 Nb Niobium 92.90638	42 Mo Molybdenum 95.94	43 Tc Technetium 98.9062	44 Ru Ruthenium 101.07	45 Rh Rhodium 102.9055	46 Pd Palladium 106.42	47 Ag Silver 107.8682	48 Cd Cadmium 112.411	49 In Indium 114.818	50 Sn Tin 118.71	51 Sb Antimony 121.760	52 Te Tellurium 127.6	53 I Iodine 126.90447	54 Xe Xenon 131.29		
55 Cs Cesium 132.90545	56 Ba Barium 137.327	57-71	72 Hf Hafnium 178.49	73 Ta Tantalum 180.9479	74 W Tungsten 183.85	75 Re Rhenium 186.207	76 Os Osmium 190.23	77 Ir Iridium 192.22	78 Pt Platinum 195.08	79 Au Gold 196.9666	80 Hg Mercury 200.59	81 Tl Thallium 204.3833	82 Pb Lead 207.2	83 Bi Bismuth 208.98039	84 Po Polonium [209]	85 At Astatine 209	86 Rn Radon 222.01758		
87 Fr Francium [223]	88 Ra Radium 226.0254	89-103	104 Rf Rutherfordium [261]	105 Db Dubnium [262]	106 Sg Seaborgium [266]	107 Bh Bohrium [264]	108 Hs Hassium [265]	109 Mt Meitnerium [268]	110 Ds Darmstadtium [281]	111 Rg Roentgenium [272]	112 Cn Copernicium [277]	113 Uut Ununtrium unknown	114 Uuq Ununquadium [286]	115 Uup Ununpentium unknown	116 Uuh Ununhexium [286]	117 Uus Ununseptium unknown	118 Uuo Ununoctium unknown		

Lanthanide Series

57 La Lanthanum 138.9055	58 Ce Cerium 140.12	59 Pr Praseodymium 140.90766	60 Nd Neodymium 144.24	61 Pm Promethium 144.9127	62 Sm Samarium 150.36	63 Eu Europium 151.9654	64 Gd Gadolinium 157.25	65 Tb Terbium 158.92534	66 Dy Dysprosium 162.50	67 Ho Holmium 164.93033	68 Er Erbium 167.26	69 Tm Thulium 168.93421	70 Yb Ytterbium 173.04	71 Lu Lutetium 174.967
-----------------------------------	------------------------------	---------------------------------------	---------------------------------	------------------------------------	--------------------------------	----------------------------------	----------------------------------	----------------------------------	----------------------------------	----------------------------------	------------------------------	----------------------------------	---------------------------------	---------------------------------

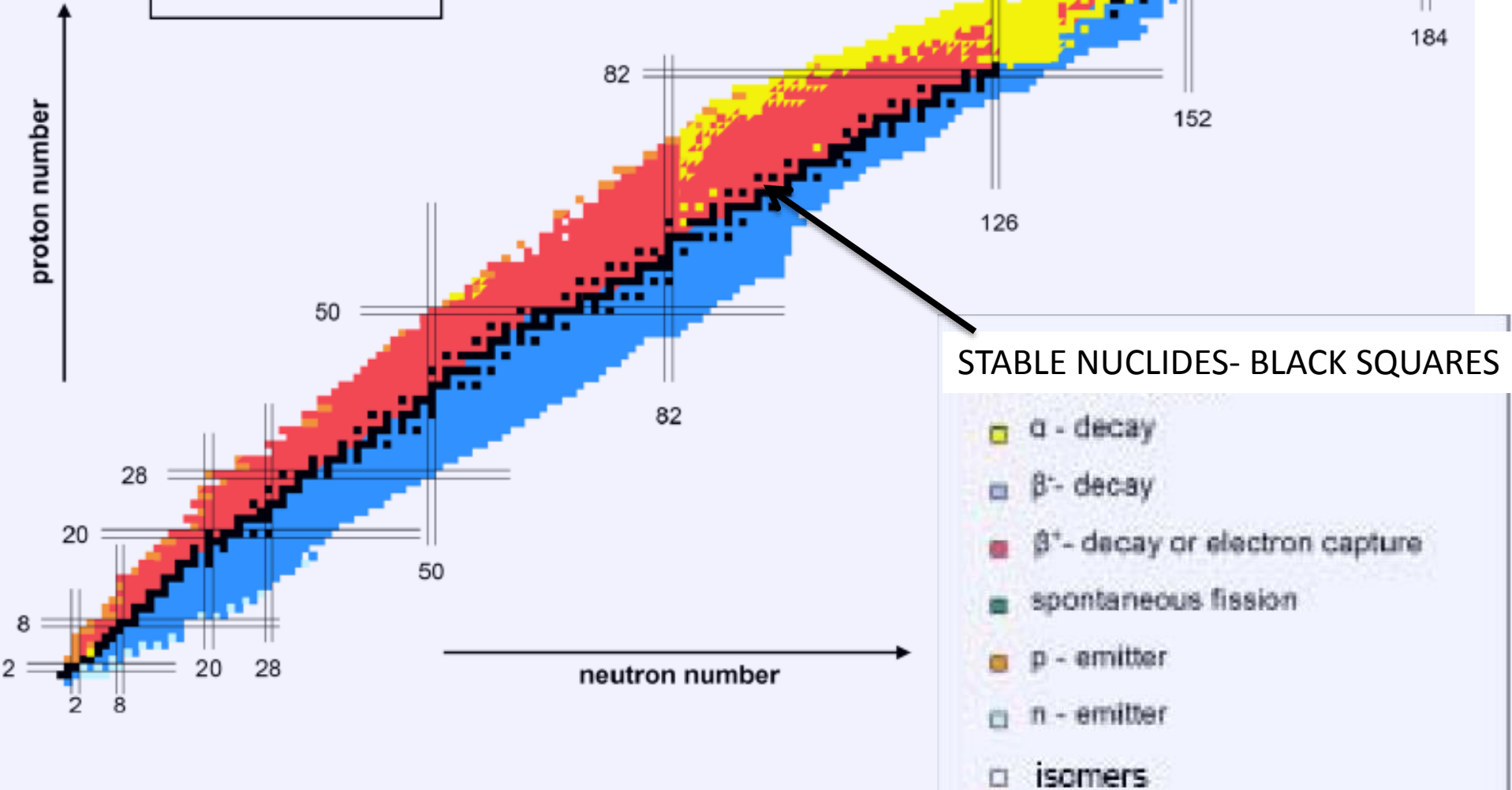
Actinide Series

89 Ac Actinium 207.0289	90 Th Thorium 232.0377	91 Pa Protactinium 231.03689	92 U Uranium 238.02891	93 Np Neptunium 237.04817	94 Pu Plutonium 244.0642	95 Am Americium 243.0613	96 Cm Curium 247.0703	97 Bk Berkelium 247.0703	98 Cf Californium 251.07958	99 Es Einsteinium [252]	100 Fm Fermium [257]	101 Md Mendelevium [258]	102 No Nobelium [259]	103 Lr Lawrencium [260]
----------------------------------	---------------------------------	---------------------------------------	---------------------------------	------------------------------------	-----------------------------------	-----------------------------------	--------------------------------	-----------------------------------	--------------------------------------	----------------------------------	-------------------------------	-----------------------------------	--------------------------------	----------------------------------

Alkali Metal	Alkaline Earth	Transition Metal	Basic Metal	Semimetals	Nonmetals	Halogens	Noble Gas	Lanthanides	Actinides
--------------	----------------	------------------	-------------	------------	-----------	----------	-----------	-------------	-----------

# Chart of the Nuclides 2009

nuclei total: 2974  
in nature: 286





# Nuclear Binding Energy

Consider the formation of an atom from its constituents



- Define binding energy as the mass difference between the sum of the mass of free constituents (protons, neutrons, electrons) and the mass of the nucleus

$$E_B = [ ( Z \times M_H + N \times M_N - M(A,Z) ) c^2 ]$$

$$c^2 = 931.5 \text{ MeV/u}$$

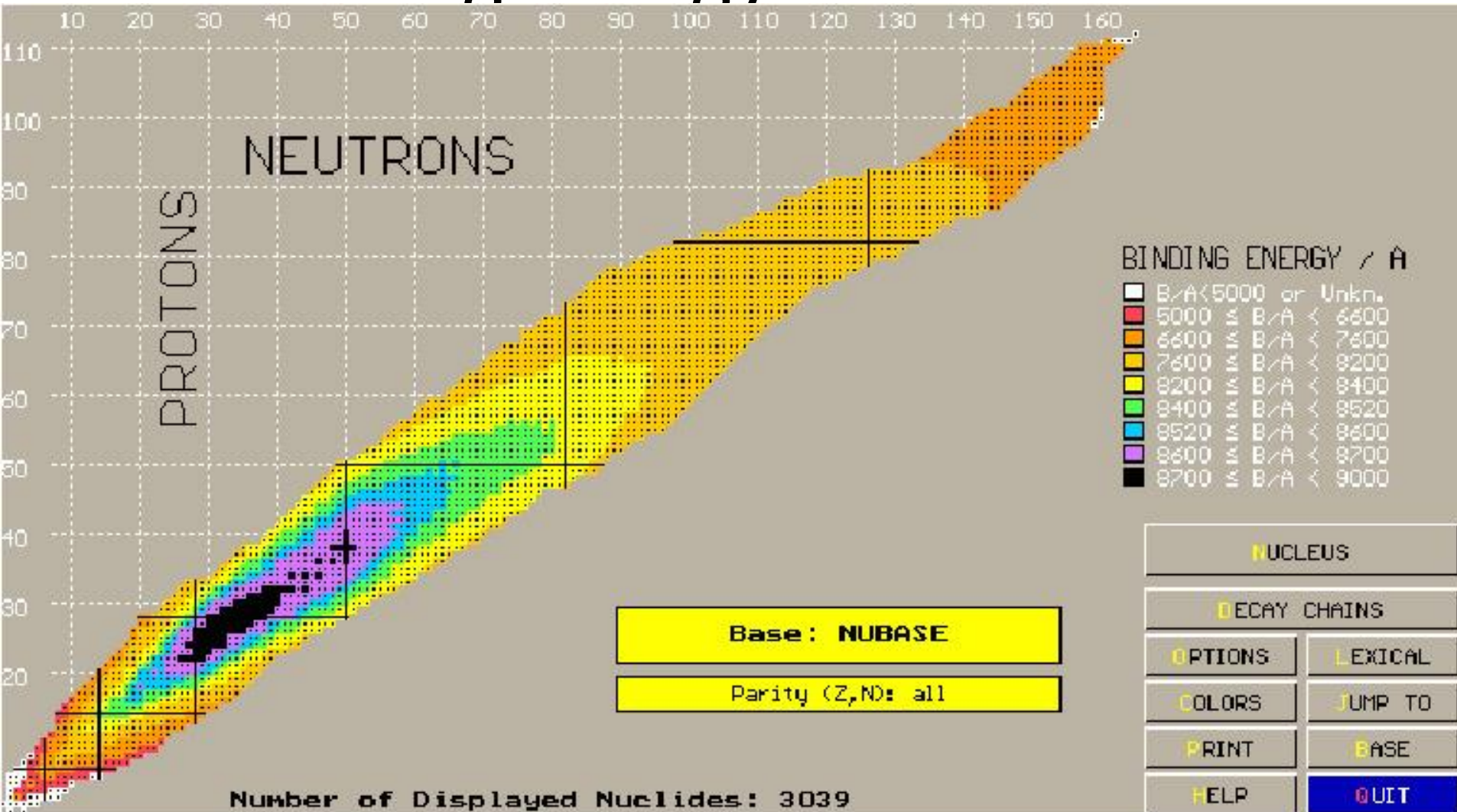
- **Binding Energy**

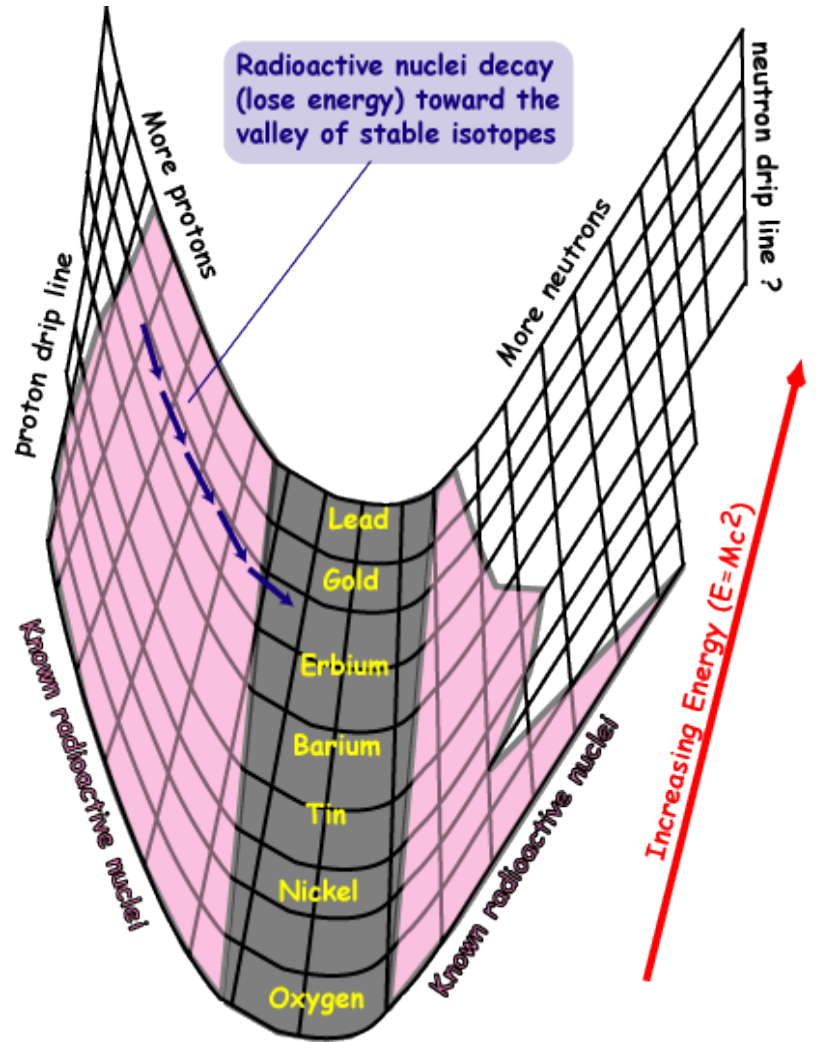
- The difference in mass between the constituent protons, electrons and neutrons and that of the isotope formed converted into energy, usually in MeV.
- For  $^{208}\text{Pb}$   $\text{BE} = 1636 \text{ MeV}$

- **Binding Energy per Nucleon**

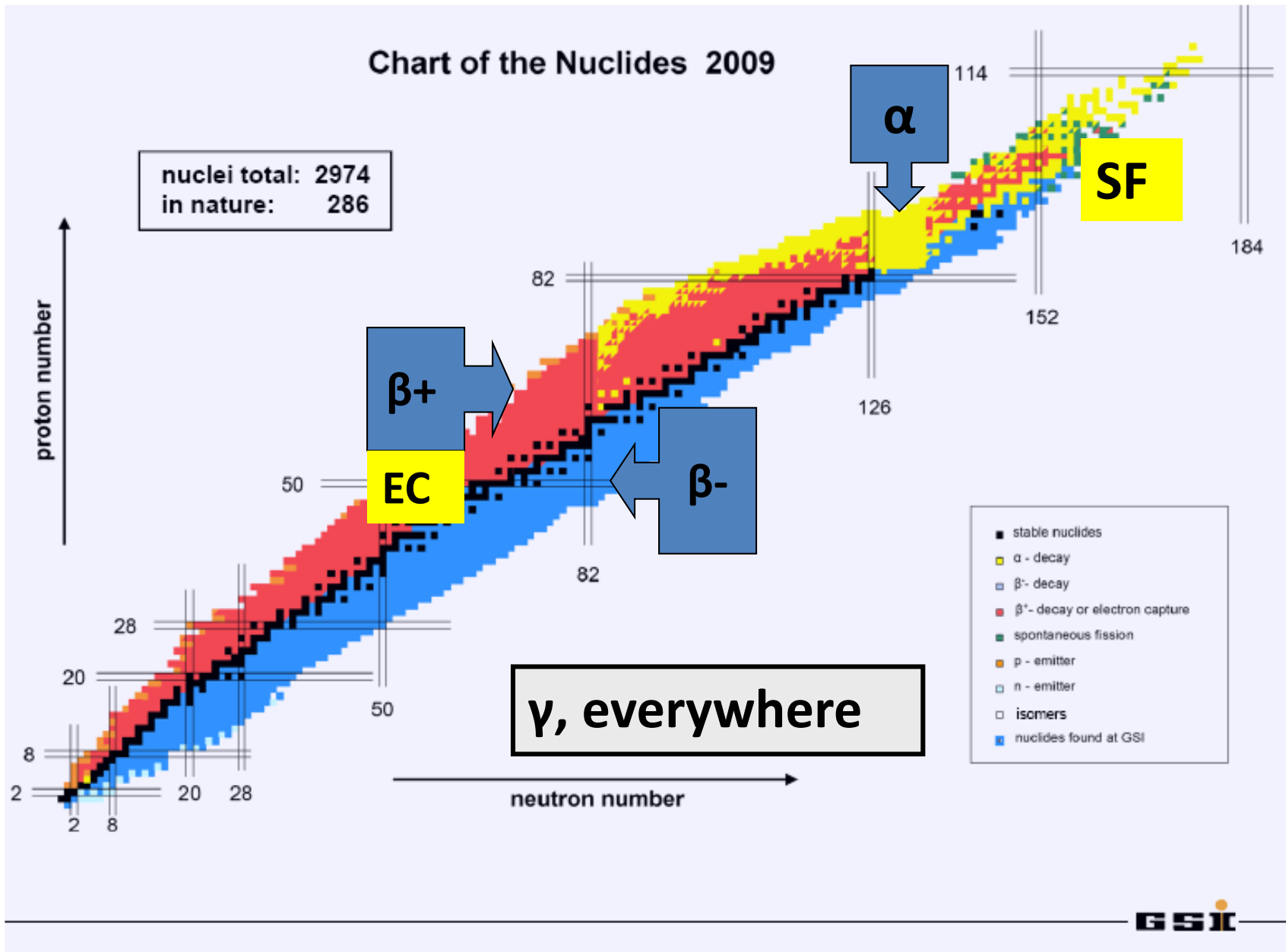
- The Binding energy divided by A, the total number of nucleons.
- For  $^{208}\text{Pb}$   $\text{BE} = 1636/208 = 7.87 \text{ MeV/nucleon}$

# Binding Energy Per Nucleon

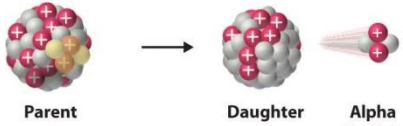

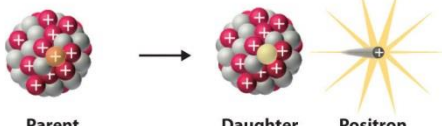


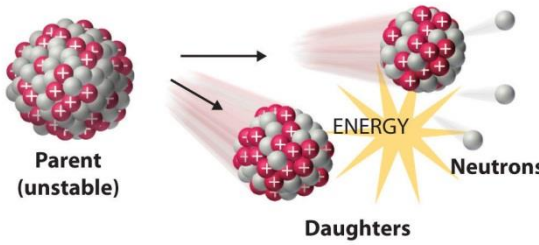




# Most Isotopes are Radioactive

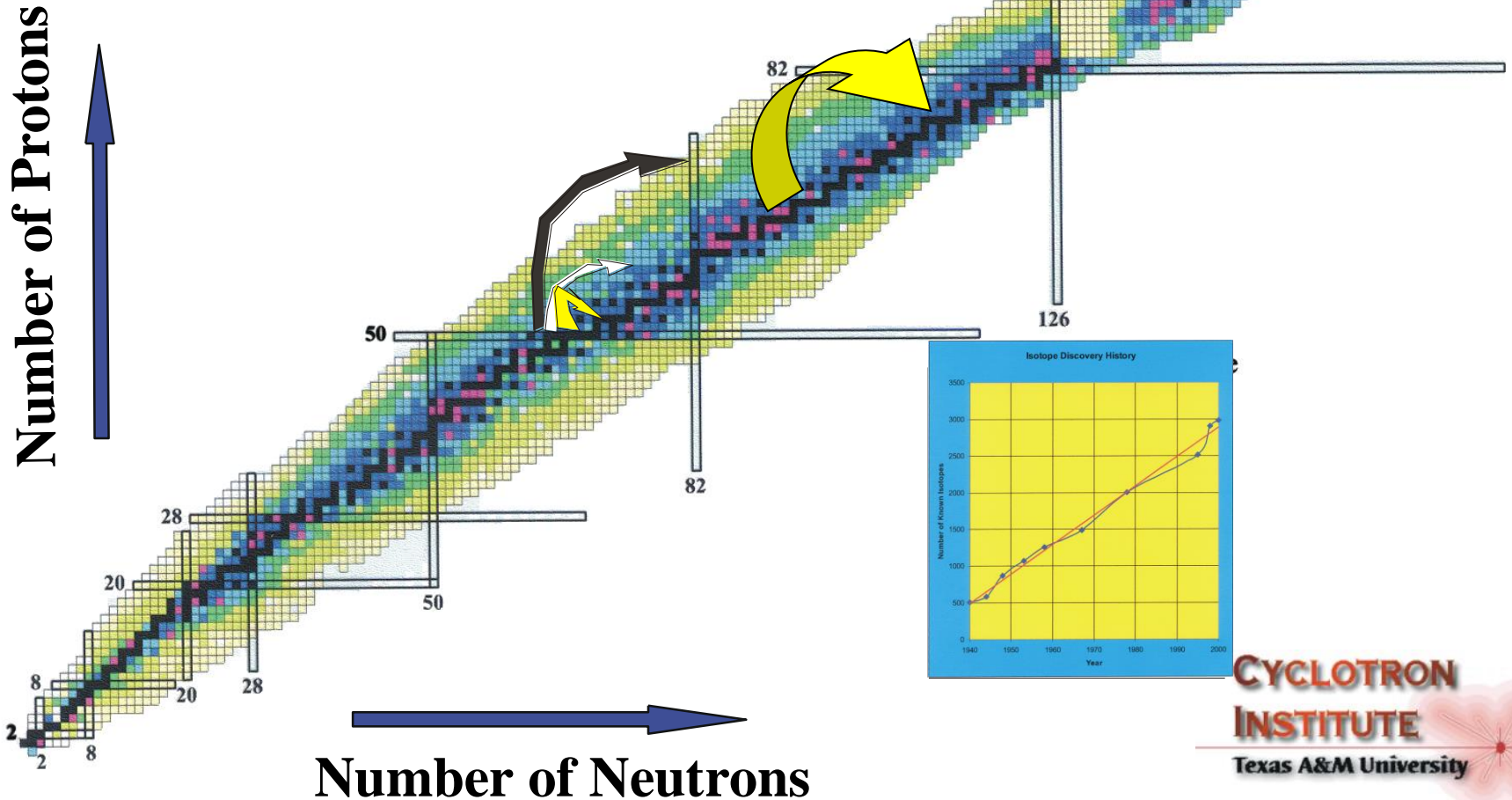


**Note:**  
**In these**  
**three,**  
**neutrinos**  
**are also**  
**emitted**

Decay Type	Radiation Emitted	Generic Equation	Model
Alpha decay	${}^4_2\alpha$	${}^A_ZX \longrightarrow {}^{A-4}_{Z-2}X' + \frac{4}{2}\alpha$	 <p>Parent → Daughter + Alpha Particle</p>
Beta decay	${}^0_{-1}\beta$	${}^A_ZX \longrightarrow {}^A_{Z+1}X' + {}^0_{-1}\beta$	 <p>Parent → Daughter + Beta Particle</p>
Positron emission	${}^0_{+1}\beta$	${}^A_ZX \longrightarrow {}^A_{Z-1}X' + {}^0_{+1}\beta$	 <p>Parent → Daughter + Positron</p>
Electron capture	X rays	${}^A_ZX + {}^0_{-1}e \longrightarrow {}^A_{Z-1}X' + \text{X ray}$	 <p>Parent + Electron → Daughter + X ray</p>
Gamma emission	${}^0_0\gamma$	${}^A_ZX^* \xrightarrow{\text{Relaxation}} {}^A_ZX' + {}^0_0\gamma$	 <p>Parent (excited nuclear state) → Daughter + Gamma ray</p>
Spontaneous fission	Neutrons	${}^{A+B+C}_{Z+Y}X \longrightarrow {}^A_ZX' + {}^B_YX' + C{}_0^1n$	 <p>Parent (unstable) → Daughters + Neutrons + ENERGY</p>

# Reversing the Trend -- Nuclear Reactions

*Experimental Chart of Nuclides 2000*  
2975 isotopes



# NEED AN ACCELERATOR

K500 SUPERCONDUCTING CYCLOTRON FACILITY  
TEXAS A&M UNIVERSITY - CYCLOTRON INSTITUTE

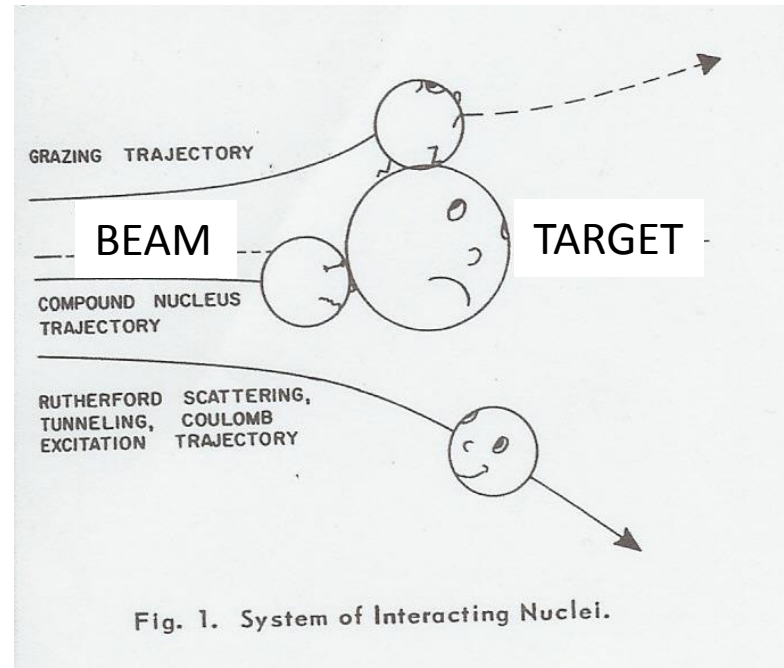
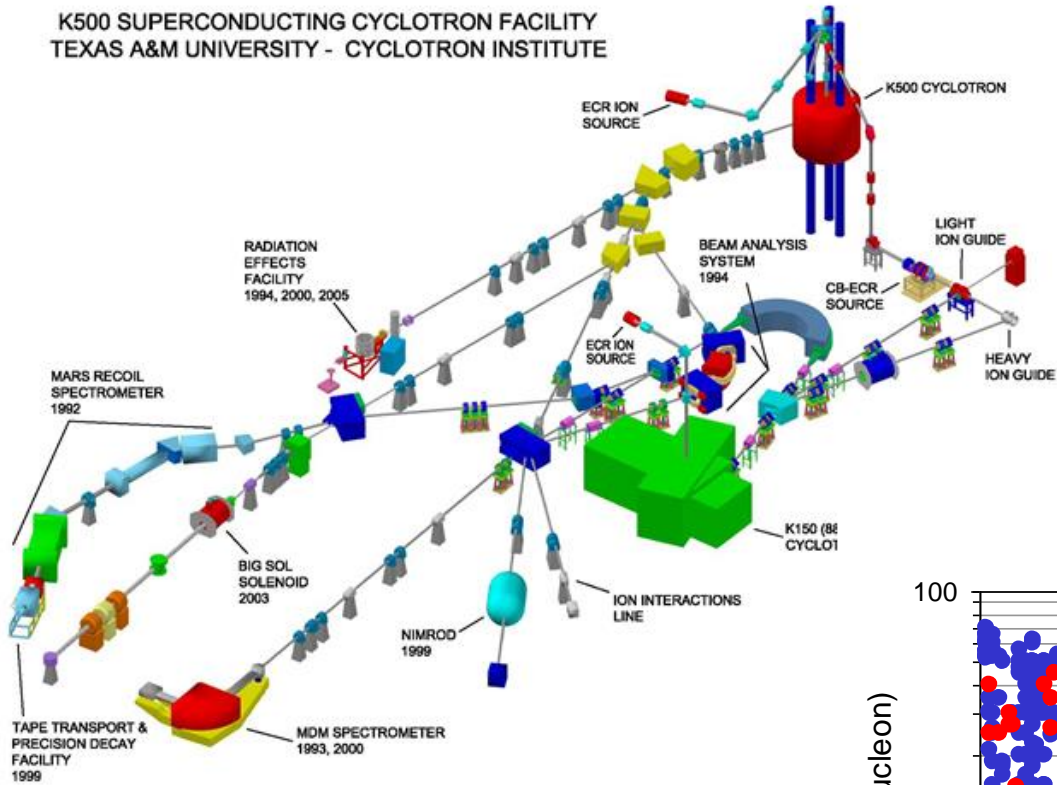
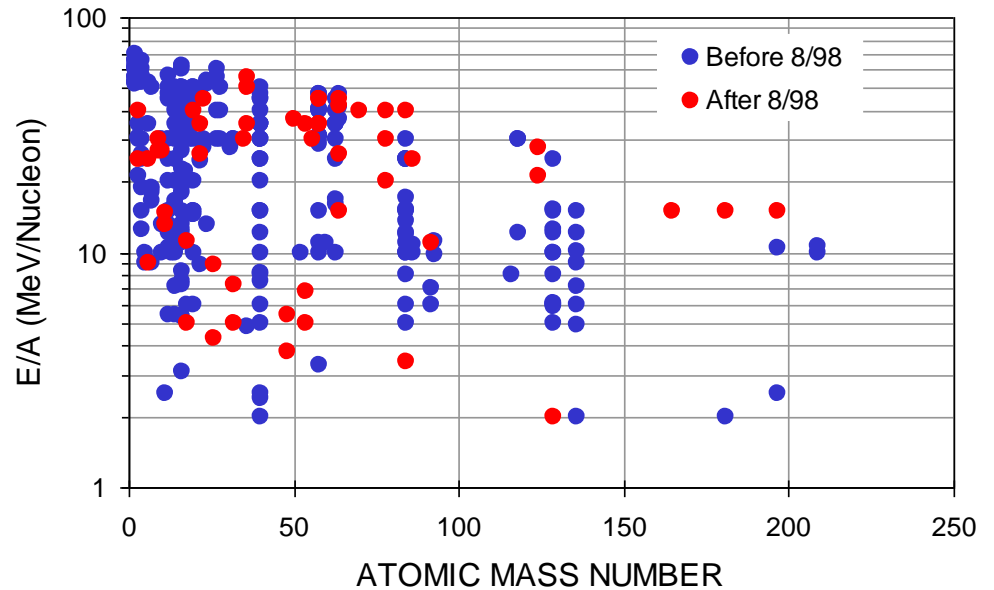


Fig. 1. System of Interacting Nuclei.

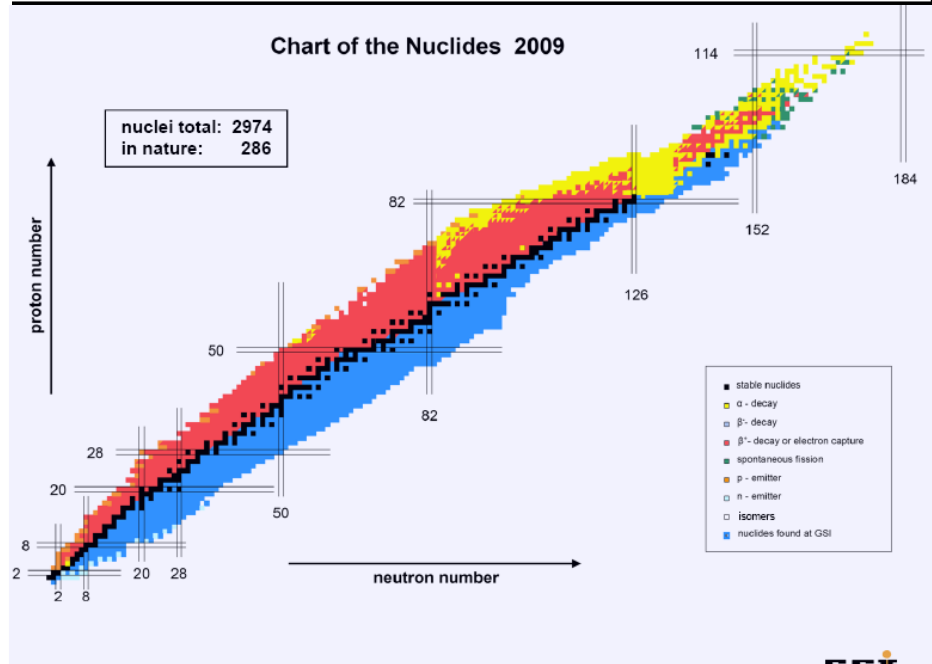
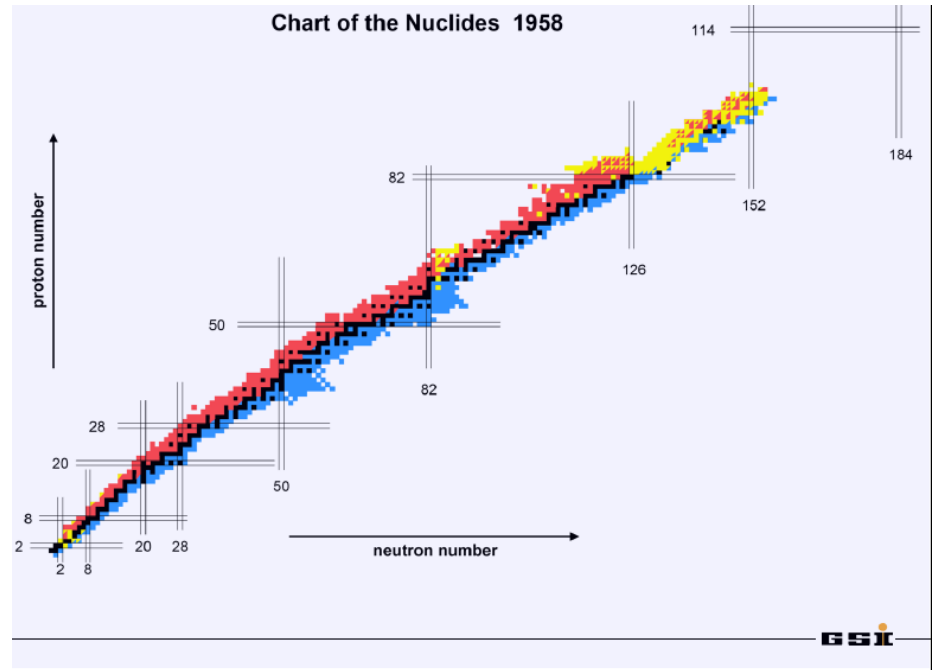
K500 CYCLOTRON + ECR





# 1958-My first course in nuclear chemistry

- With such reactions new isotopes  
and  
new elements  
can be made



# Synthesis of superheavy elements (cold and hot fusion)



**Cold synthesis:**

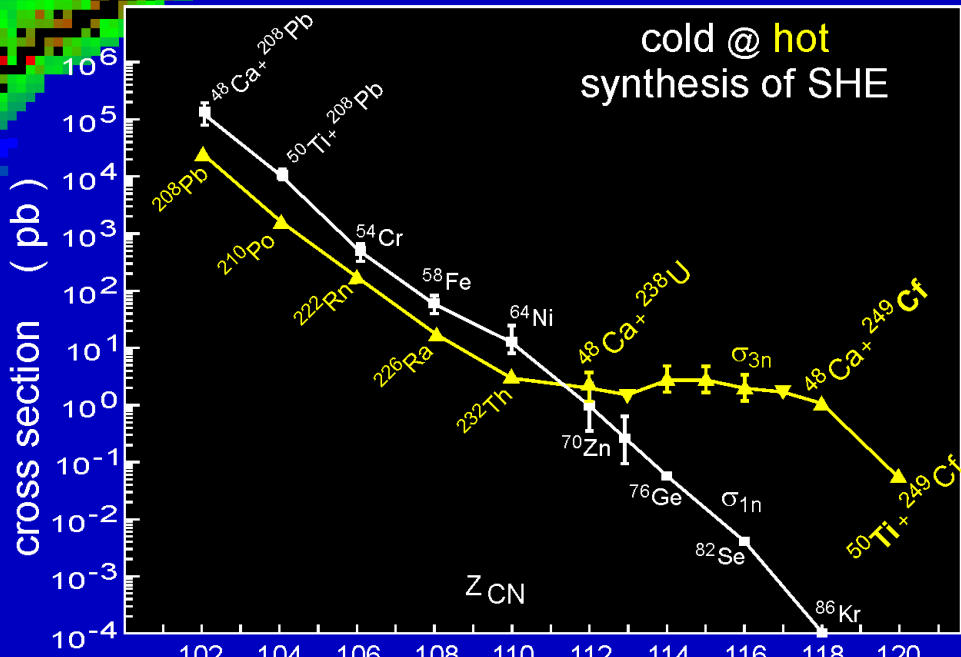
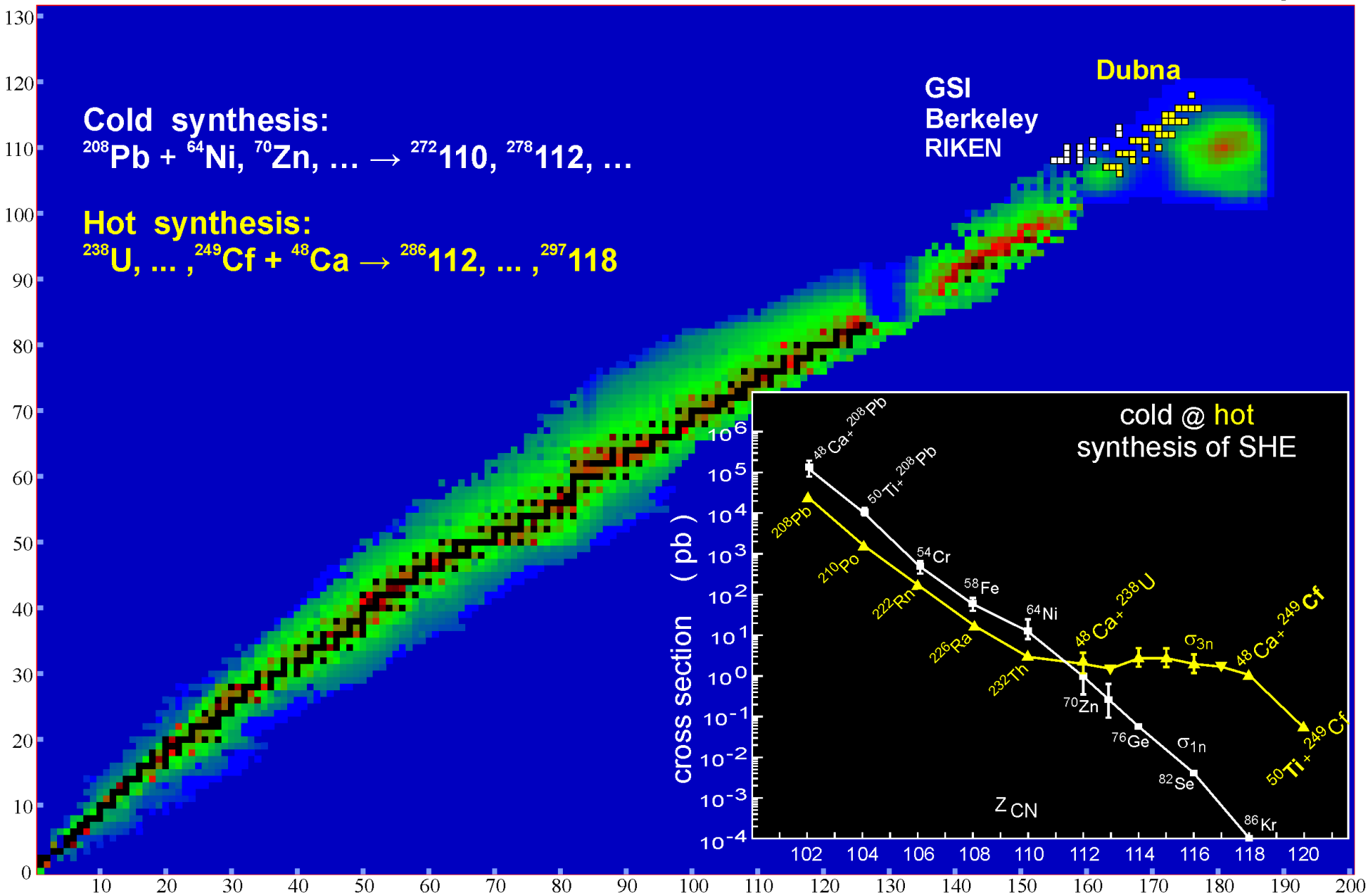


**Hot synthesis:**



GSI  
Berkeley  
RIKEN

Dubna

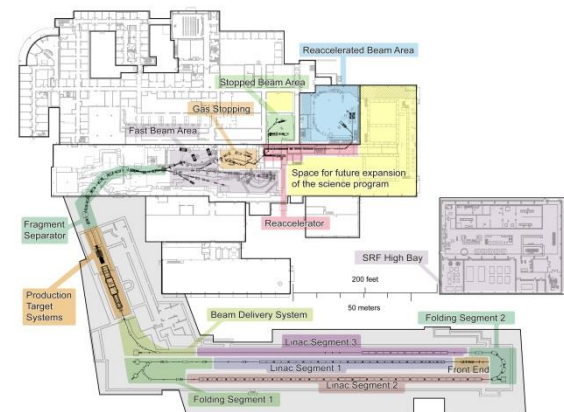
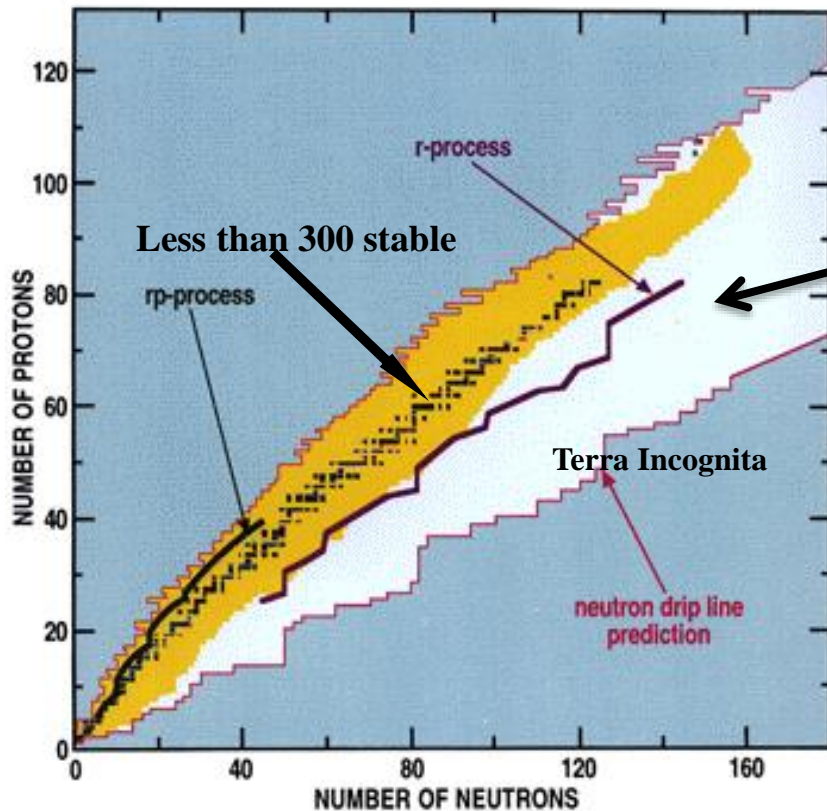


# Periodic Table of the Elements

1 1IA 11A											2 VIII 8A						
1 H Hydrogen 1.0079											2 He Helium 4.00260						
3 Li Lithium 6.941	4 Be Beryllium 9.01218											6 B Boron 10.811	7 C Carbon 12.011	8 N Nitrogen 14.00674	9 O Oxygen 15.9994	10 F Fluorine 18.998403	11 Ne Neon 20.1797
11 Na Sodium 22.989769	12 Mg Magnesium 24.305	3 IIIB 3B	4 IVB 4B	5 VB 5B	6 VIB 6B	7 VIIB 7B	8 VIII 8	9 VIII 8	10 VIII 8	11 IB 1B	12 IIB 2B	13 Al Aluminum 26.981539	14 Si Silicon 28.0855	15 P Phosphorus 30.973762	16 S Sulfur 32.065	17 Cl Chlorine 35.4527	18 Ar Argon 39.948
19 K Potassium 39.0983	20 Ca Calcium 40.078	21 Sc Scandium 44.95591	22 Ti Titanium 47.88	23 V Vanadium 50.9415	24 Cr Chromium 51.9961	25 Mn Manganese 54.938	26 Fe Iron 55.847	27 Co Cobalt 58.9332	28 Ni Nickel 58.6934	29 Cu Copper 63.546	30 Zn Zinc 65.39	31 Ga Gallium 69.723	32 Ge Germanium 72.64	33 As Arsenic 74.921595	34 Se Selenium 78.96	35 Br Bromine 79.904	36 Kr Krypton 83.80
37 Rb Rubidium 85.4678	38 Sr Strontium 87.62	39 Y Yttrium 88.90585	40 Zr Zirconium 91.224	41 Nb Niobium 92.90638	42 Mo Molybdenum 95.94	43 Tc Technetium 98.9062	44 Ru Ruthenium 101.07	45 Rh Rhodium 102.9055	46 Pd Palladium 106.42	47 Ag Silver 107.8682	48 Cd Cadmium 112.411	49 In Indium 114.818	50 Sn Tin 118.71	51 Sb Antimony 121.757	52 Te Tellurium 127.6	53 I Iodine 126.90447	54 Xe Xenon 131.29
55 Cs Cesium 132.90545	56 Ba Barium 137.327	57-71 Lanthanide Series	72 Hf Hafnium 178.49	73 Ta Tantalum 180.9479	74 W Tungsten 183.85	75 Re Rhenium 186.207	76 Os Osmium 190.23	77 Ir Iridium 192.222	78 Pt Platinum 195.084	79 Au Gold 196.96657	80 Hg Mercury 200.59	81 Tl Thallium 204.3833	82 Pb Lead 207.2	83 Bi Bismuth 208.9804	84 Po Polonium [209]	85 At Astatine [210]	86 Rn Radon [222]
87 Fr Francium [223]	88 Ra Radium [226]	89-103 Actinide Series	104 Rf Rutherfordium [261]	105 Db Dubnium [262]	106 Sg Seaborgium [263]	107 Bh Bohrium [264]	108 Hs Hassium [265]	109 Mt Meitnerium [266]	110 Ds Darmstadtium [267]	111 Rg Roentgenium [268]	112 Cn Copernicium [269]	113 Uut Ununtrium [271]	114 Uuq Ununquadium [272]	115 Uup Ununpentium [273]	116 Uuh Ununhexium [274]	117 Uus Ununseptium [275]	118 Uuo Ununoctium [276]
Lanthanide Series			57 La Lanthanum 138.9055	58 Ce Cerium 140.12	59 Pr Praseodymium 140.90766	60 Nd Neodymium 144.24	61 Pm Promethium [145]	62 Sm Samarium [147]	63 Eu Europium [152]	64 Gd Gadolinium [157]	65 Tb Terbium [159]	66 Dy Dysprosium [163]	67 Ho Holmium [165]	68 Er Erbium [167]	69 Tm Thulium [169]	70 Yb Ytterbium [173]	71 Lu Lutetium [175]
Actinide Series			89 Ac Actinium [227]	90 Th Thorium [232]	91 Pa Protactinium [231]	92 U Uranium [238]	93 Np Neptunium [237]	94 Pu Plutonium [244]	95 Am Americium [243]	96 Cm Curium [247]	97 Bk Berkelium [247]	98 Cf Californium [251]	99 Es Einsteinium [252]	100 Fm Fermium [257]	101 Md Mendelevium [258]	102 No Nobelium [259]	103 Lr Lawrencium [260]
Alkali Metal	Alkaline Earth	Transition Metal	Basic Metal	Semimetal	Nonmetal	Halogen	Noble Gas	Lanthanides	Actinides								

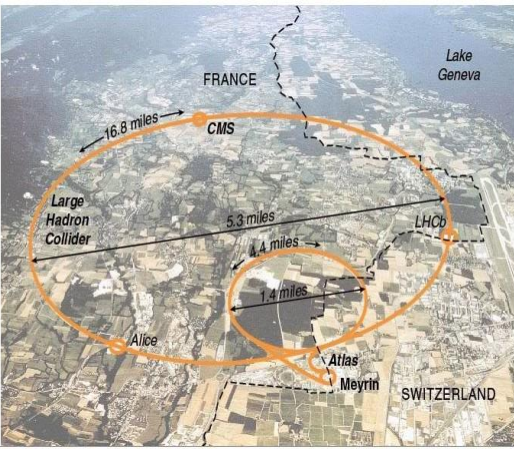
# Theoretical Limits to the Existence of Nuclei

- Only a fraction of the theoretically possible isotopes have been produced and studied.
- A new generation of accelerators being constructed will accelerate radioactive ions and probe the region of unknown isotopes



Layout of the accelerator, experimental systems and the experimental areas of the Facility for Rare Isotope Beams.

# ACCELERATORS

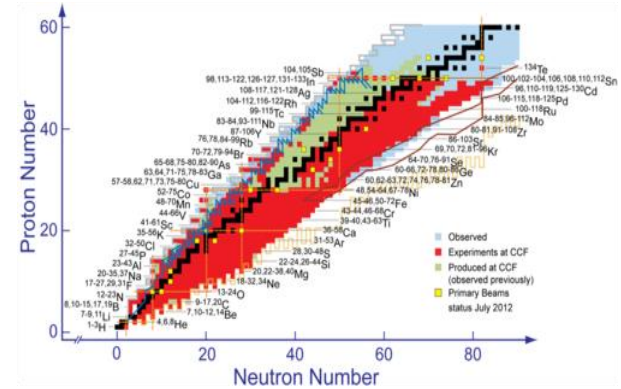
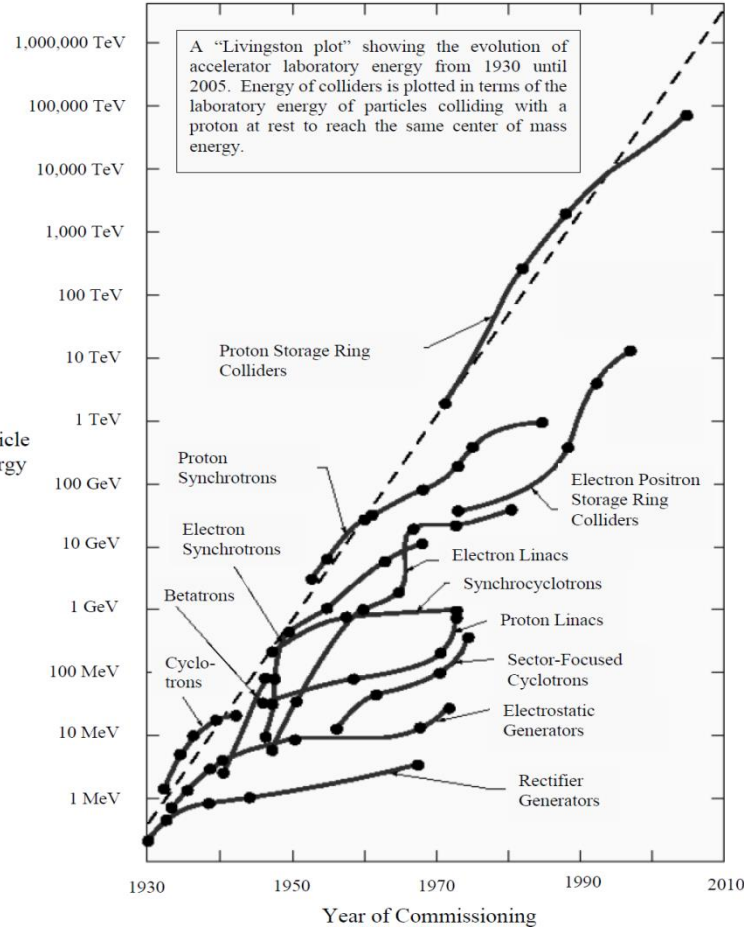


LHC



RHIC

Particle Energy

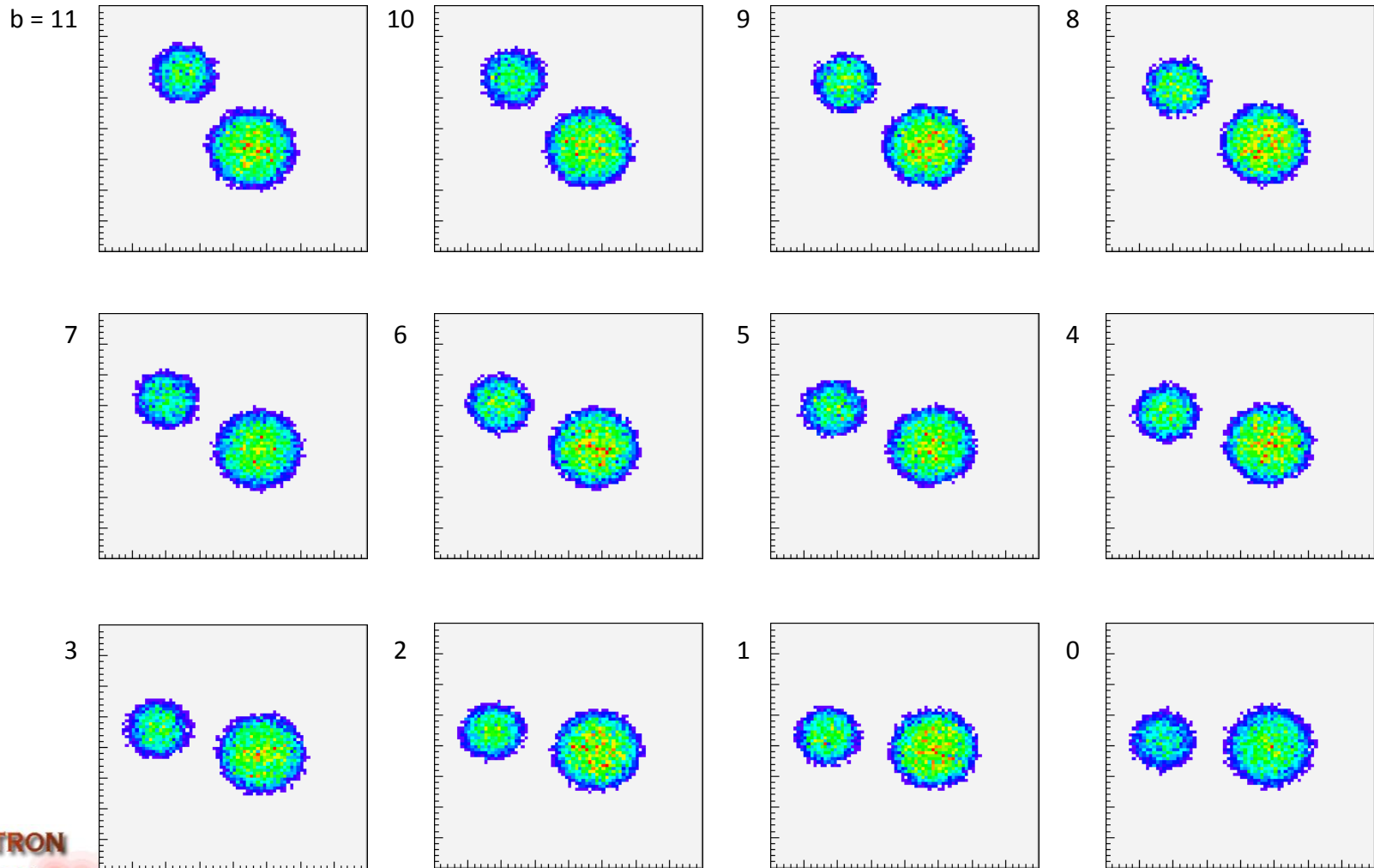


TAMU

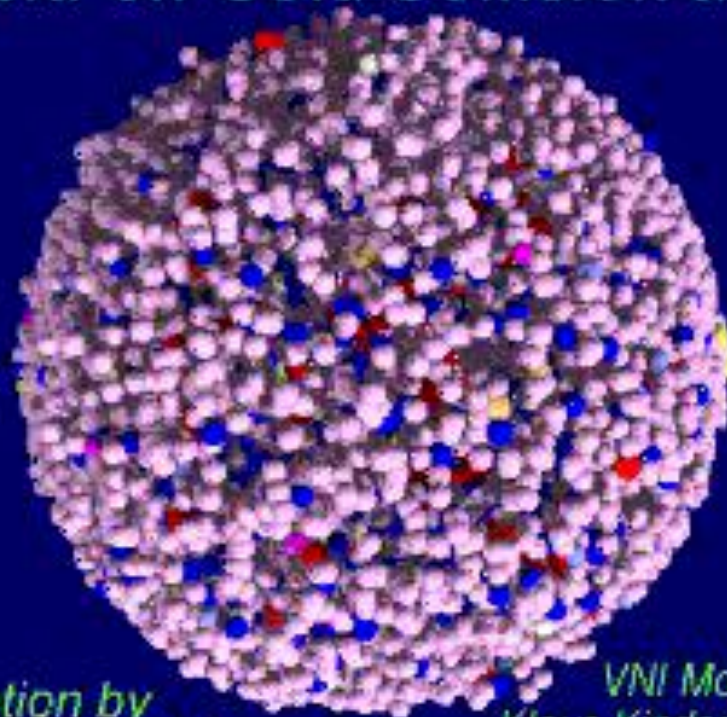
# Higher Energy Reactions

Time (fm/c) = 1

32 MeV/nucleon  $^{48}\text{Ca} + ^{124}\text{Sn}$



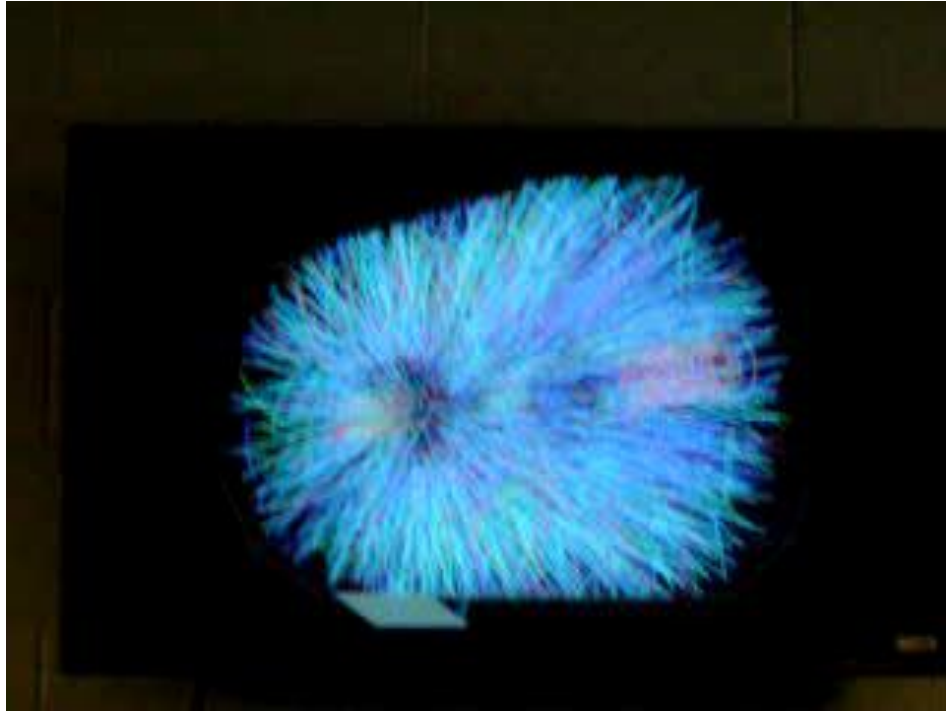
# A Gold-on-Gold Collision at RHIC



*Animation by  
Jeffery T. Mitchell*

*VNI Model by  
Klaus Kinder-Geiger and  
Ron Longacre*

# The Little Bang

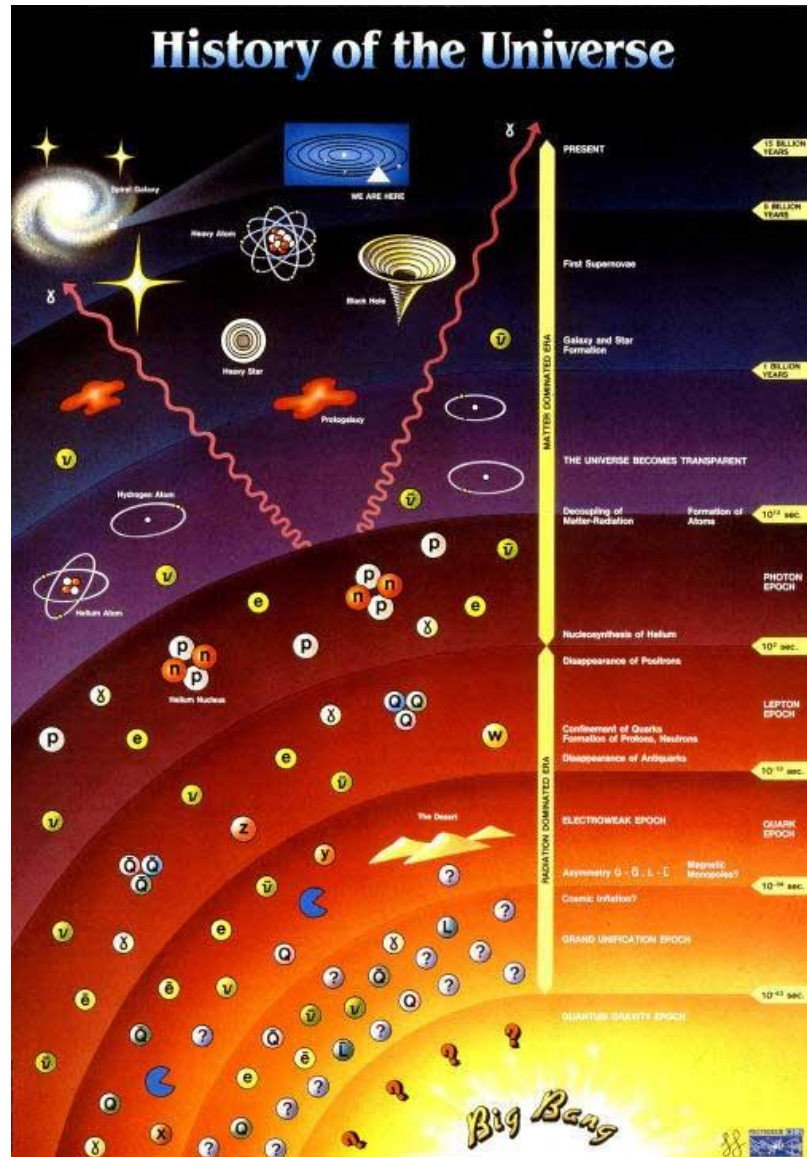


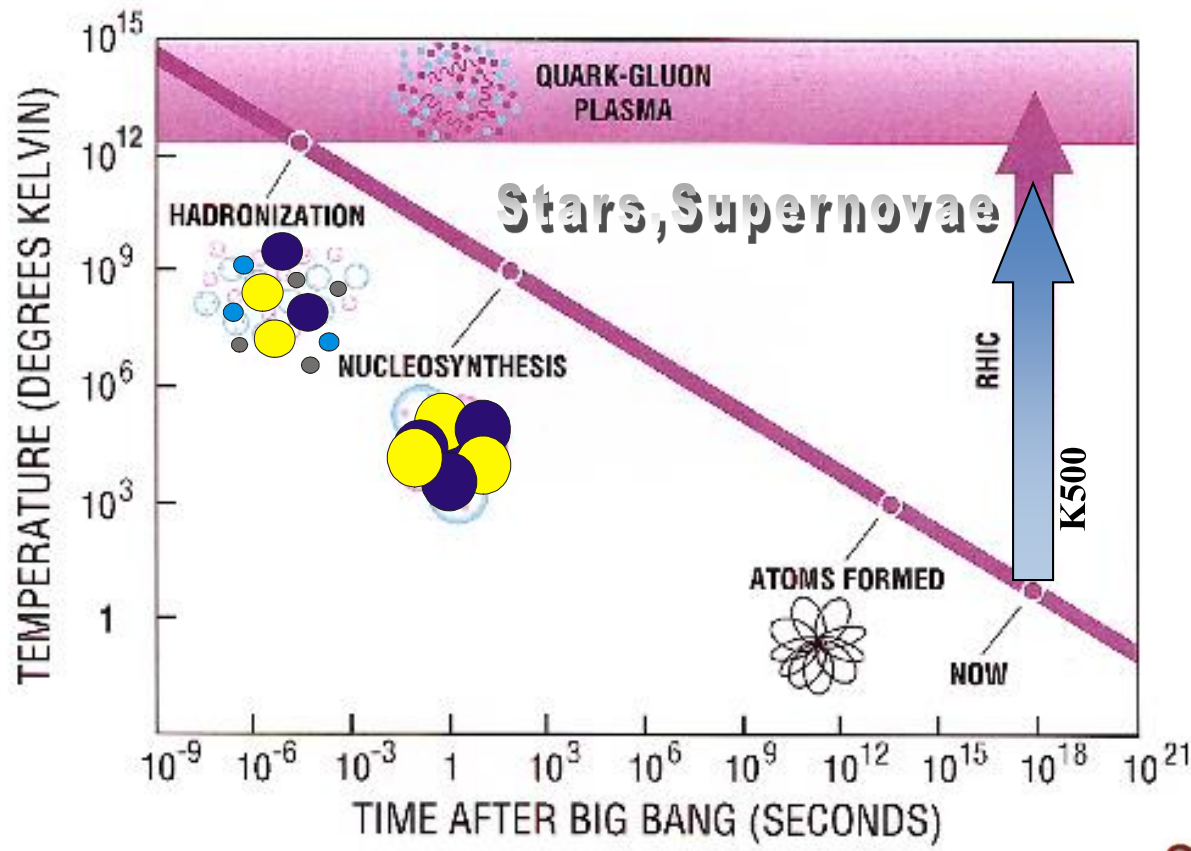


# The Big Bang



# The Big Bang



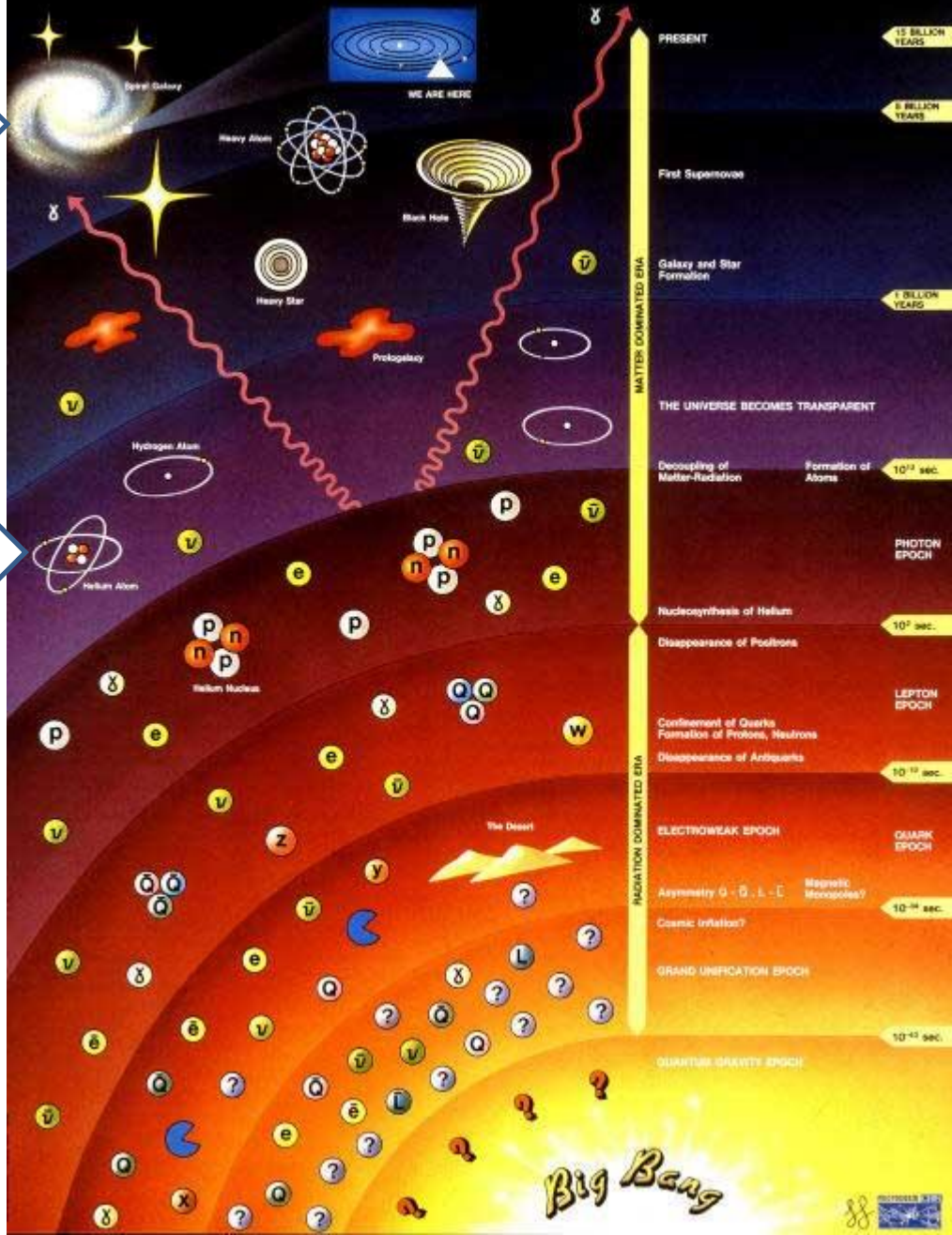
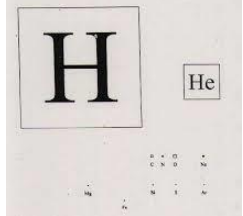


# History of the Universe

Heavier Elements

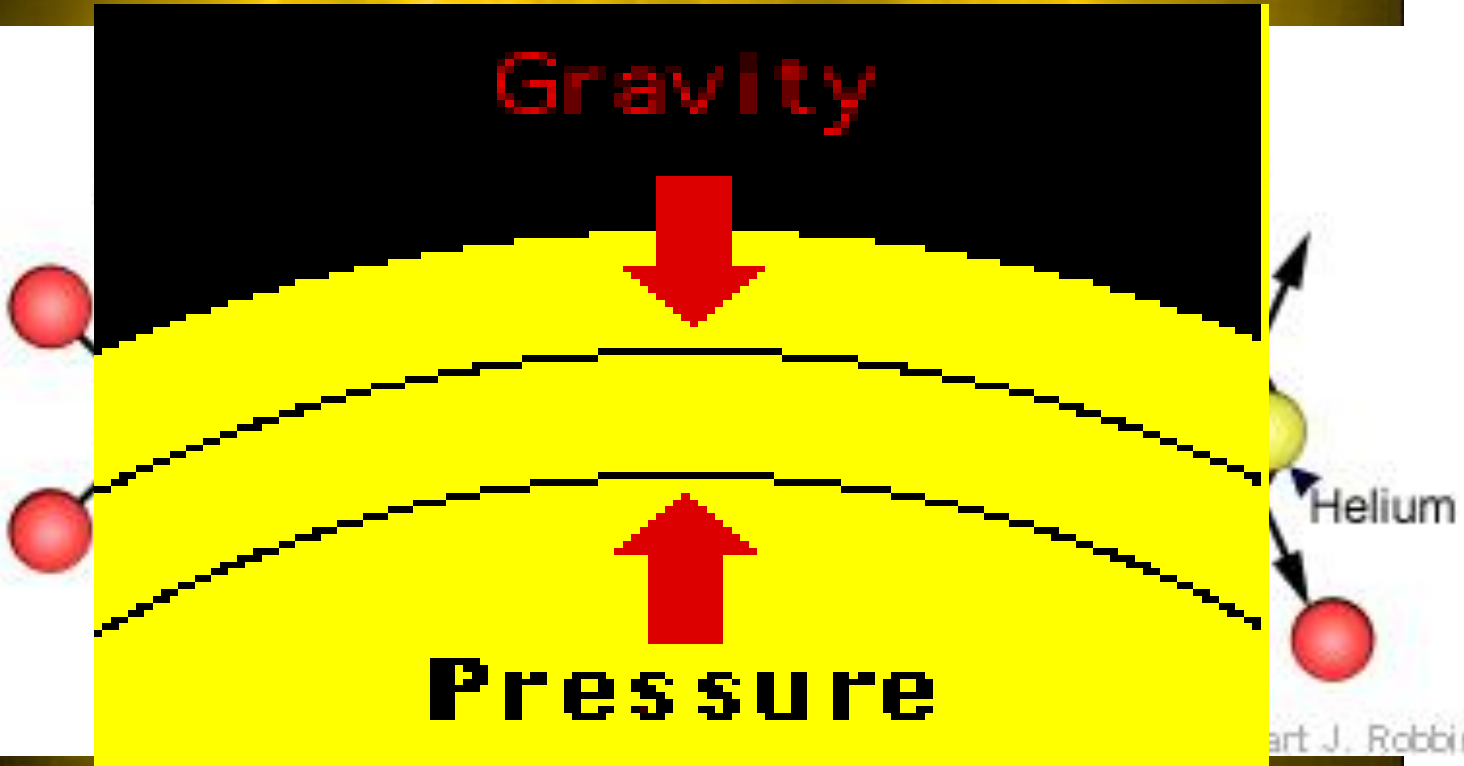
First Atoms, H and He

The Astronomer's Periodic Table  
(Ben McCall)

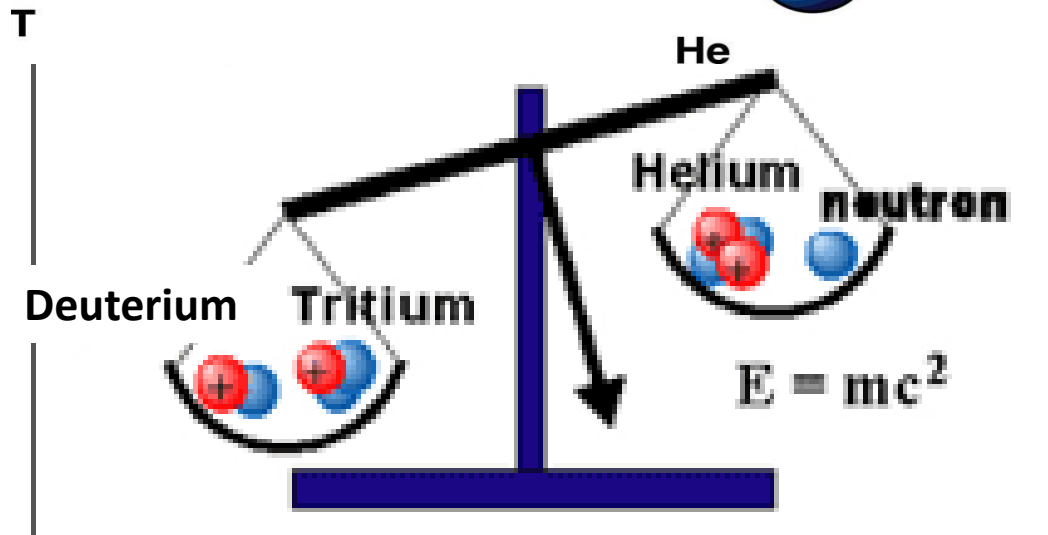
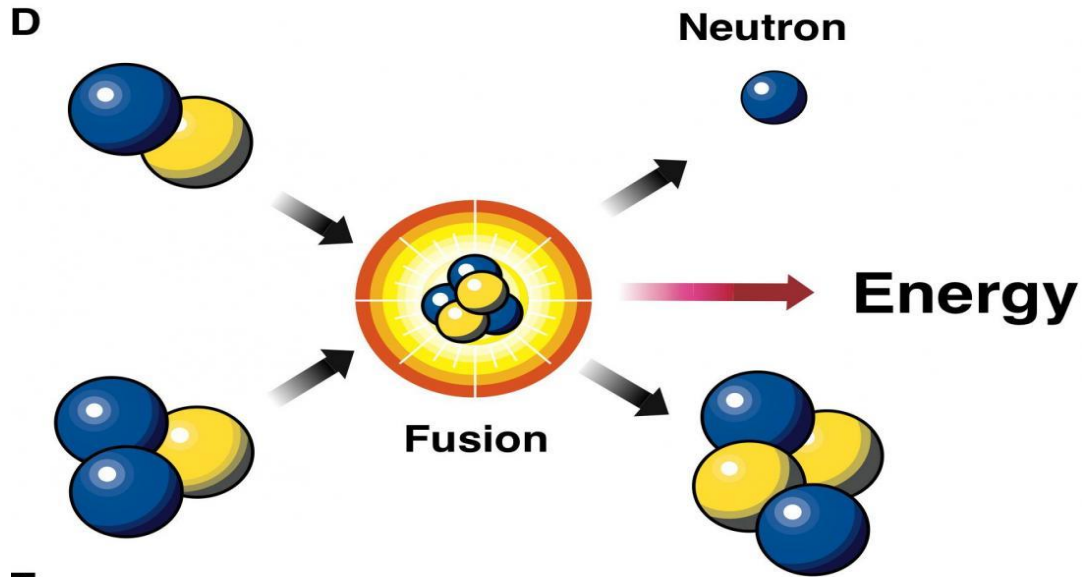


# OUR SUN

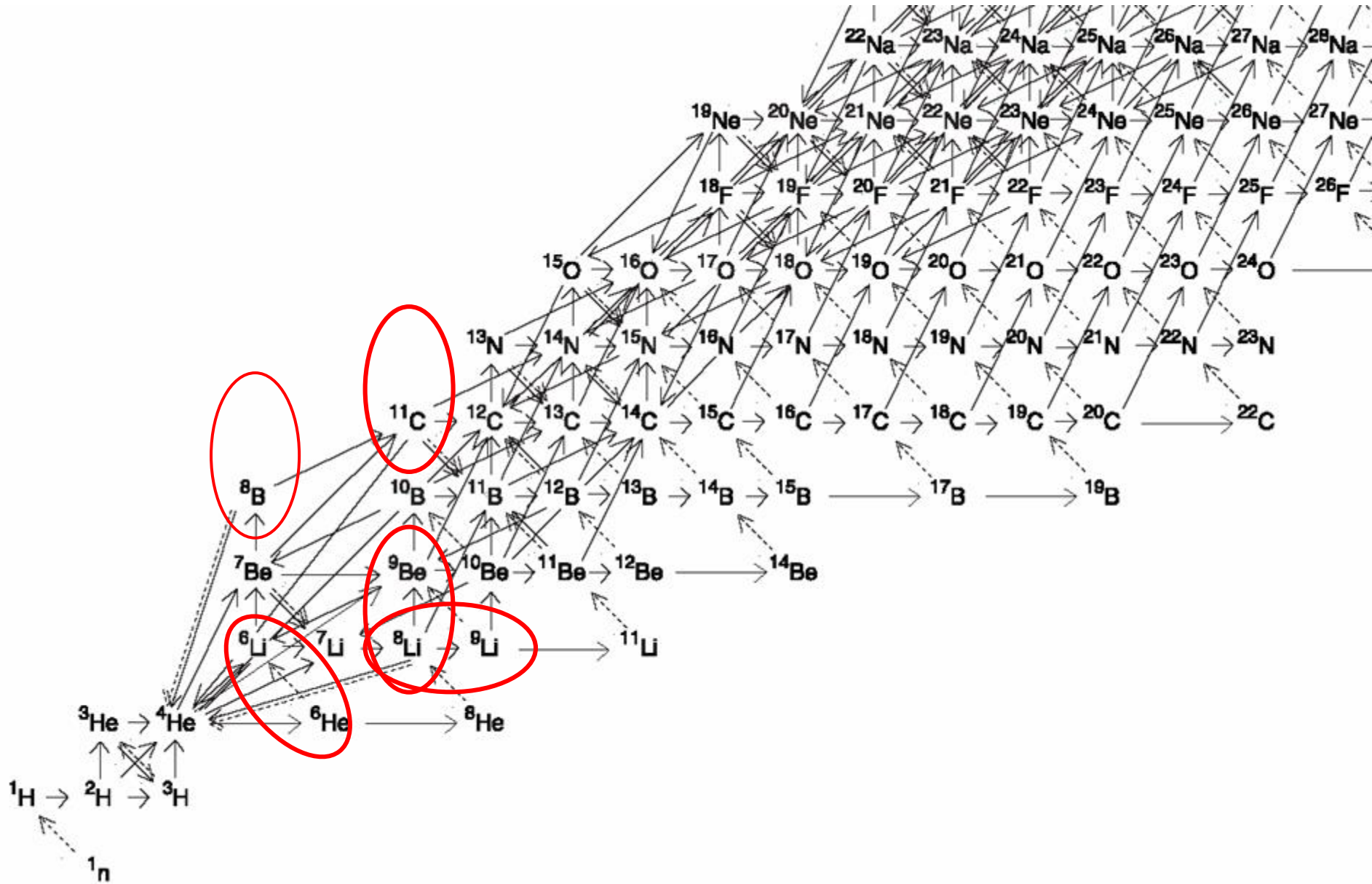
## A Ball of Hydrogen



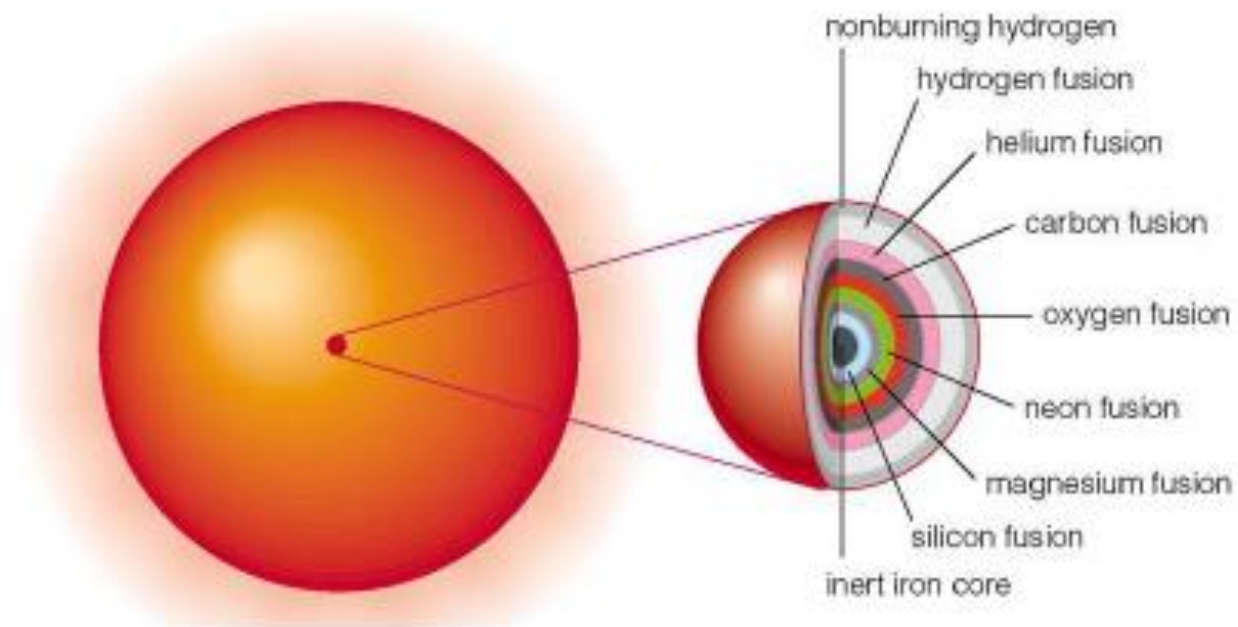
10,000,000 DEGREES KELVIN



# Origin of the Lighter Elements



*A massive star near the end of its lifetime has “onion ring” structure*

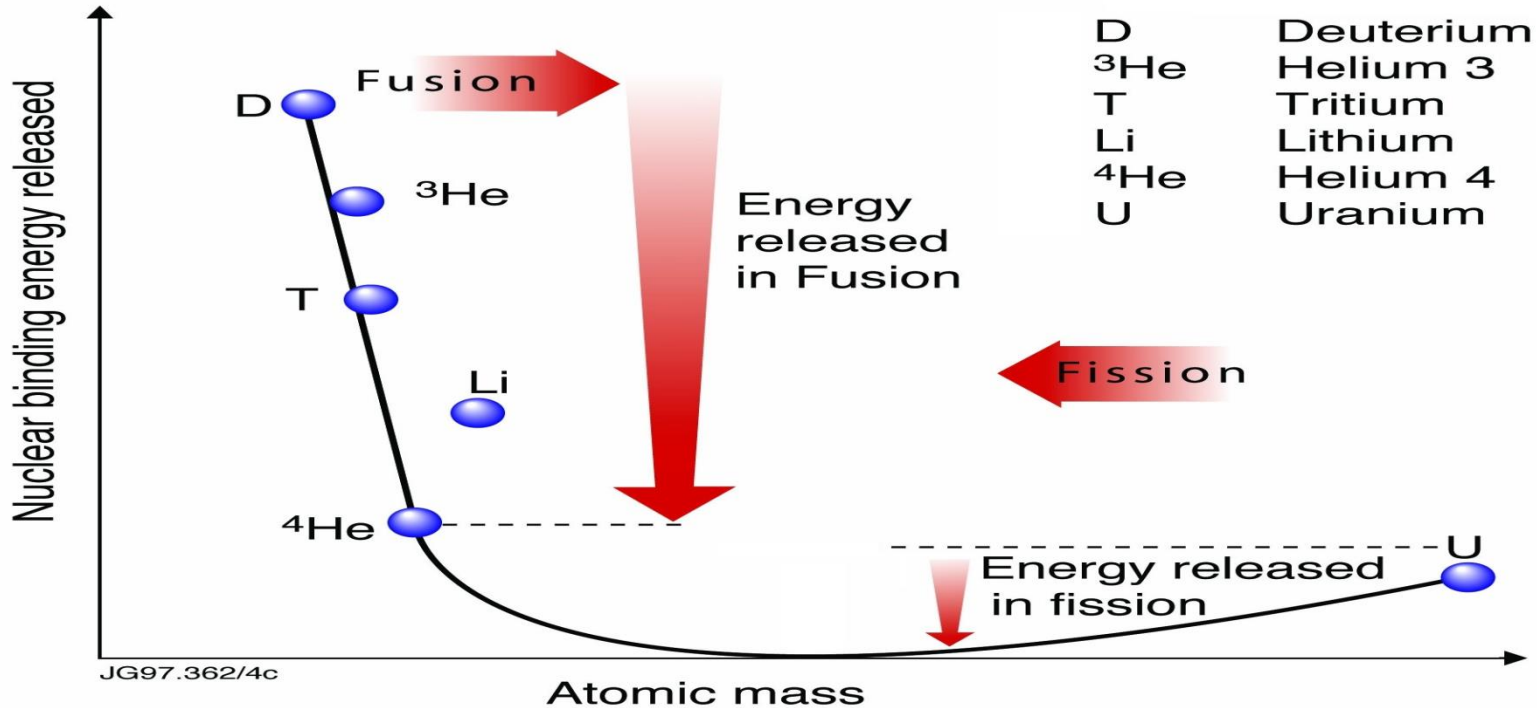




# WHY?

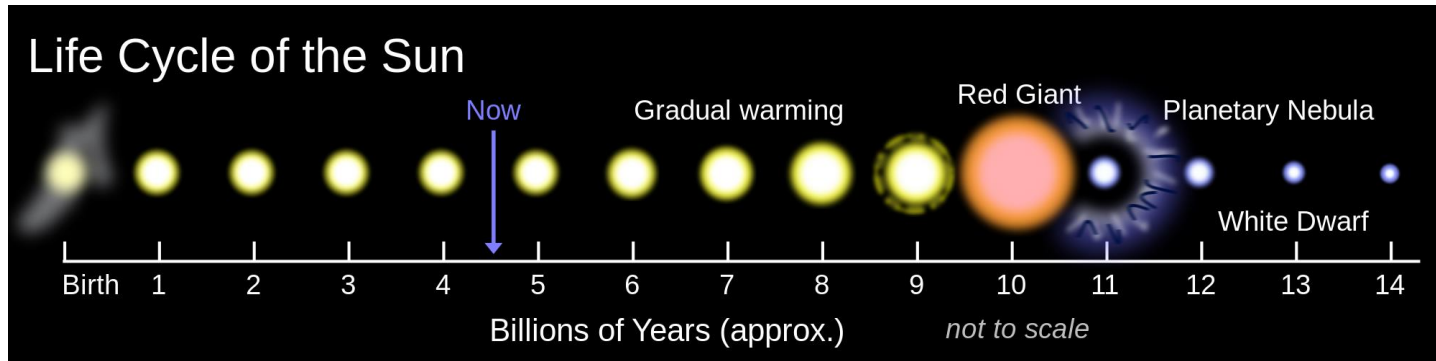
## Because Floor of Binding Energy Valley is Not Flat

For A Given Number of Nucleons, An Increase in Binding Energy per Nucleon Means that Energy Will Be Released

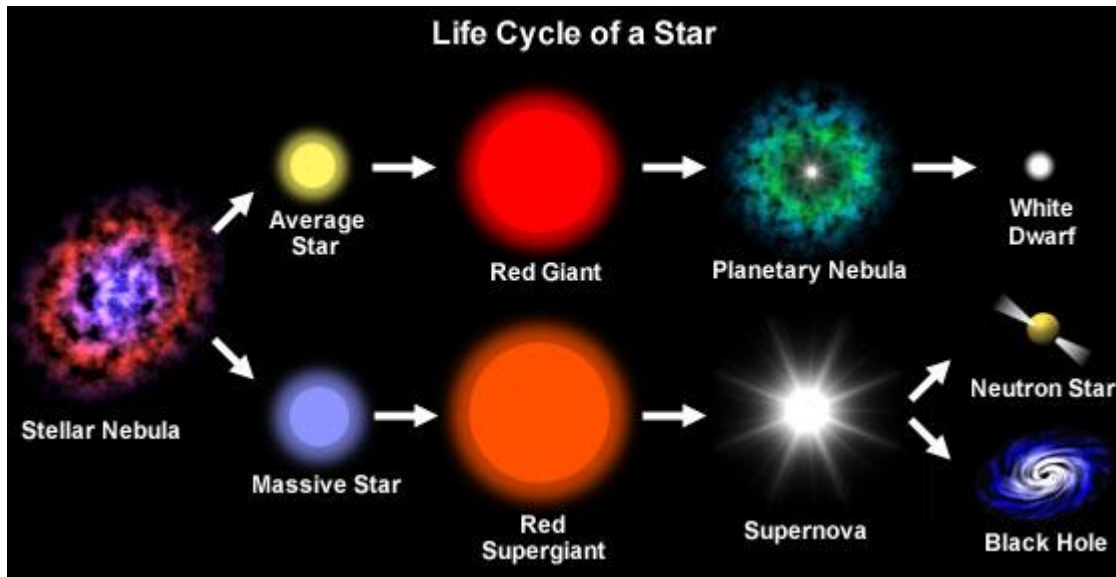


For Small Numbers of Nucleons, i.e., Nuclei Much Lighter Than Iron, Energy is Released If Nuclei Fuse (FUSION)

For Large Numbers of Nucleons i.e., Nuclei Much Heavier Than Iron, Energy is Released If the Nuclei Split (FISSION)



# HOW ARE THE HEAVIER ELEMENTS PRODUCED ?



# *One Important Source for Generation of THE ELEMENTS BEYOND IRON Is EXPLOSIONS of SUCH STARS*

## Nucleosynthesis in the r-process

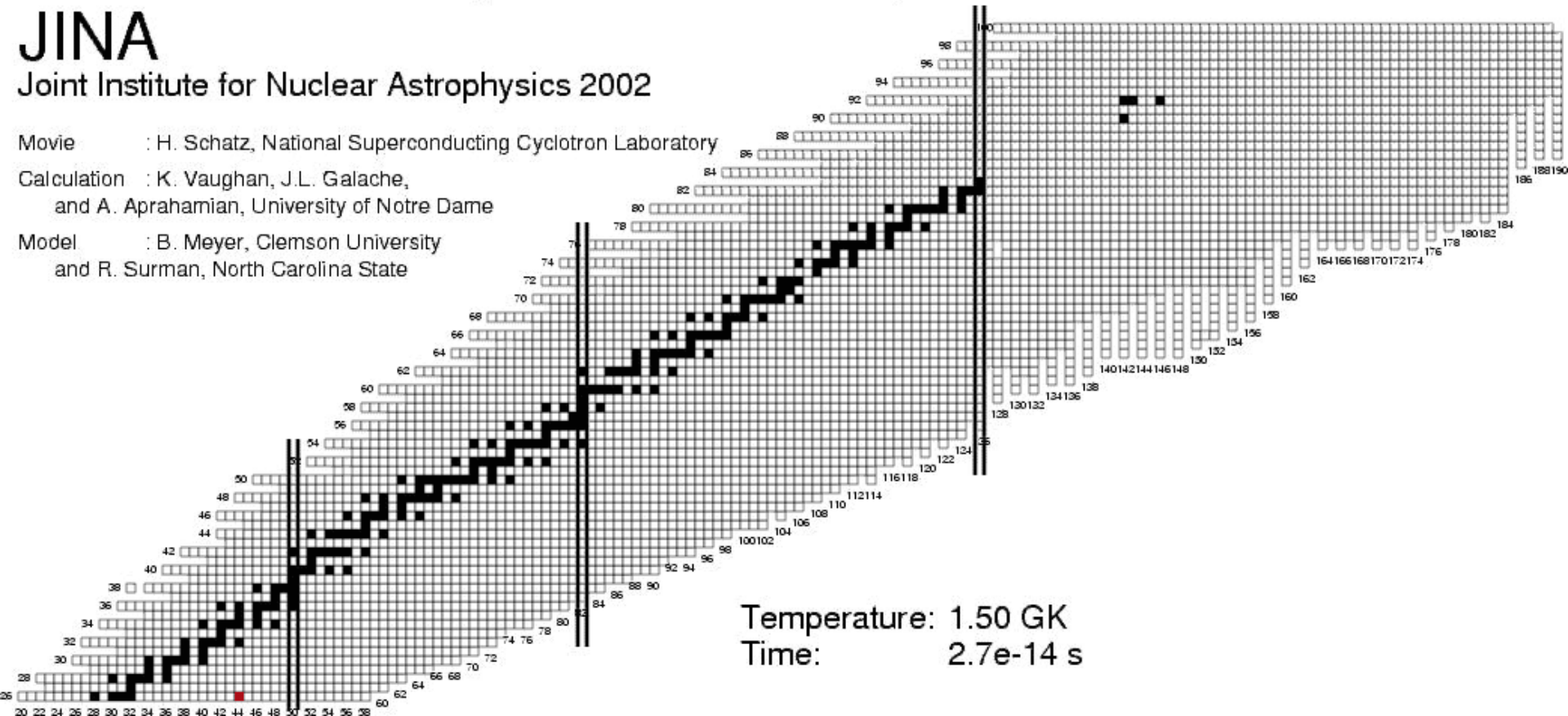
### JINA

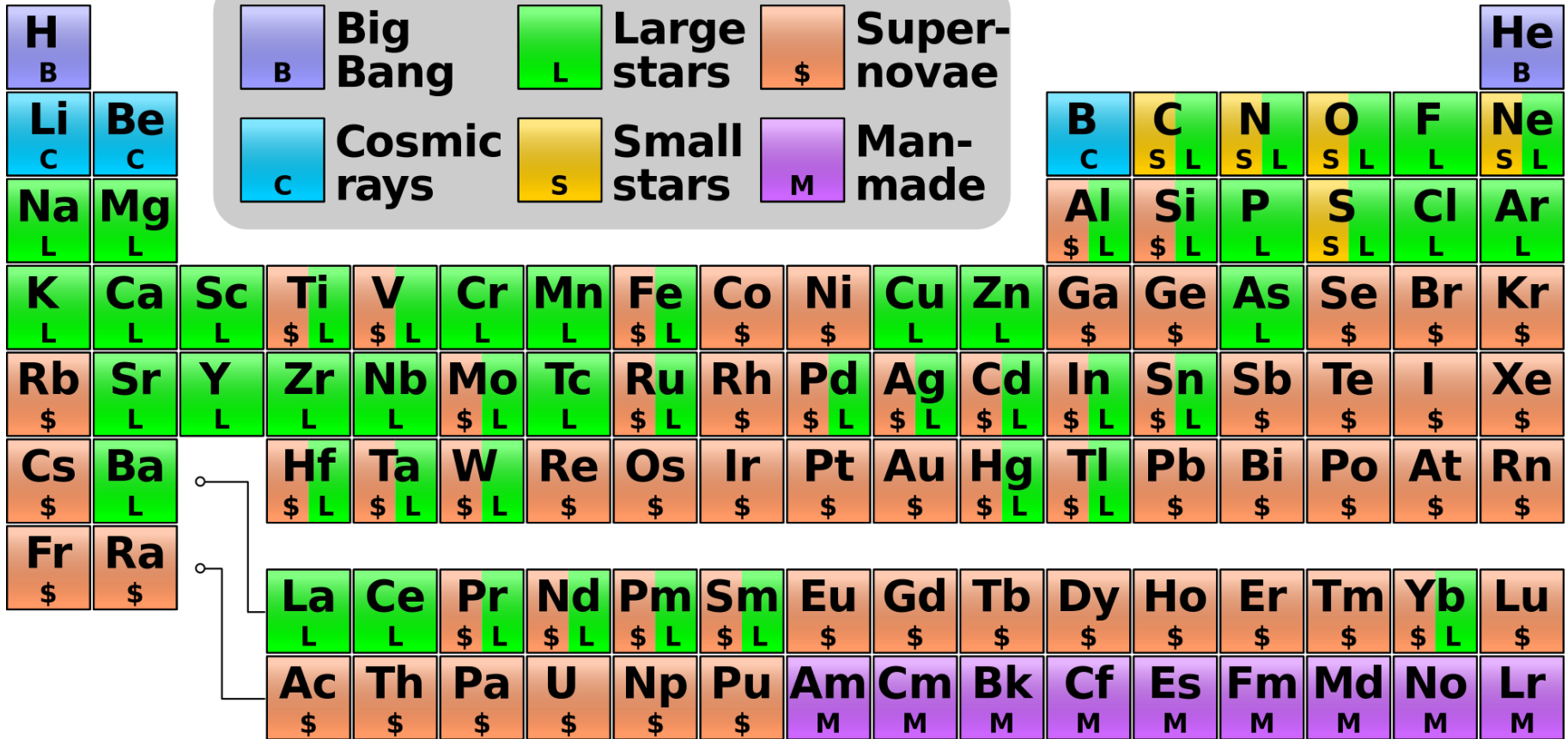
Joint Institute for Nuclear Astrophysics 2002

Movie : H. Schatz, National Superconducting Cyclotron Laboratory

Calculation : K. Vaughan, J.L. Galache,  
and A. Aprahamian, University of Notre Dame

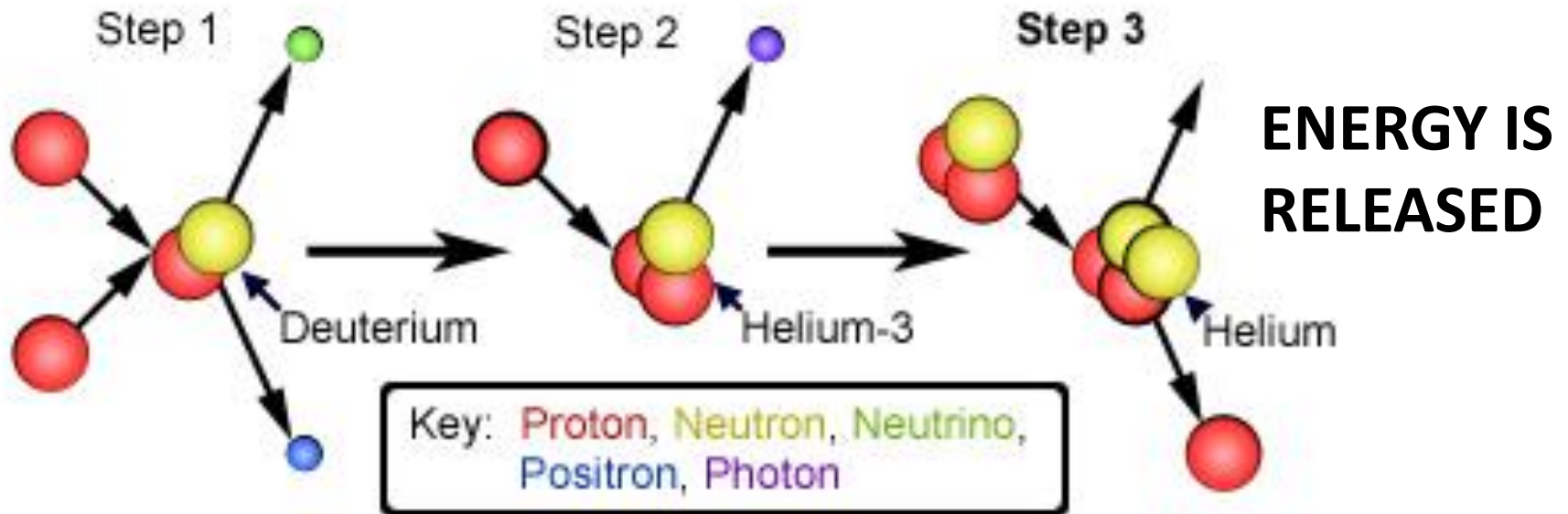
Model : B. Meyer, Clemson University  
and R. Surman, North Carolina State





# OUR SUN

## Nuclear Fusion in Stars



© 1997, 2001-2003 Stuart J. Robbins

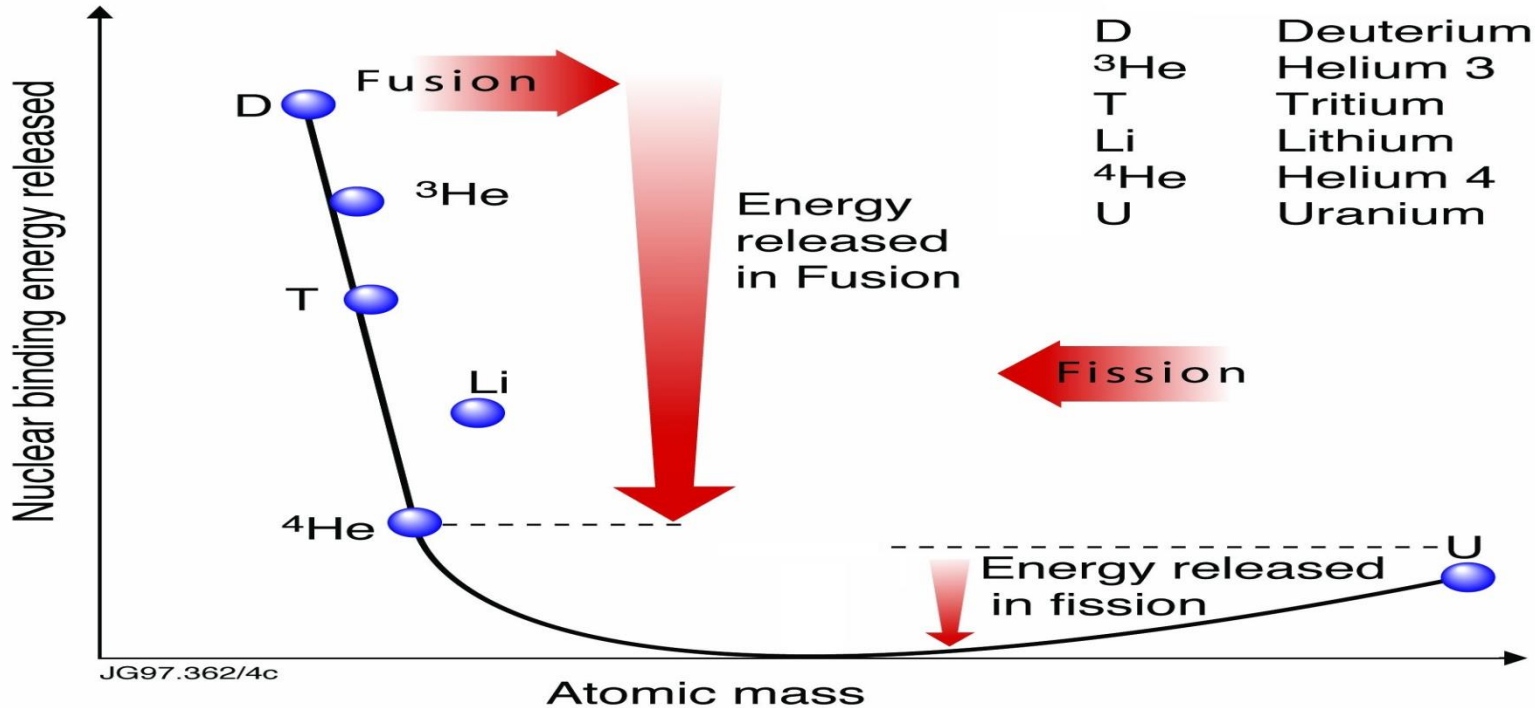
# 10,000,000 DEGREES KELVIN

2001/03/04 01:05

# WHY?

## Because Floor of Binding Energy Valley is Not Flat

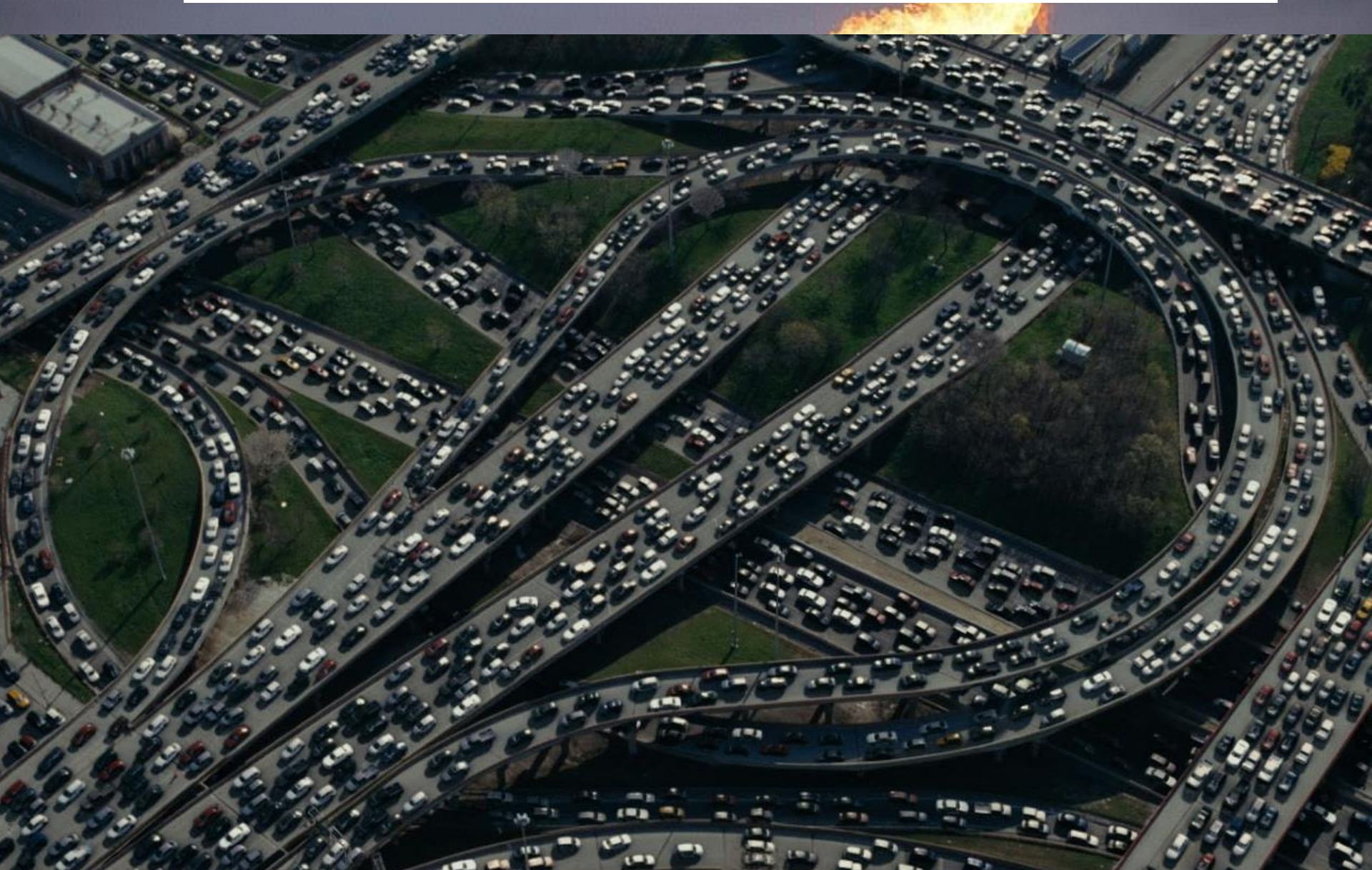
For A Given Number of Nucleons, An Increase in Binding Energy per Nucleon Means that Energy Will Be Released



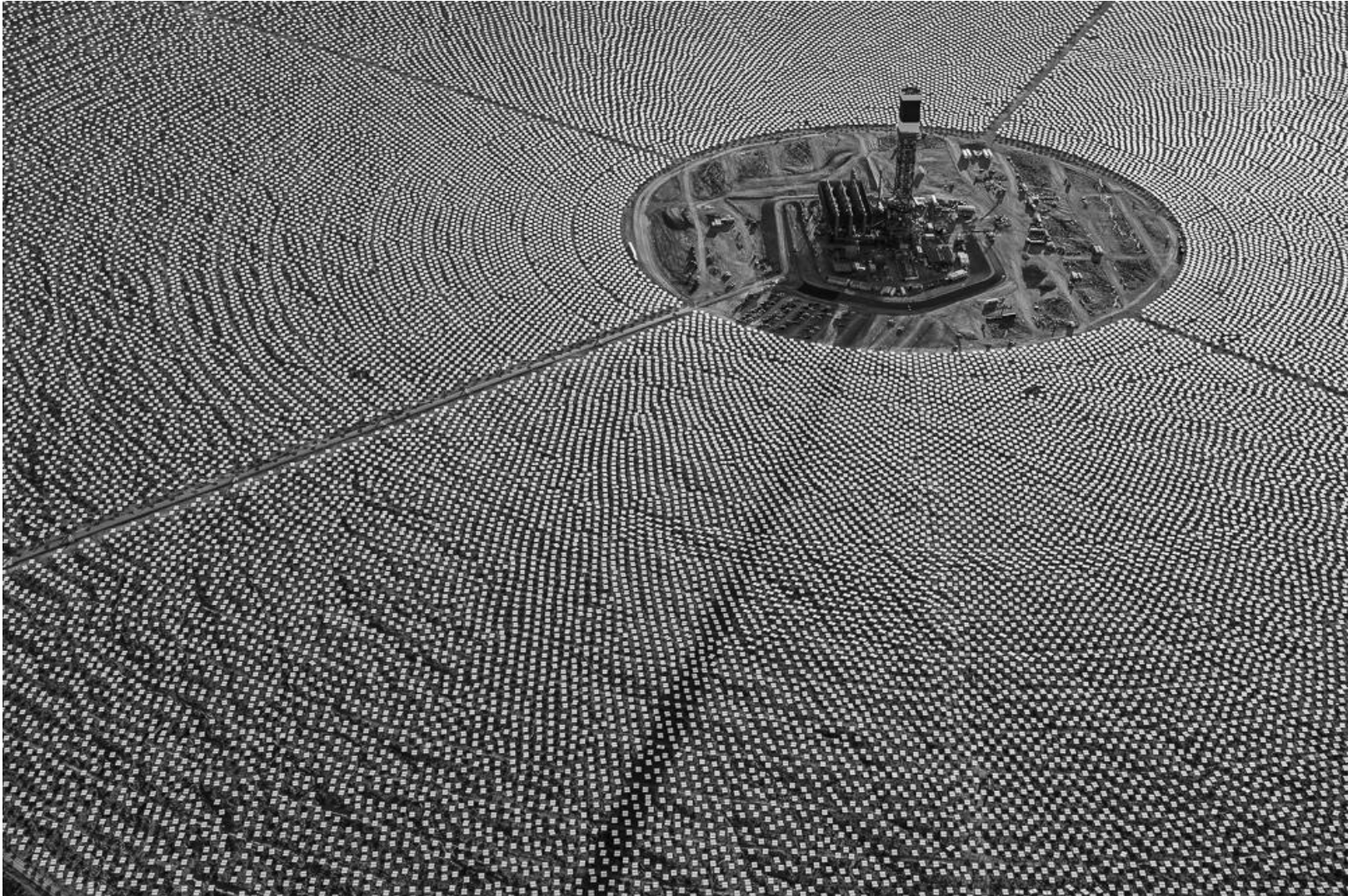
For Small Numbers of Nucleons, i.e., Nuclei Much Lighter Than Iron, Energy is Released If Nuclei Fuse (FUSION)

For Large Numbers of Nucleons i.e., Nuclei Much Heavier Than Iron, Energy is Released If the Nuclei Split (FISSION)

# Using Fossil Fuels is Indirectly Harvesting Solar Energy For Energy Production



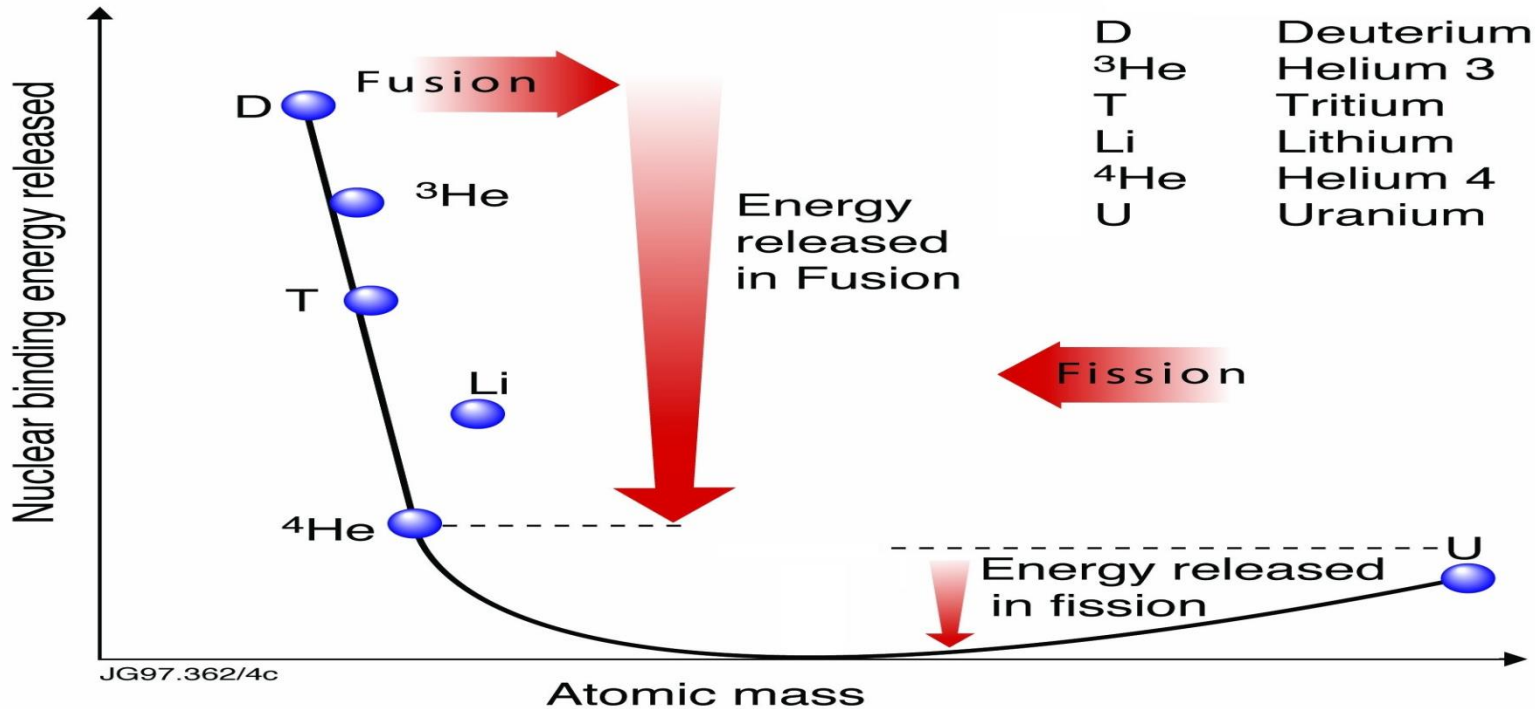
# Directly Harvesting Solar Energy For Energy Production





# Harnessing Nuclear Reactions For Energy Production

For A Given Number of Nucleons,  
An Increase in Binding Energy per  
Nucleon Means that Energy Will Be  
Released



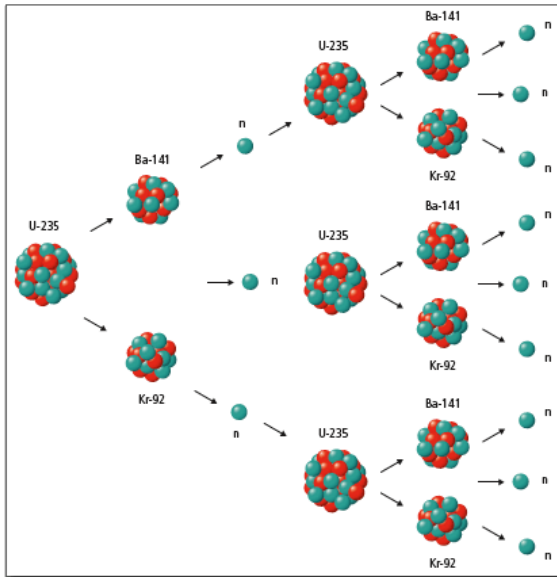
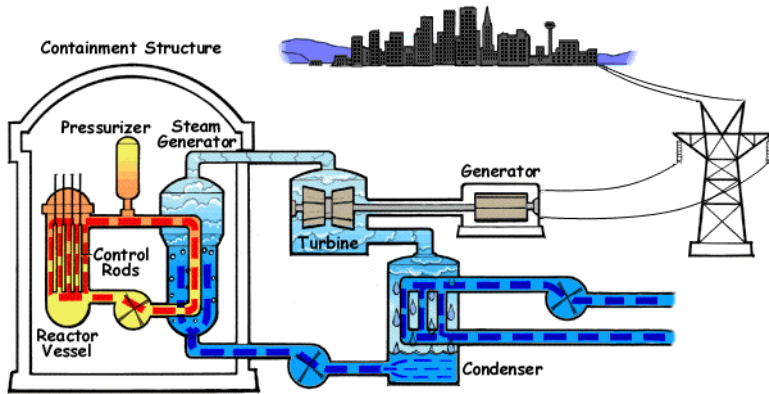
For Small Numbers of Nucleons, i.e.,  
Nuclei Much Lighter Than Iron,  
Energy is Released If Nuclei Fuse (FUSION)

For Large Numbers of Nucleons  
i.e., Nuclei Much Heavier Than Iron,  
Energy is Released If the Nuclei Split  
(FISSION)

# FISSION REACTOR

## Harnessing the Heavy Elements

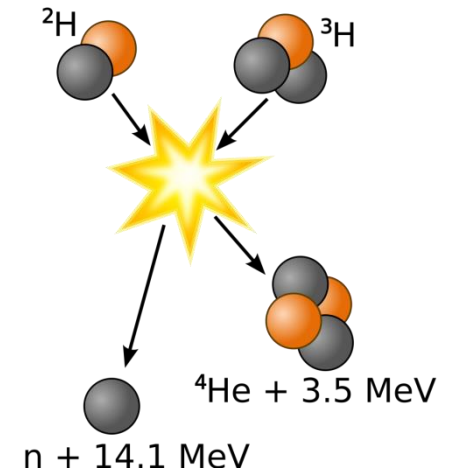
NOW



# FUSION REACTOR

## Harnessing the Light Elements

Still in the future



# Nuclear Reactions

## Where Would We Be Without Them?



“There are more things in heaven and earth, Horatio,  
Than are dreamt of in your philosophy.”

**Shakespeare**

**- *Hamlet* (1.5.167-8), Hamlet to Horatio**