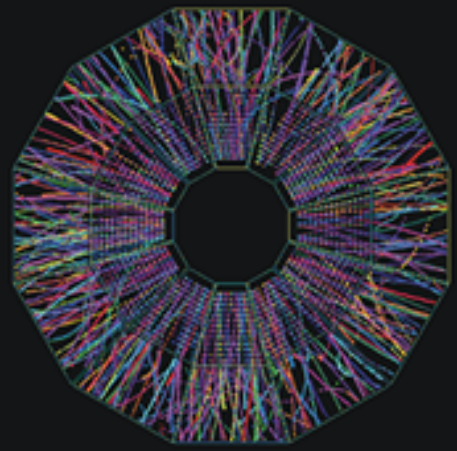


SATURDAY MORNING

# PHYSICS

AT TEXAS A&M



## Symmetries in Nature

A glimpse into the beauty and art of science

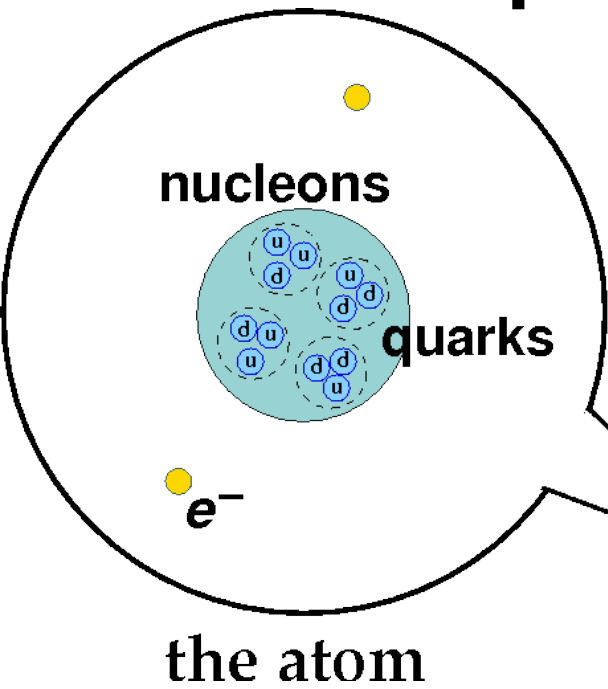
Dan Melconian

Texas A&M University

Cyclotron Institute

Feb 28, 2009

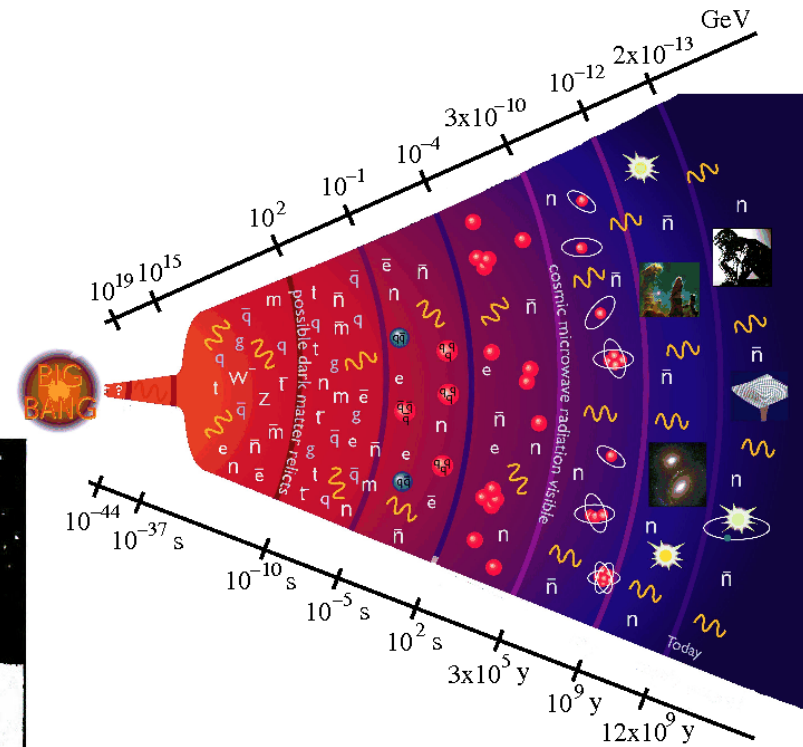
# Scope of modern physics



From the very **smallest** scales ...



... to the very **largest**



Physics lets us understand the world around us

# Art vs Science?



*There are more things in heaven and earth, Horatio,  
Than are dreamt of in your philosophy.*

Hamlet, Act I, Scene V

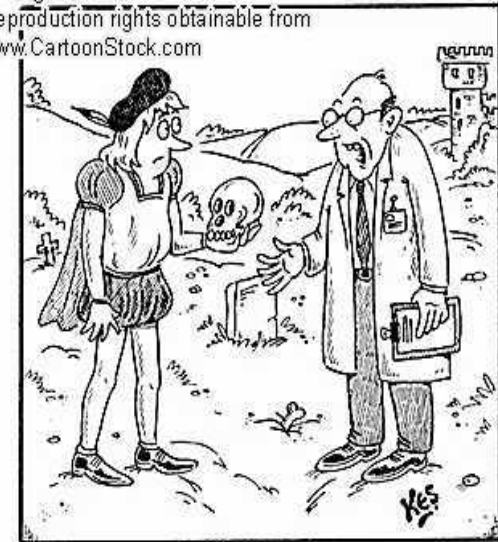
# Science vs Art?

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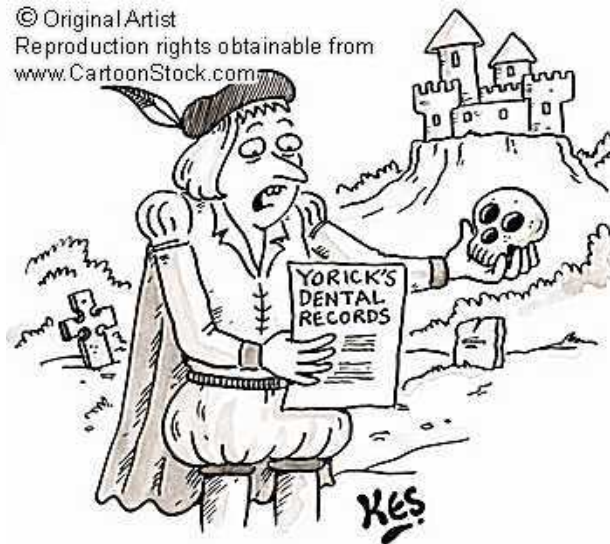


'Oh come on! How can you possibly know that it's Yorick without a proper forensic reconstruction?'

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"Yorick? No, I don't think so, unless of course he was a Neanderthal!"



"Alas irrefutable confirmation."

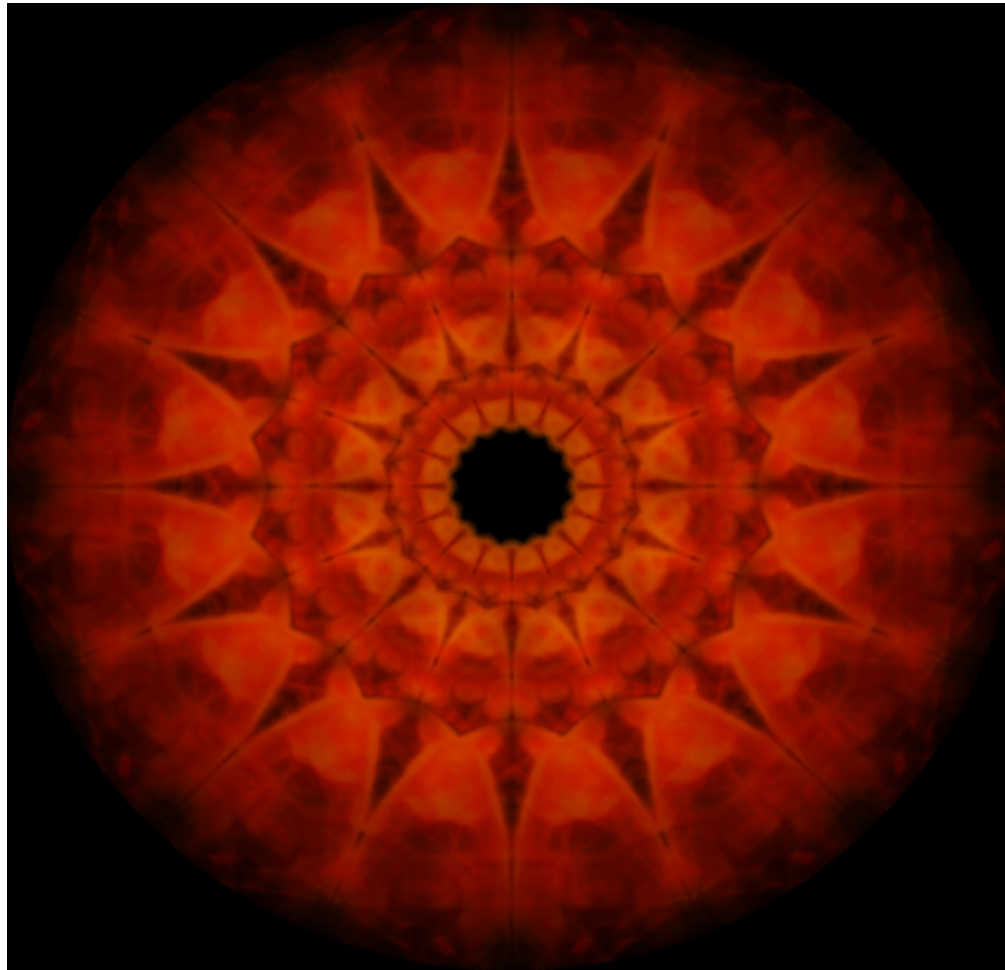
# Symmetry

## Oxford English Dictionary:

*Due or just proportion; harmony of parts with each other and the whole; fitting, regular, or balanced arrangement and relation of parts or elements; the condition or quality of being well-proportioned or well-balanced.*

*Regularity and beauty of form, fair or fine appearance, comeliness.*

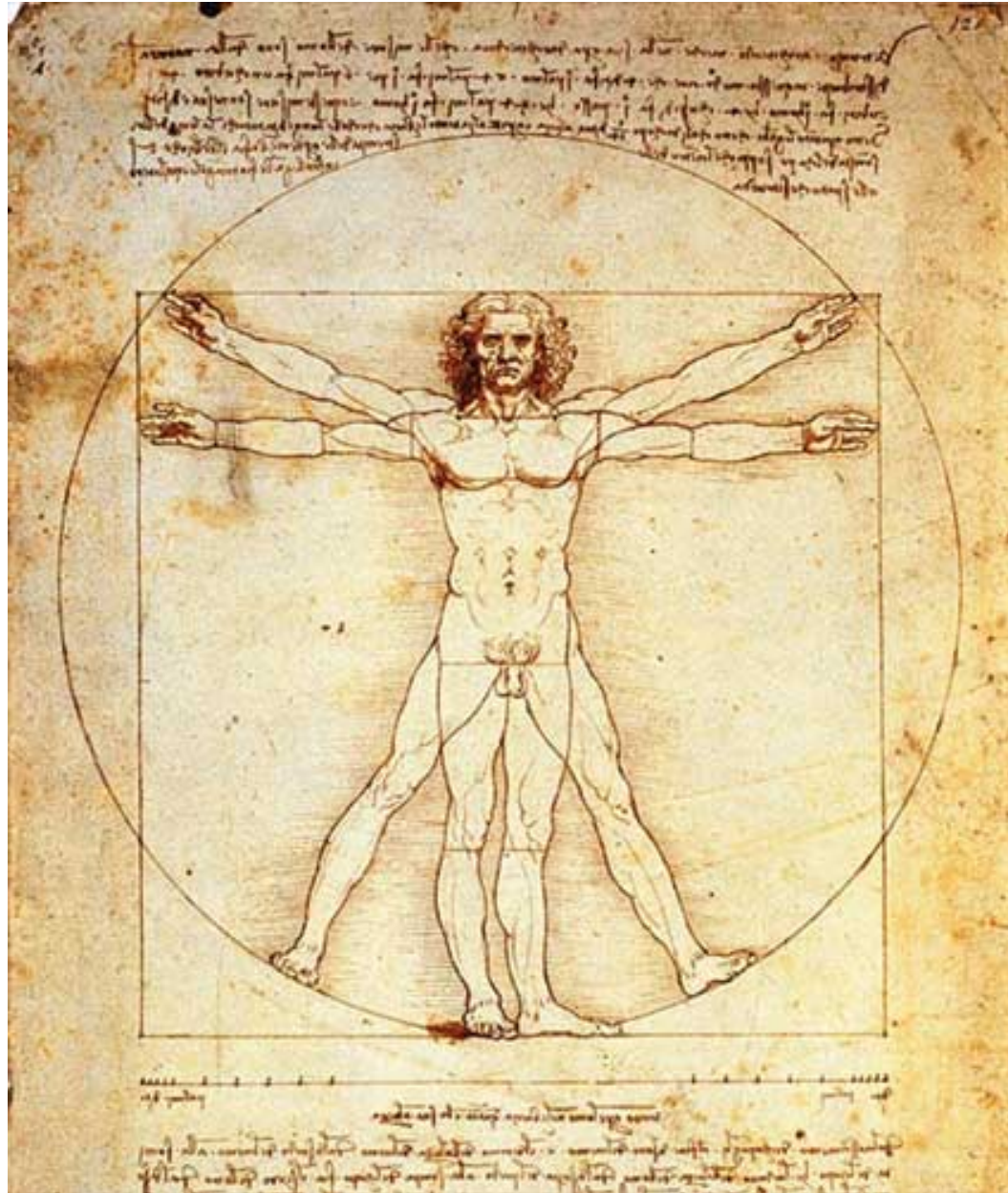
# Symmetries in Art



# Symmetries in Architecture



# Symmetries in Art & Science





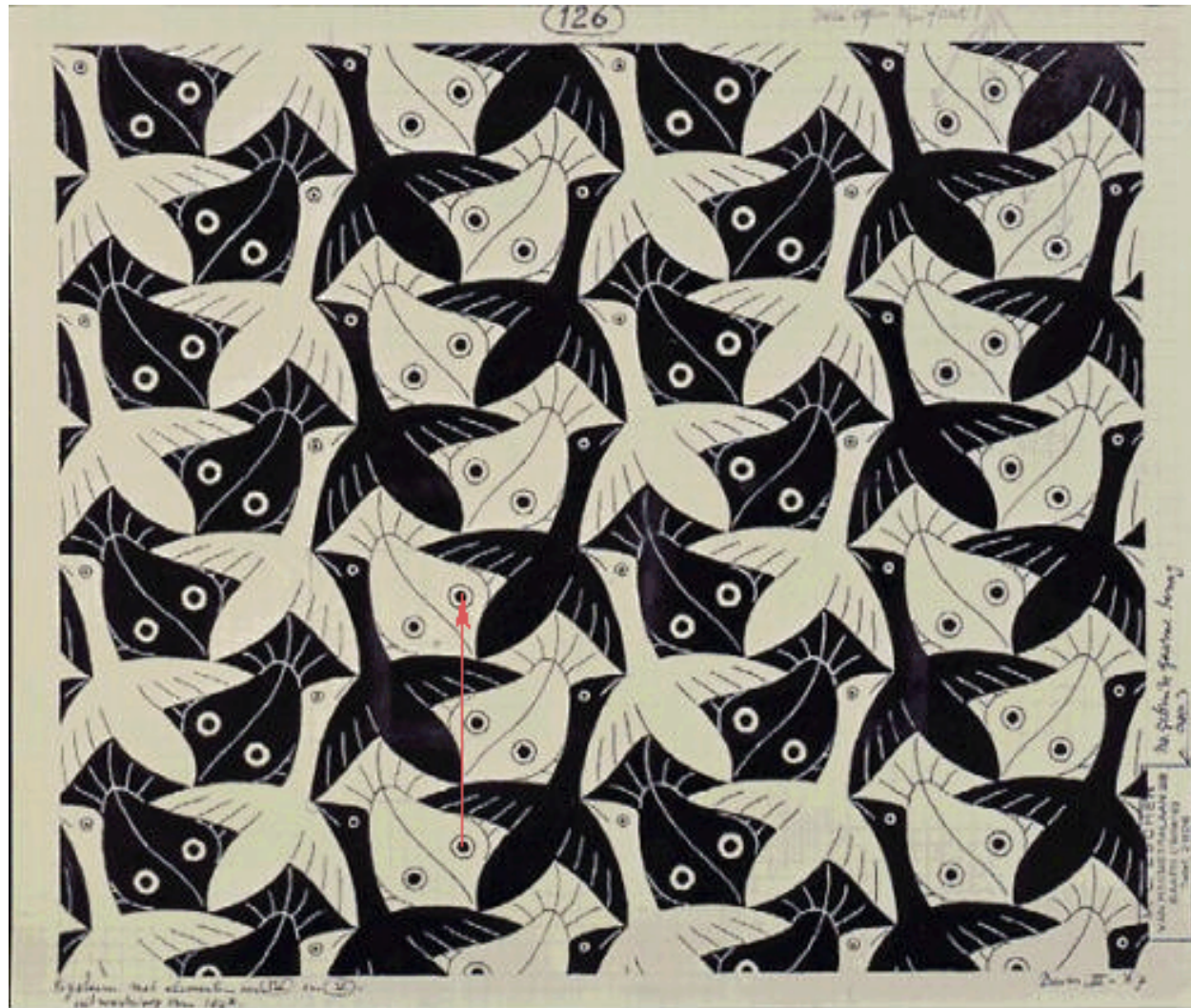
# Types of Symmetries

→ Translational → Art: M.C. Escher



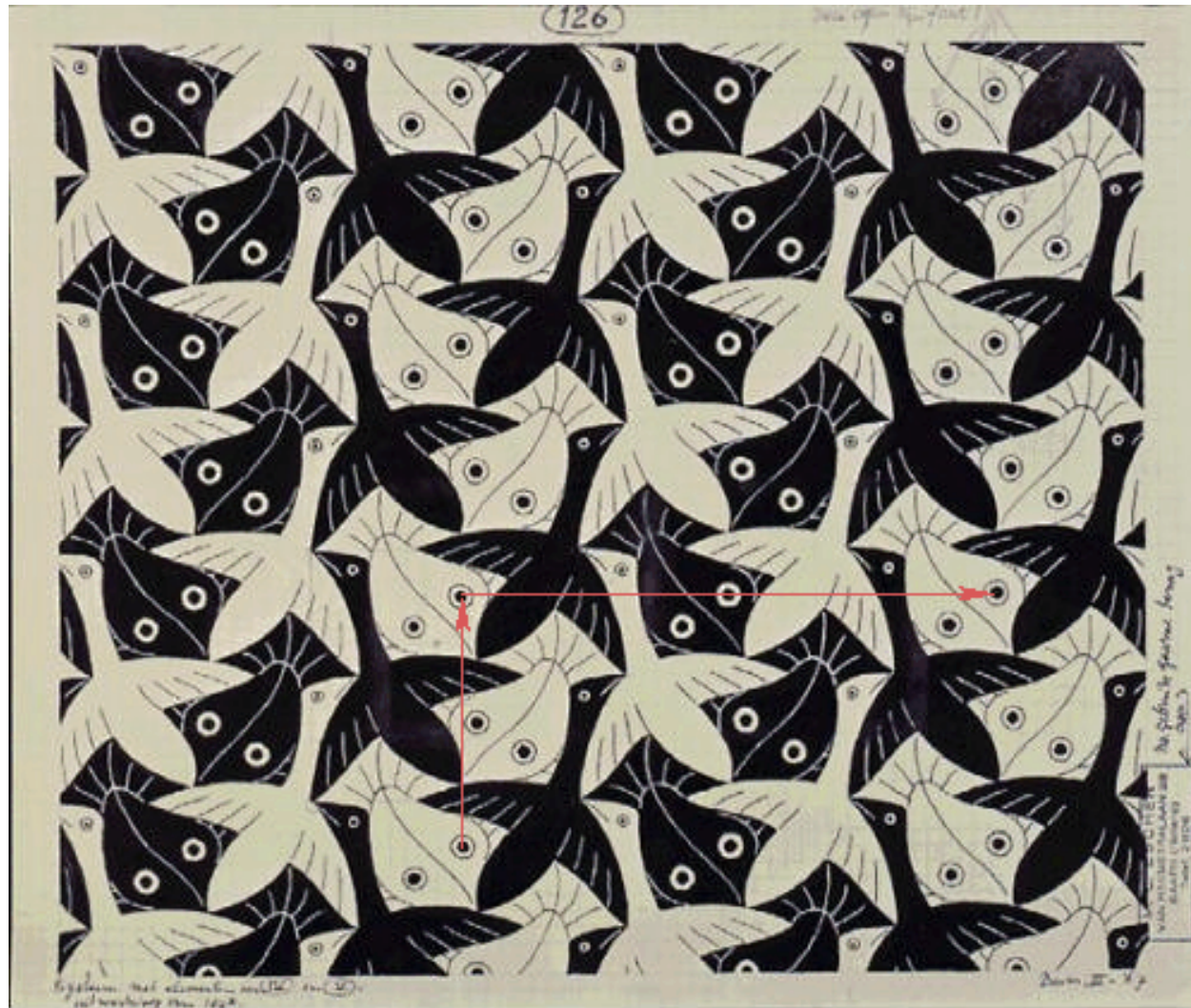
# Types of Symmetries

→ Translational → Art: M.C. Escher



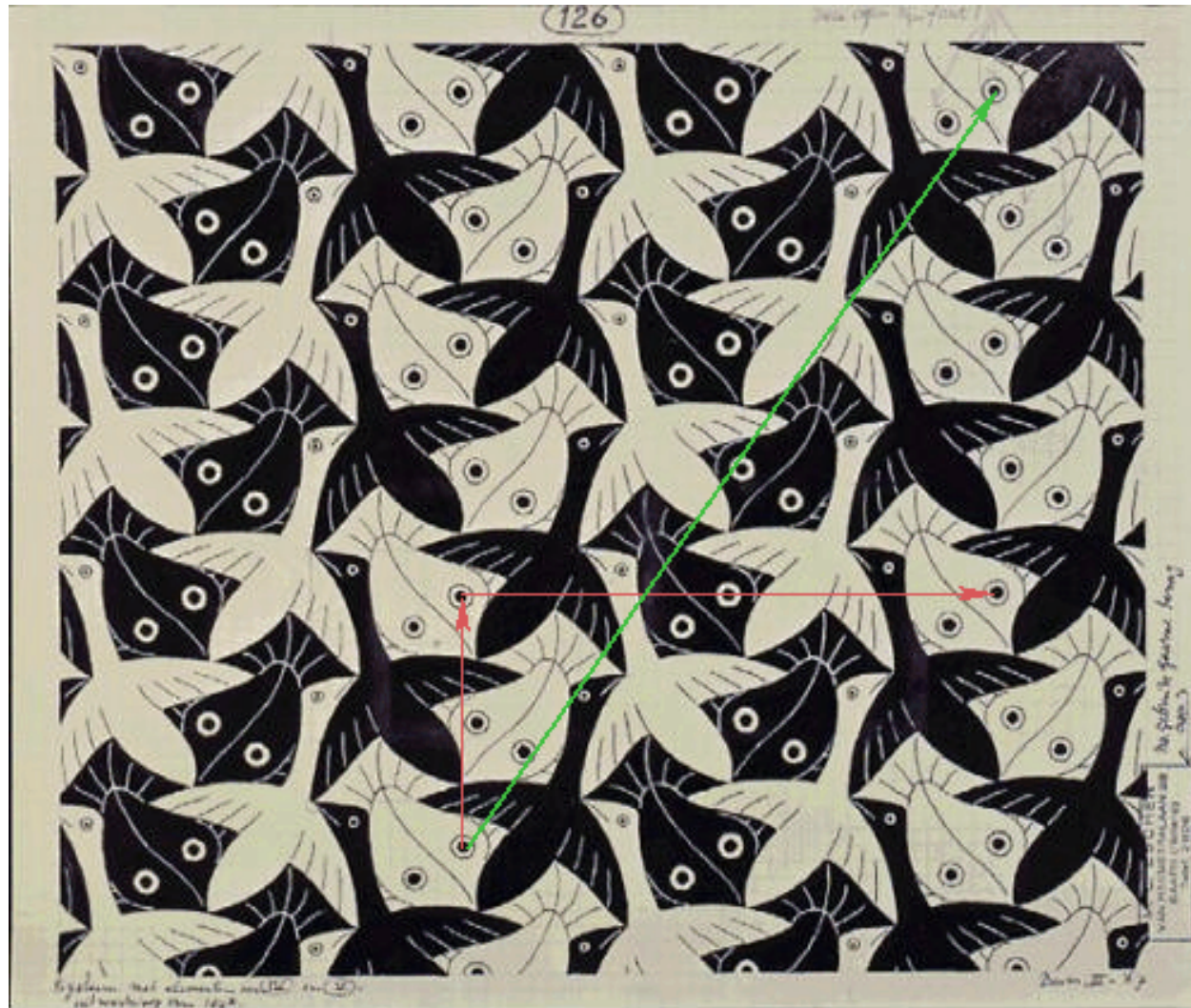
# Types of Symmetries

→ Translational → Art: M.C. Escher



# Types of Symmetries

→ Translational → Art: M.C. Escher



# Types of Symmetries

→ Reflections      ➤ the Taj Mahal



# Types of Symmetries

→ Reflections      † People



# Types of Symmetries

→ Reflections      > People



# Types of Symmetries

→ Reflections      ➤ People





# Types of Symmetries

→ Reflections      > People



# Types of Symmetries

→ Reflections      > People



# Types of Symmetries

→ Reflections      † People



# Types of Symmetries

→ Reflections      > People



# Types of Symmetries

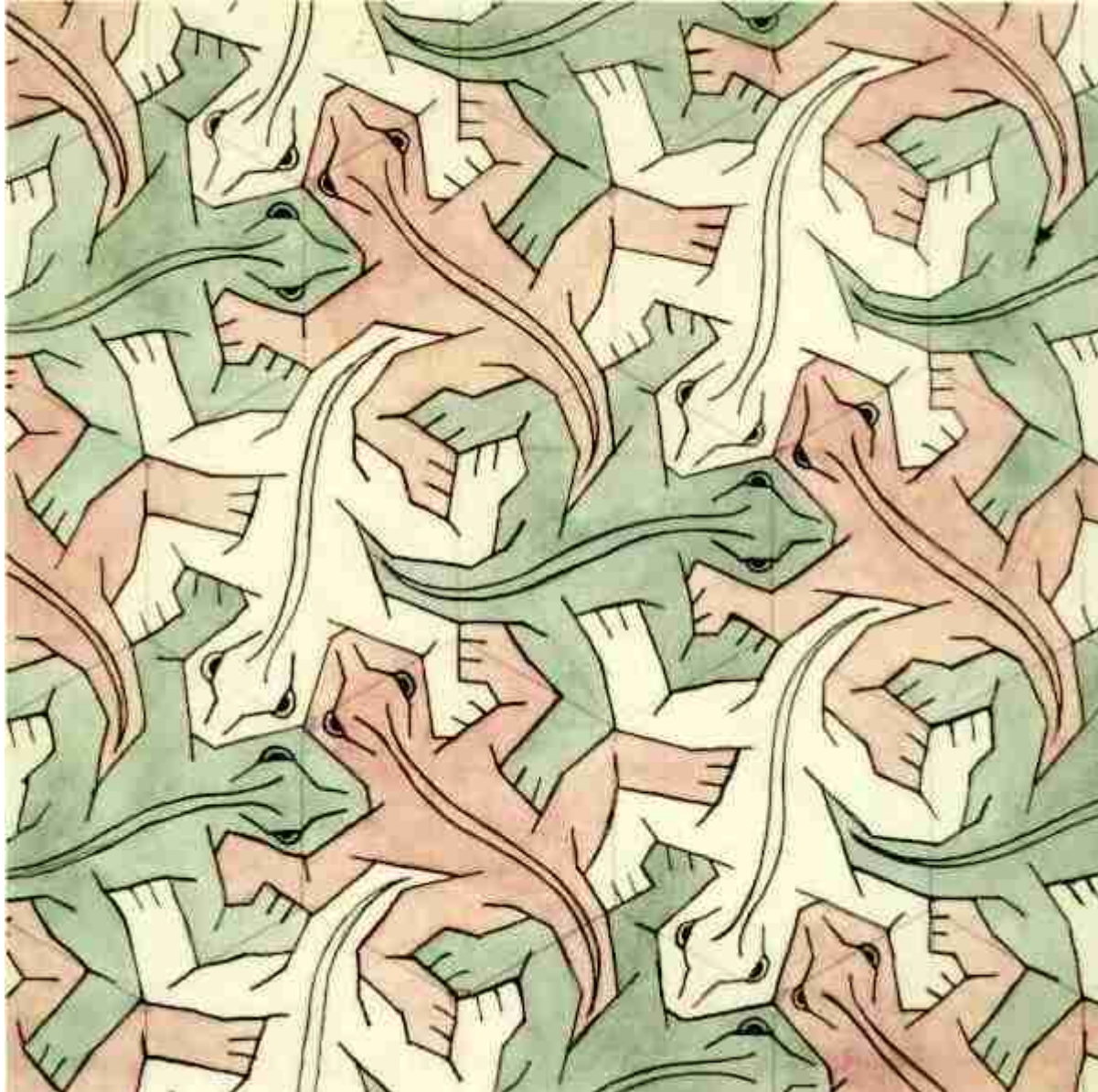
→ Reflections      > People



# Types of Symmetries

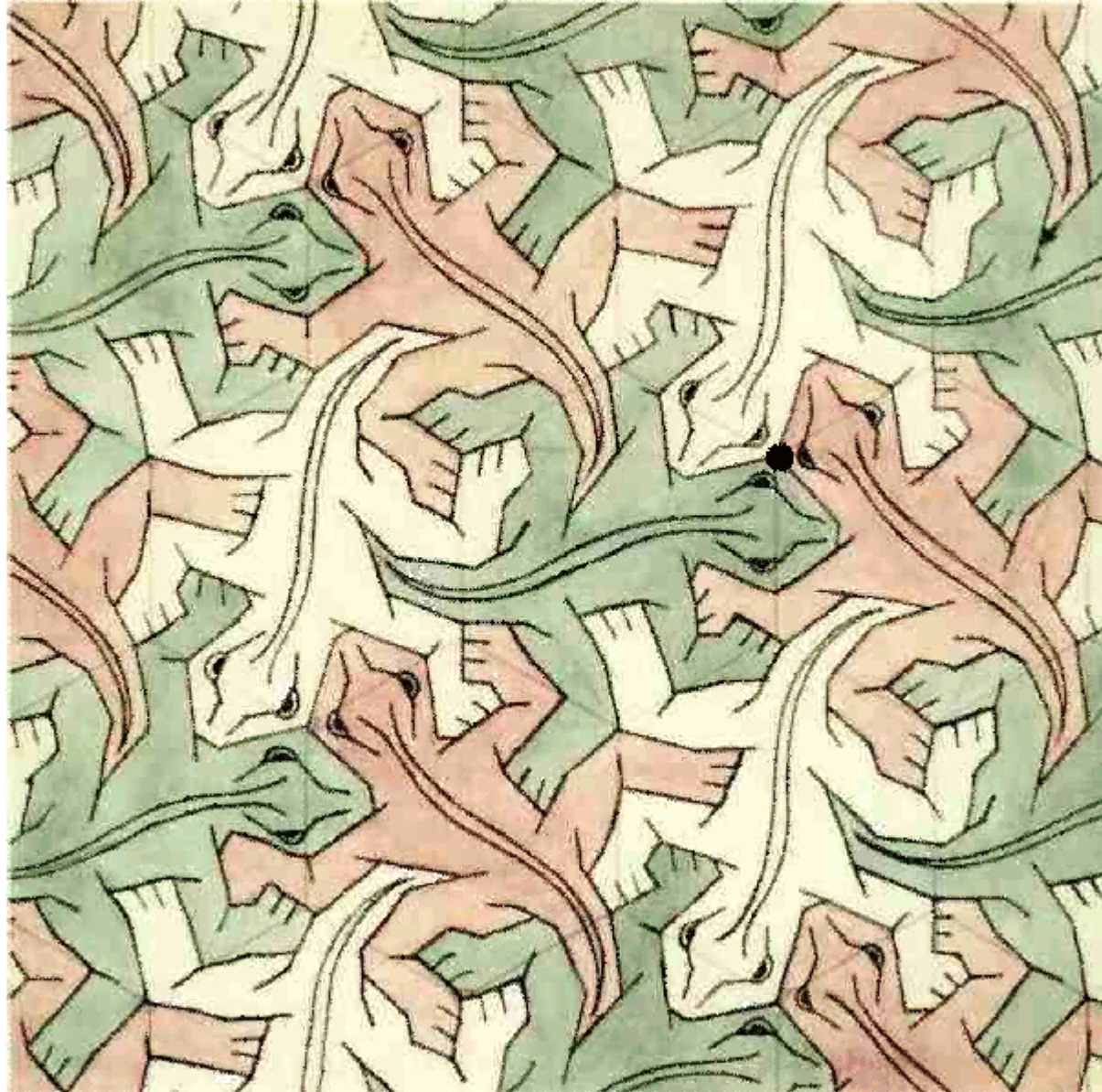
→ Rotations

→ Art: M.C. Escher



# Types of Symmetries

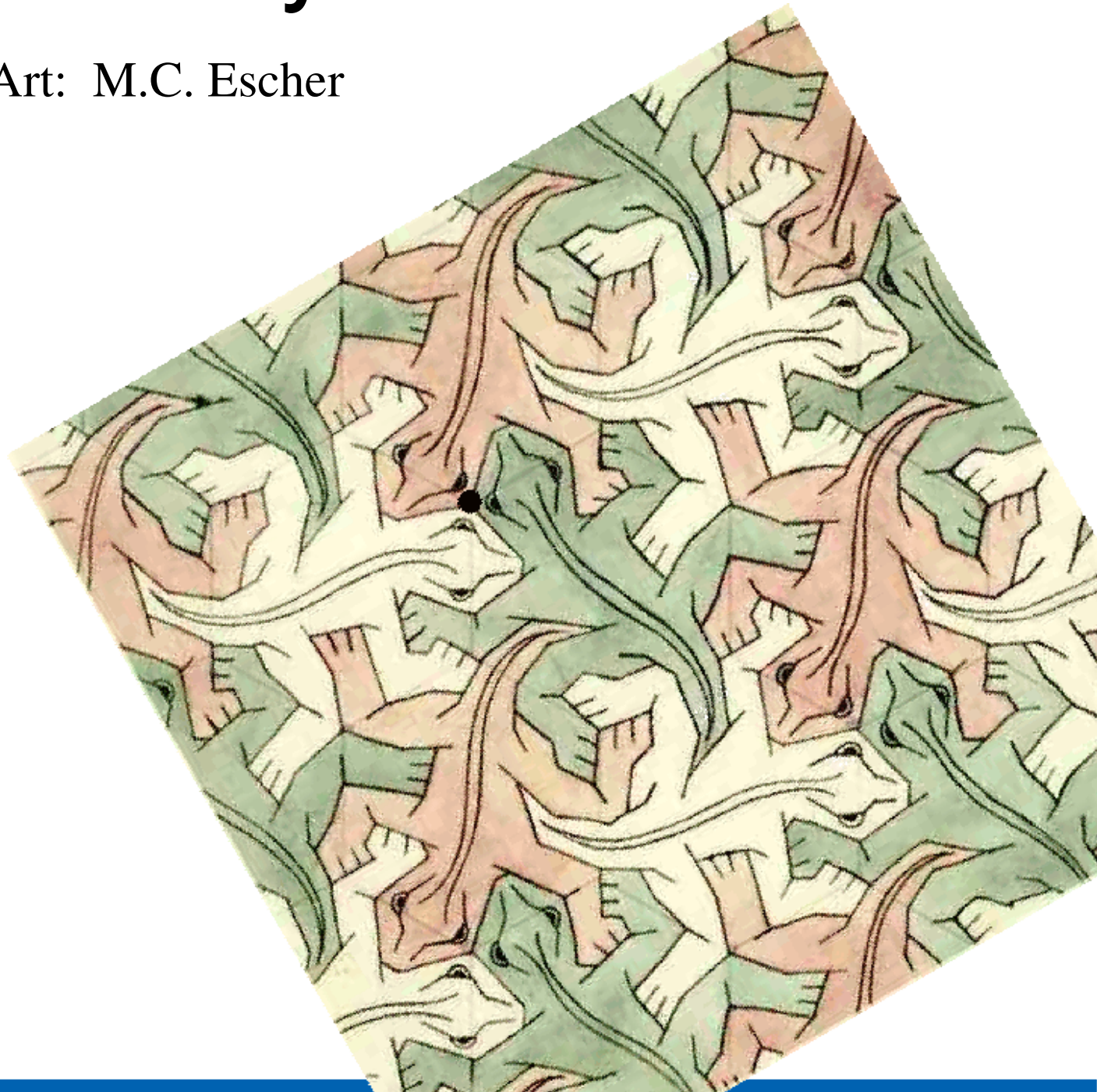
→ Rotations



# Types of Symmetries

→ Rotations

‣ Art: M.C. Escher





# Types of

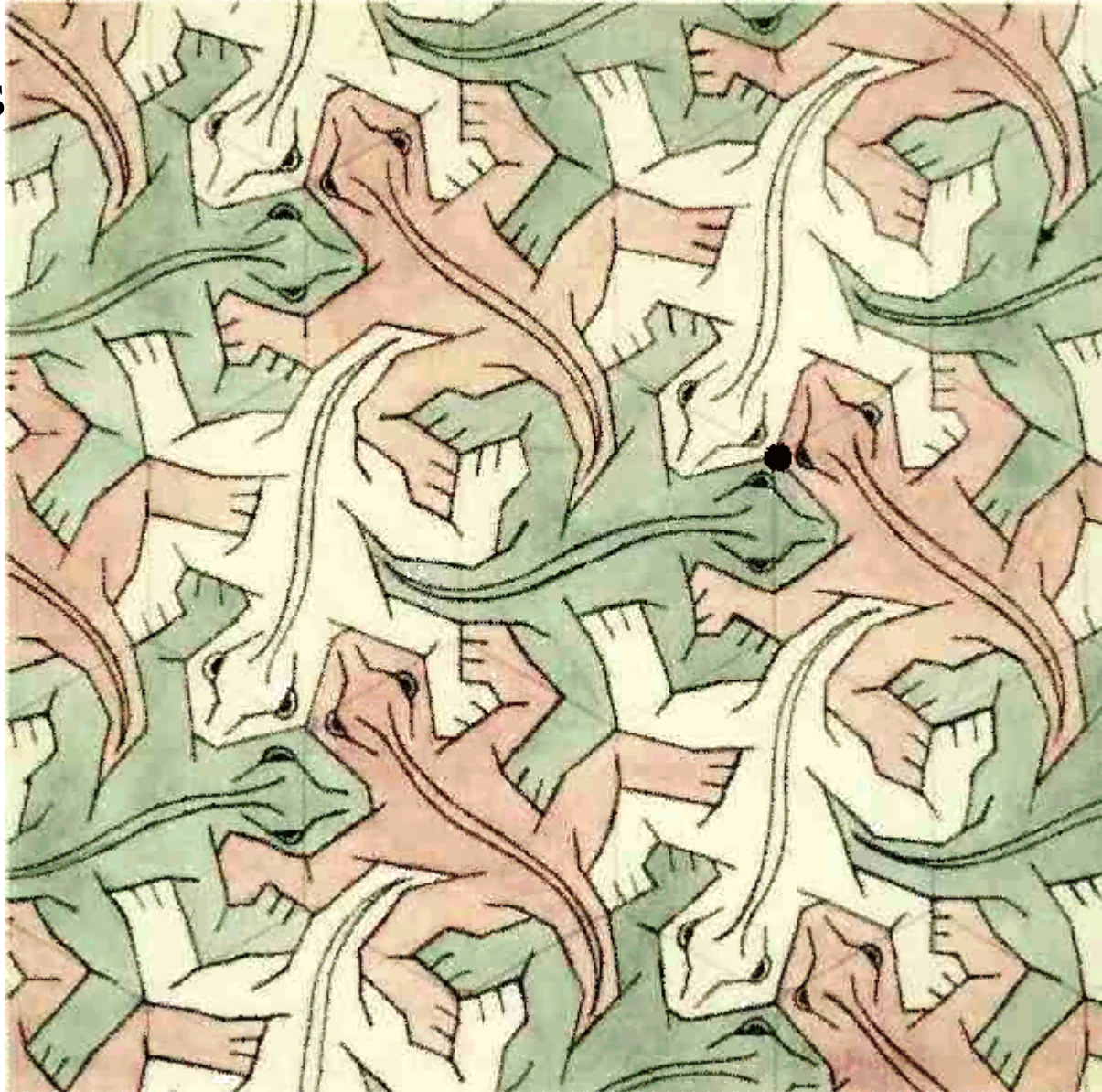
→ Rotations

→ Art:



# Types of Symmetries

→ Rotations



# Symmetries in Physics

Murray Gell-Mann's  
*“Eightfold Way”*

Organized the zoo of particles  
that emerged by 1961

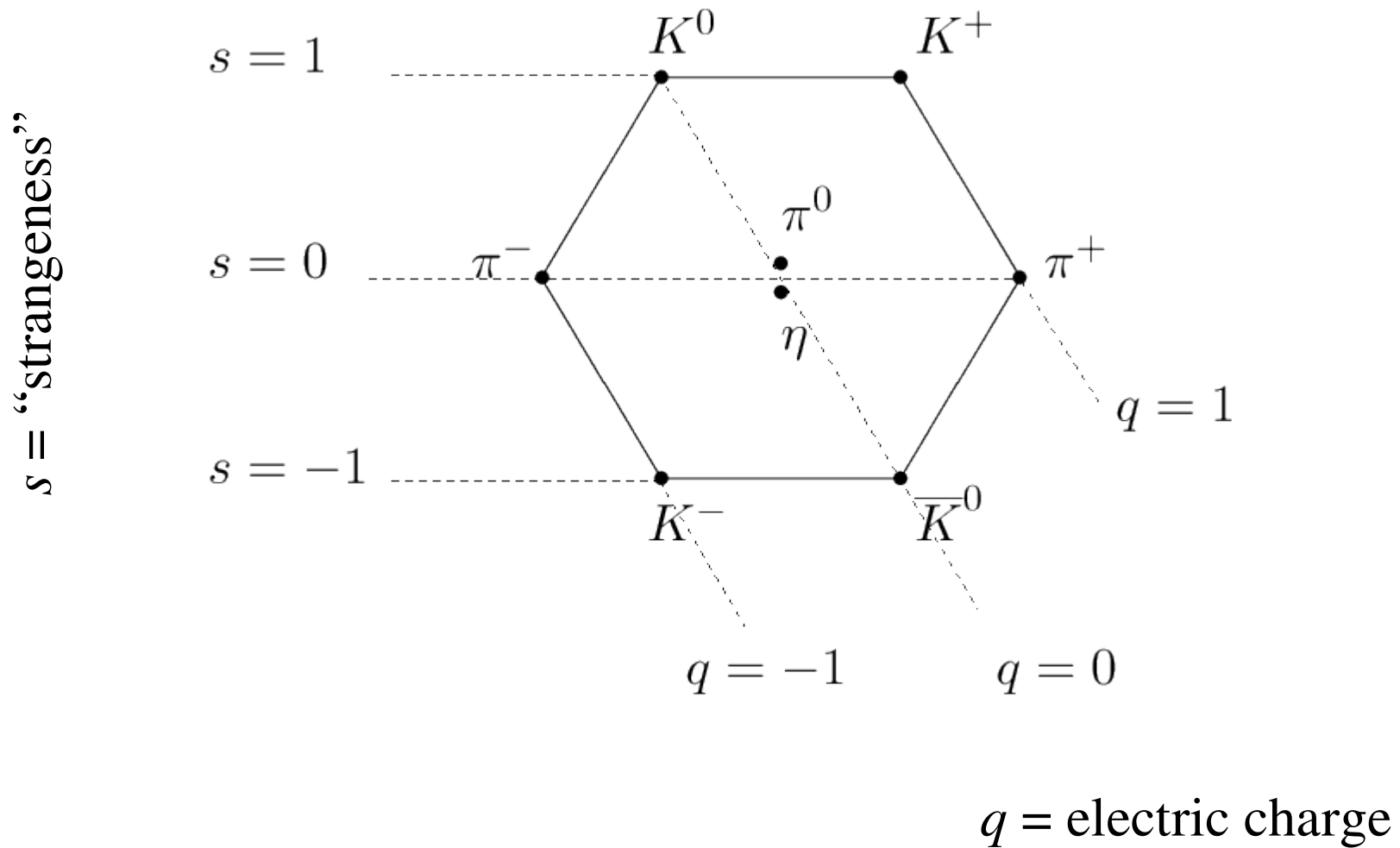
*c.f.* the Periodic Table



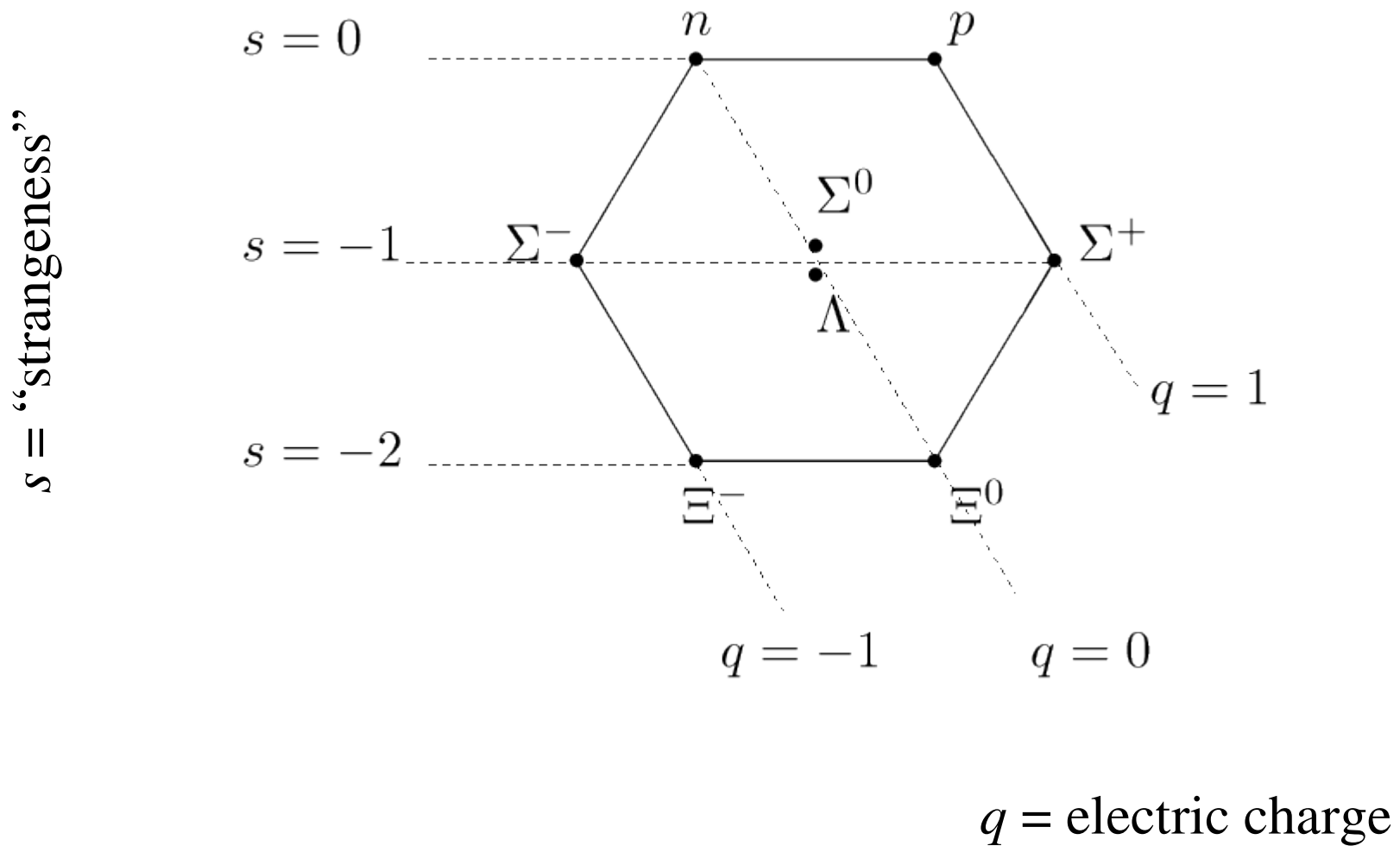
*“Young man, if I could remember the names of  
these particles, I would have been a botanist”*

Wolfgang Pauli to Leon Lederman

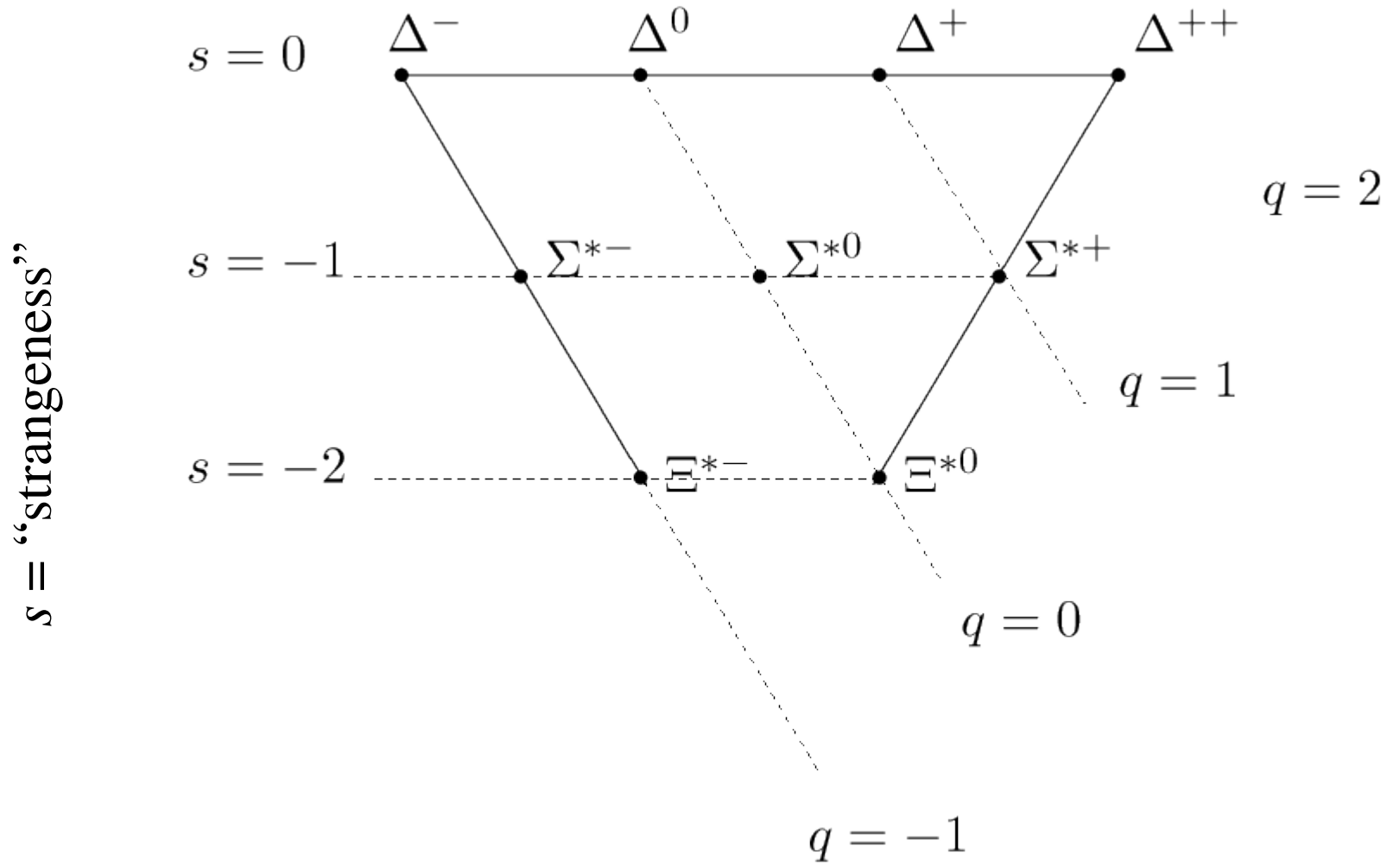
# The meson octet



# The baryon octet



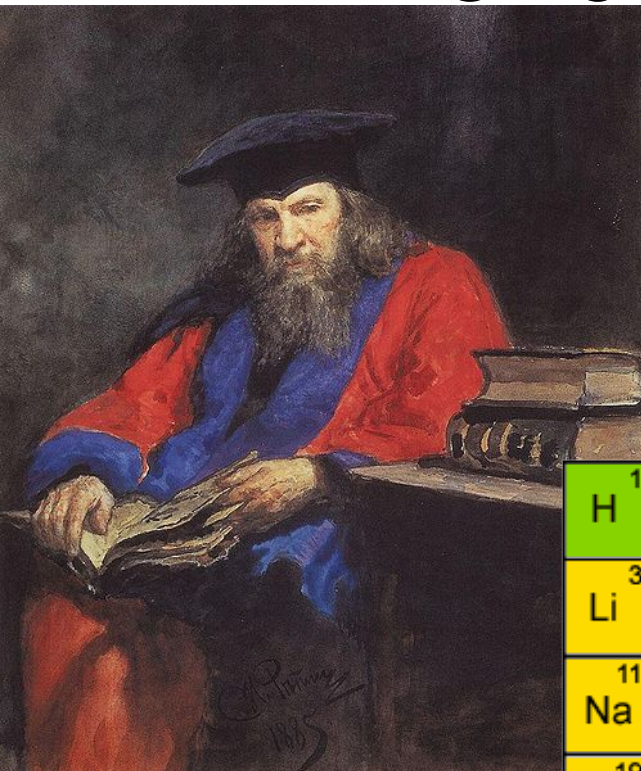
# The other baryons



$s = \text{“strangeness”}$

$q = \text{electric charge}$

# Mendeleev's bold prediction



Missing elements!

Periodic Table of the Elements

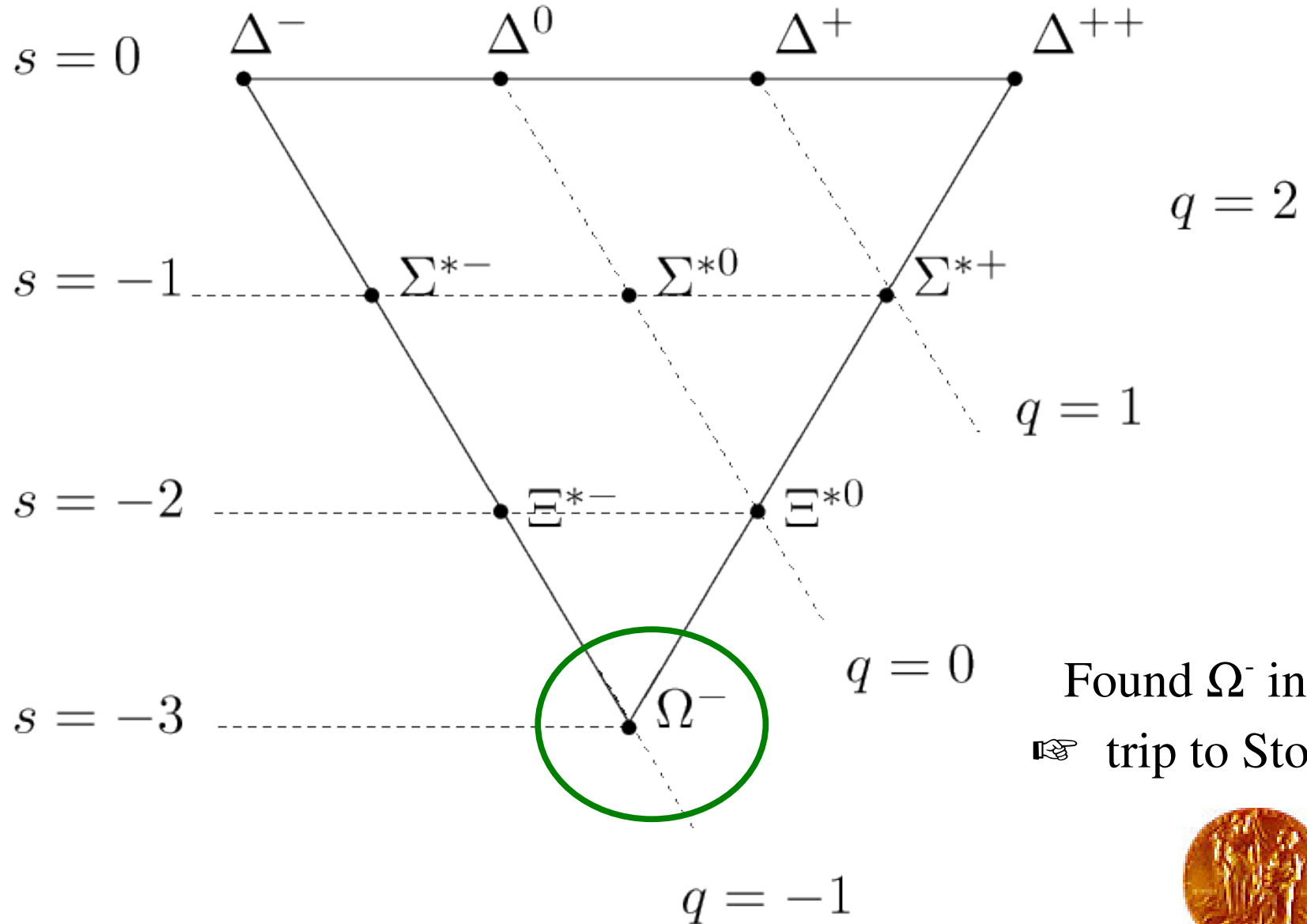
- hydrogen
- alkali metals
- alkali earth metals
- transition metals
- poor metals
- nonmetals
- noble gases
- rare earth metals

|          |          |          |            |            |            |            |            |            |            |          |          |          |          |          |          |          |          |
|----------|----------|----------|------------|------------|------------|------------|------------|------------|------------|----------|----------|----------|----------|----------|----------|----------|----------|
| 1<br>H   |          |          |            |            |            |            |            |            |            |          |          |          |          |          |          |          | 2<br>He  |
| 3<br>Li  | 4<br>Be  |          |            |            |            |            |            |            |            |          |          | 5<br>B   | 6<br>C   | 7<br>N   | 8<br>O   | 9<br>F   | 10<br>Ne |
| 11<br>Na | 12<br>Mg |          |            |            |            |            |            |            |            |          |          | 13<br>Al | 14<br>Si | 15<br>P  | 16<br>S  | 17<br>Cl | 18<br>Ar |
| 19<br>K  | 20<br>Ca |          | 22<br>Ti   | 23<br>V    | 24<br>Cr   | 25<br>Mn   | 26<br>Fe   | 27<br>Co   | 28<br>Ni   | 29<br>Cu | 30<br>Zn |          |          | 33<br>As | 34<br>Se | 35<br>Br | 36<br>Kr |
| 37<br>Rb | 38<br>Sr | 39<br>Y  | 40<br>Zr   | 41<br>Nb   | 42<br>Mo   | 43<br>Tc   | 44<br>Ru   | 45<br>Rh   | 46<br>Pd   | 47<br>Ag | 48<br>Cd | 49<br>In | 50<br>Sn | 51<br>Sb | 52<br>Te | 53<br>I  | 54<br>Xe |
| 55<br>Cs | 56<br>Ba | 57<br>La | 72<br>Hf   | 73<br>Ta   | 74<br>W    | 75<br>Re   | 76<br>Os   | 77<br>Ir   | 78<br>Pt   | 79<br>Au | 80<br>Hg | 81<br>Tl | 82<br>Pb | 83<br>Bi | 84<br>Po | 85<br>At | 86<br>Rn |
| 87<br>Fr | 88<br>Ra | 89<br>Ac | 104<br>Unq | 105<br>Unp | 106<br>Unh | 107<br>Uns | 108<br>Uno | 109<br>Une | 110<br>Unn |          |          |          |          |          |          |          |          |

Sc, Ga & Ge  
all discovered  
20 yrs after their  
existence was predicted

|          |          |          |          |          |          |          |          |          |          |           |           |           |           |
|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|-----------|-----------|-----------|-----------|
| 58<br>Ce | 59<br>Pr | 60<br>Nd | 61<br>Pm | 62<br>Sm | 63<br>Eu | 64<br>Gd | 65<br>Tb | 66<br>Dy | 67<br>Ho | 68<br>Er  | 69<br>Tm  | 70<br>Yb  | 71<br>Lu  |
| 90<br>Th | 91<br>Pa | 92<br>U  | 93<br>Np | 94<br>Pu | 95<br>Am | 96<br>Cm | 97<br>Bk | 98<br>Cf | 99<br>Es | 100<br>Fm | 101<br>Md | 102<br>No | 103<br>Lr |

# Gell-Mann: the Mendeleev of particle physics



Found  $\Omega^-$  in 1964

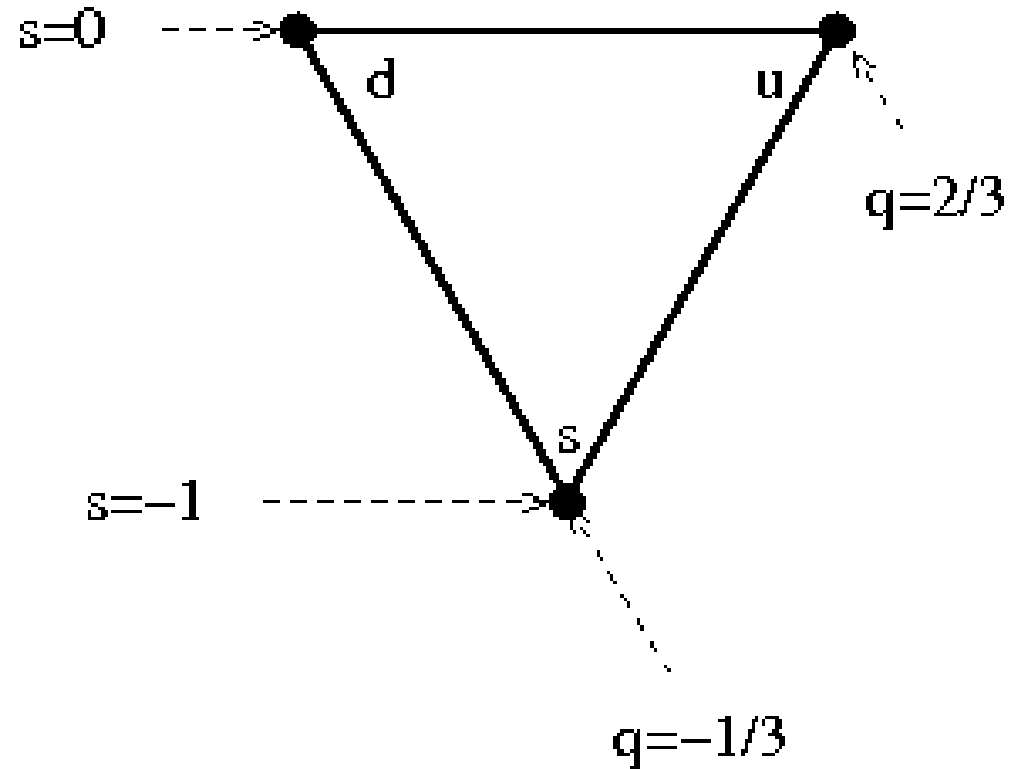
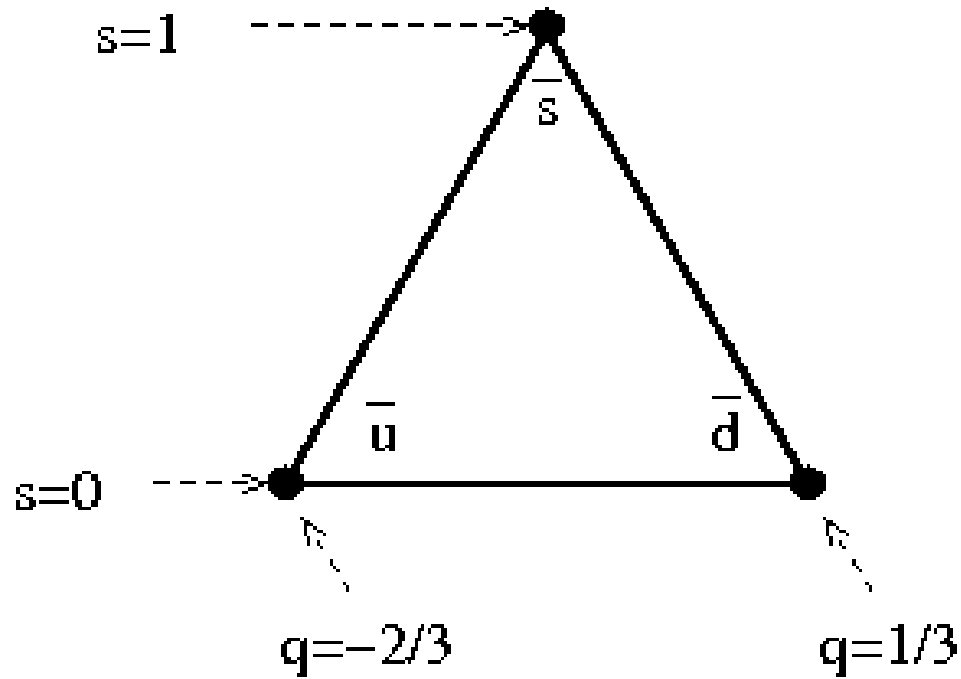
👉 trip to Stockholm!





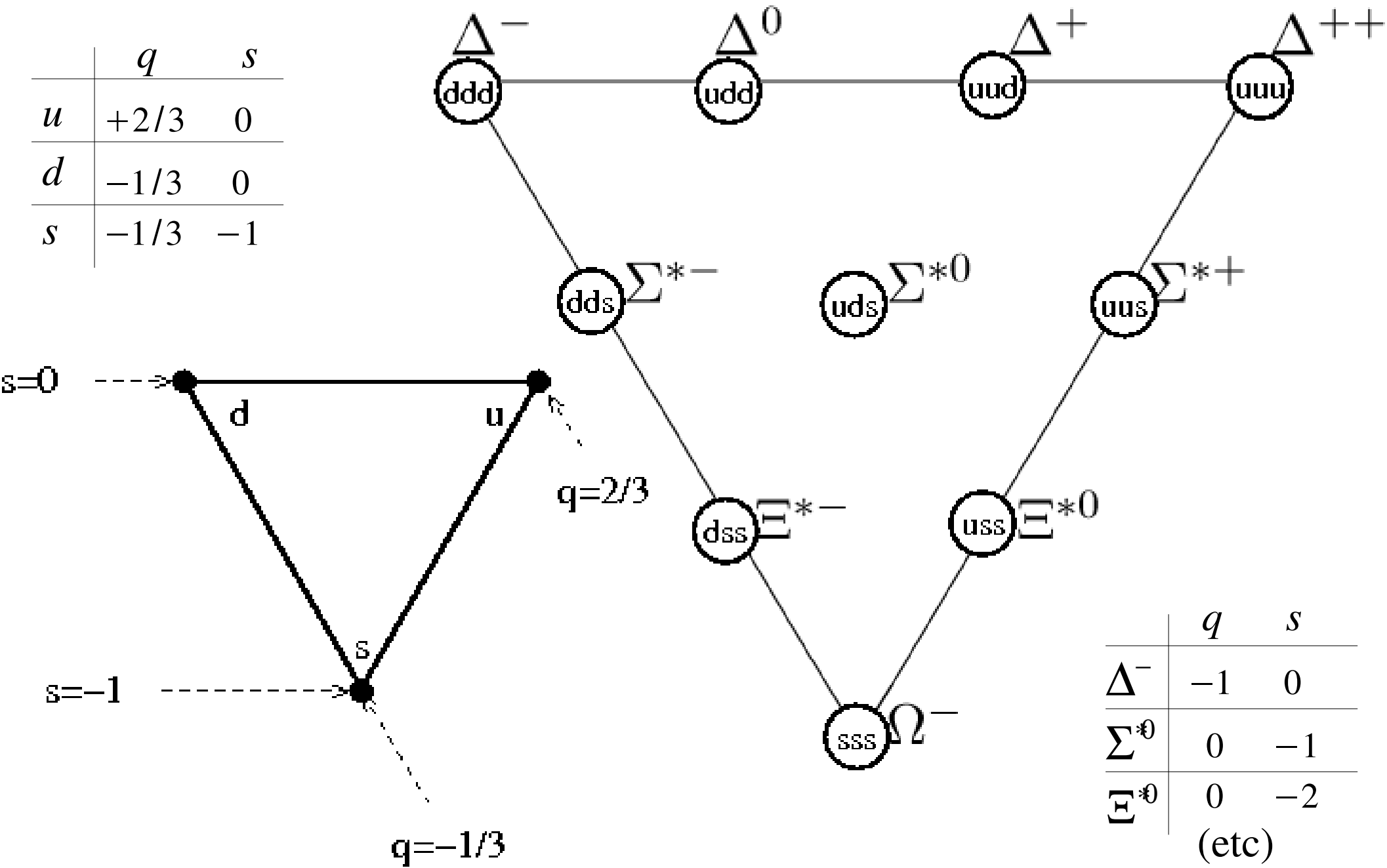
# Multiplet of quarks/anti-quarks

Gell-Mann & Zweig



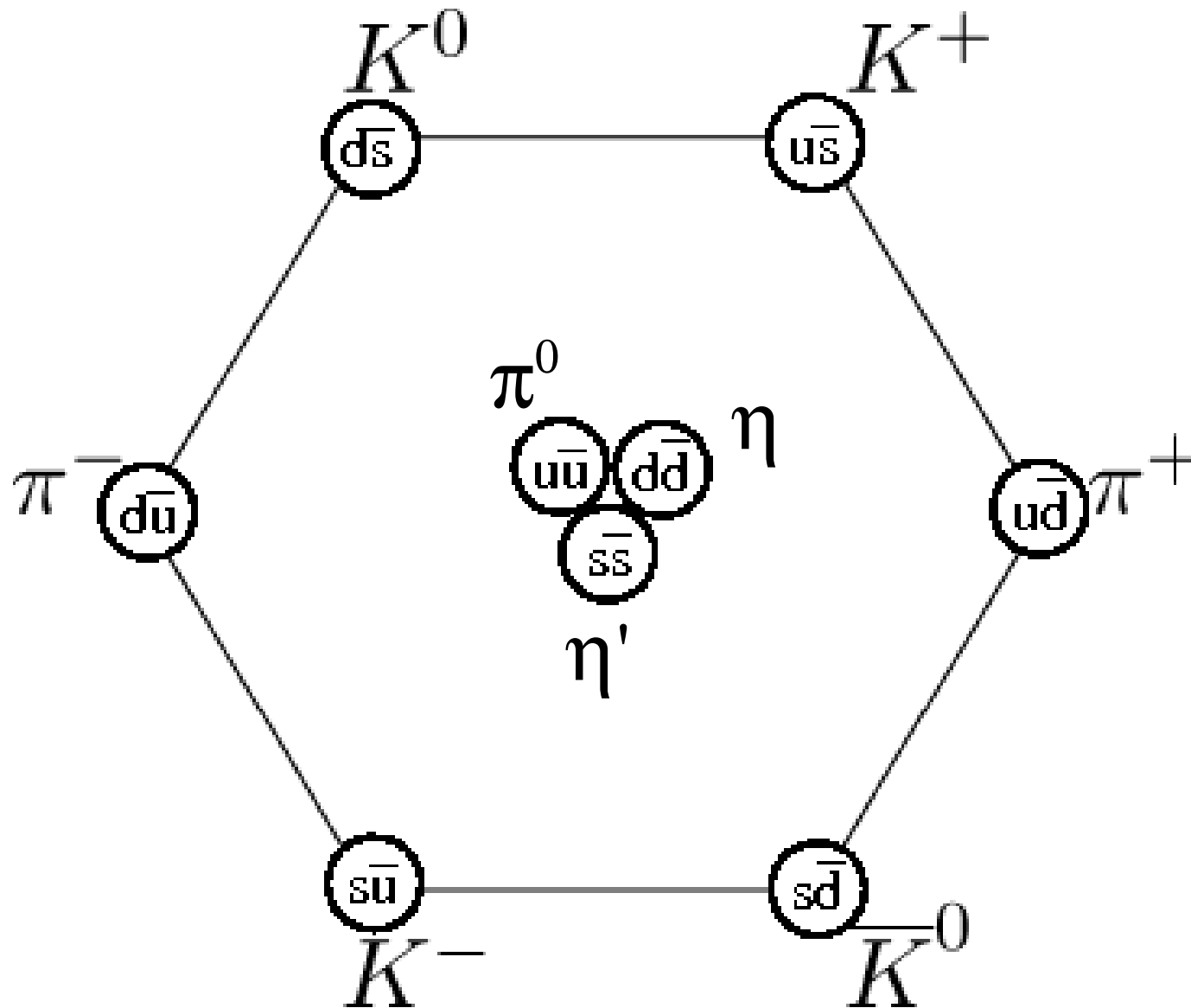
# Baryon decuplet in terms of quarks

|     | $q$    | $s$  |
|-----|--------|------|
| $u$ | $+2/3$ | $0$  |
| $d$ | $-1/3$ | $0$  |
| $s$ | $-1/3$ | $-1$ |



|               | $q$  | $s$   |
|---------------|------|-------|
| $\Delta^-$    | $-1$ | $0$   |
| $\Sigma^{*0}$ | $0$  | $-1$  |
| $\Xi^{*0}$    | $0$  | $-2$  |
|               |      | (etc) |

# The meson *nonet*



# Basic constituents of matter

## FERMIONS

matter constituents  
spin = 1/2, 3/2, 5/2, ...

### Leptons spin = 1/2

| Flavor                     | Mass<br>GeV/c <sup>2</sup>   | Electric<br>charge |
|----------------------------|------------------------------|--------------------|
| $\nu_L$ lightest neutrino* | $(0-0.13)\times 10^{-9}$     | 0                  |
| <b>e</b> electron          | 0.000511                     | -1                 |
| $\nu_M$ middle neutrino*   | $(0.009-0.13)\times 10^{-9}$ | 0                  |
| $\mu$ muon                 | 0.106                        | -1                 |
| $\nu_H$ heaviest neutrino* | $(0.04-0.14)\times 10^{-9}$  | 0                  |
| $\tau$ tau                 | 1.777                        | -1                 |

### Quarks spin = 1/2

| Flavor           | Approx.<br>Mass<br>GeV/c <sup>2</sup> | Electric<br>charge |
|------------------|---------------------------------------|--------------------|
| <b>u</b> up      | 0.002                                 | 2/3                |
| <b>d</b> down    | 0.005                                 | -1/3               |
| <b>c</b> charm   | 1.3                                   | 2/3                |
| <b>s</b> strange | 0.1                                   | -1/3               |
| <b>t</b> top     | 173                                   | 2/3                |
| <b>b</b> bottom  | 4.2                                   | -1/3               |

# Fundamental symmetries

**Noether's Theorem:** Symmetries  $\leftrightarrow$  Conservation Law



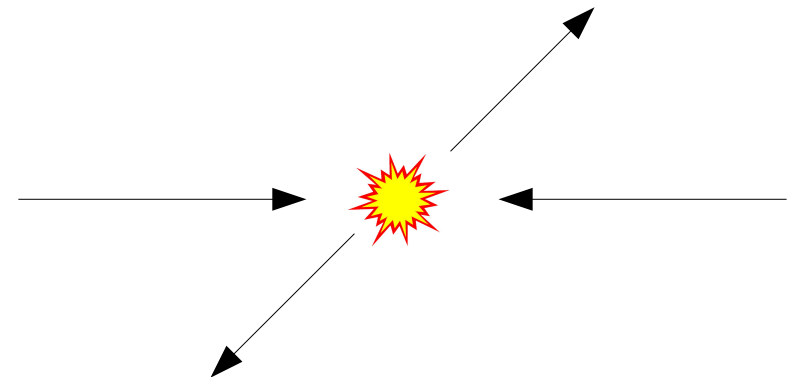
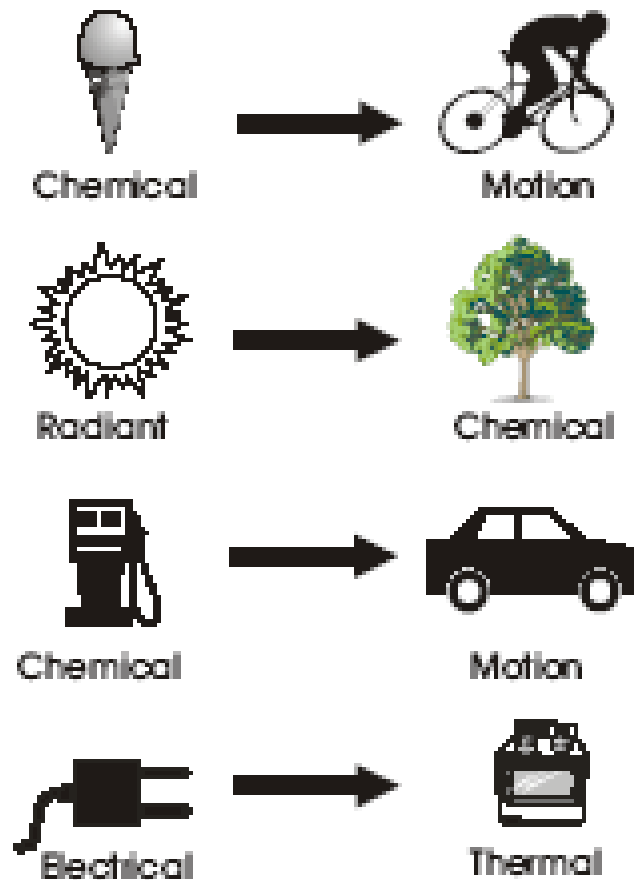
# Fundamental symmetries

**Noether's Theorem:** Symmetries  $\leftrightarrow$  Conservation Law

Energy is conserved

$\leftrightarrow$

time-reversal symmetry



# Fundamental symmetries

**Noether's Theorem:** Symmetries  $\leftrightarrow$  Conservation Law

Energy is conserved  $\leftrightarrow$  time-reversal symmetry

Momentum is conserved  $\leftrightarrow$  translational symmetry

Angular momentum is conserved  $\leftrightarrow$  rotational symmetry

Charge is conserved  $\leftrightarrow$  “gauge” symmetry

⋮

⋮

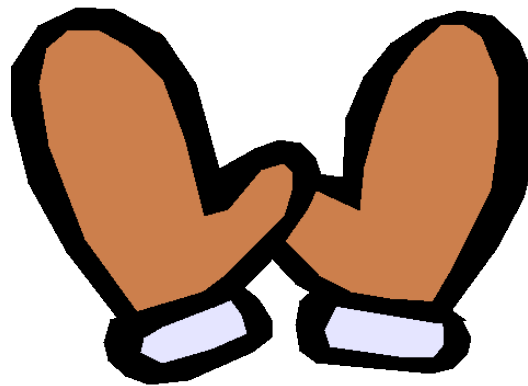
# History of parity



# History of parity

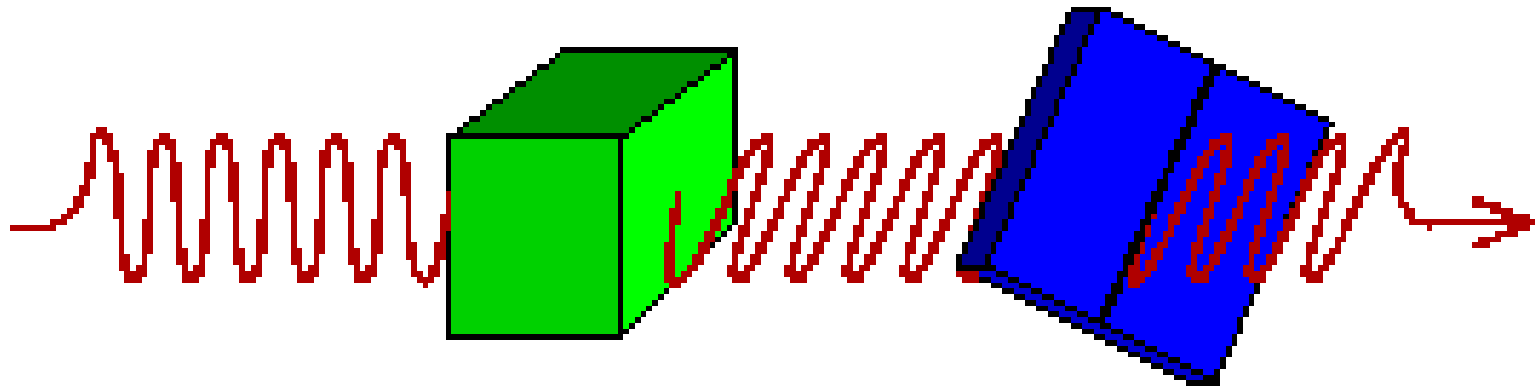
- 1786: Kant debates the nature of incongruent counterparts

Hmmmm ...



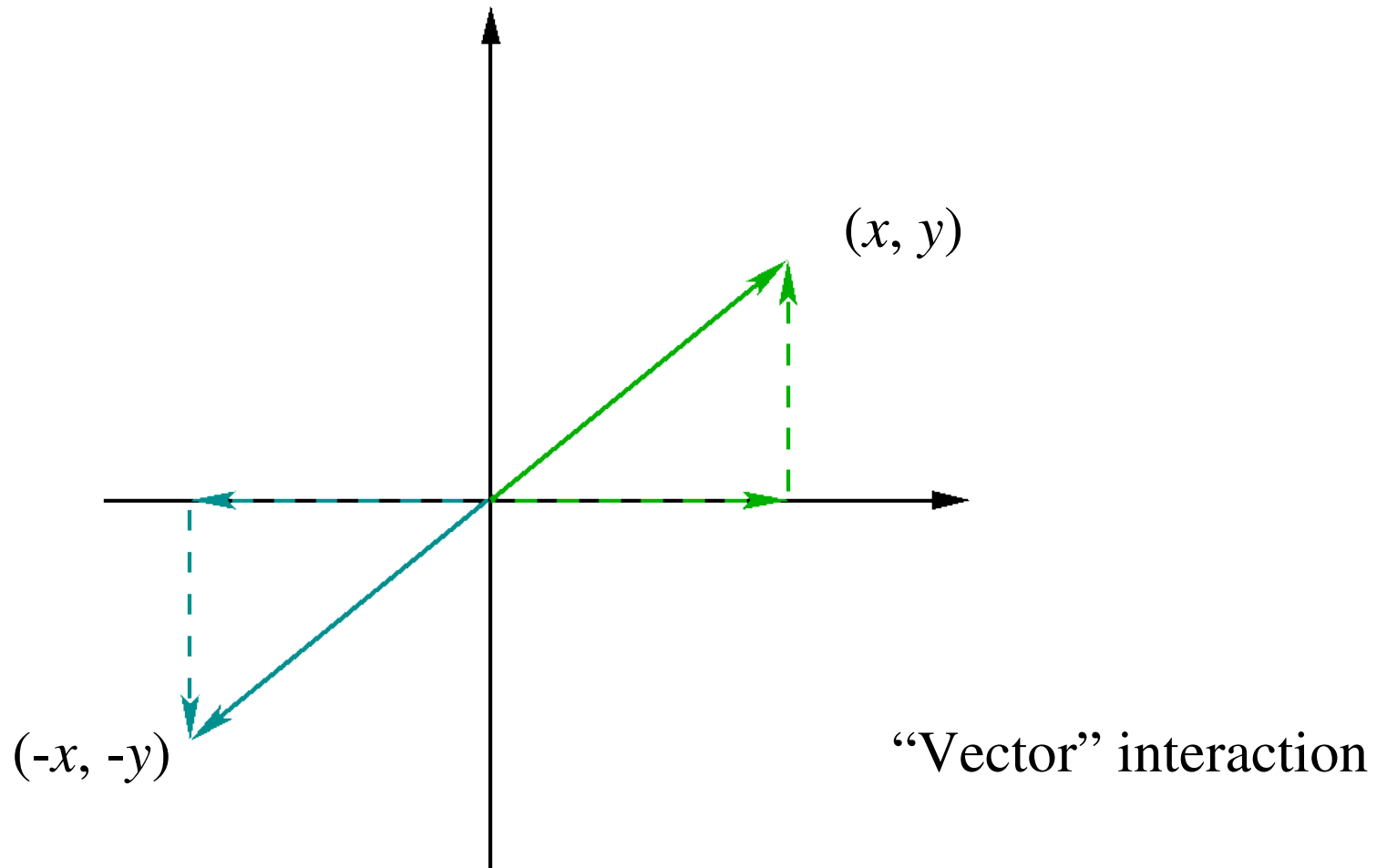
# History of parity

- 1786: Kant debates the nature of incongruent counterparts
- 1848: Pasteur observes optical rotation in chemical isomers



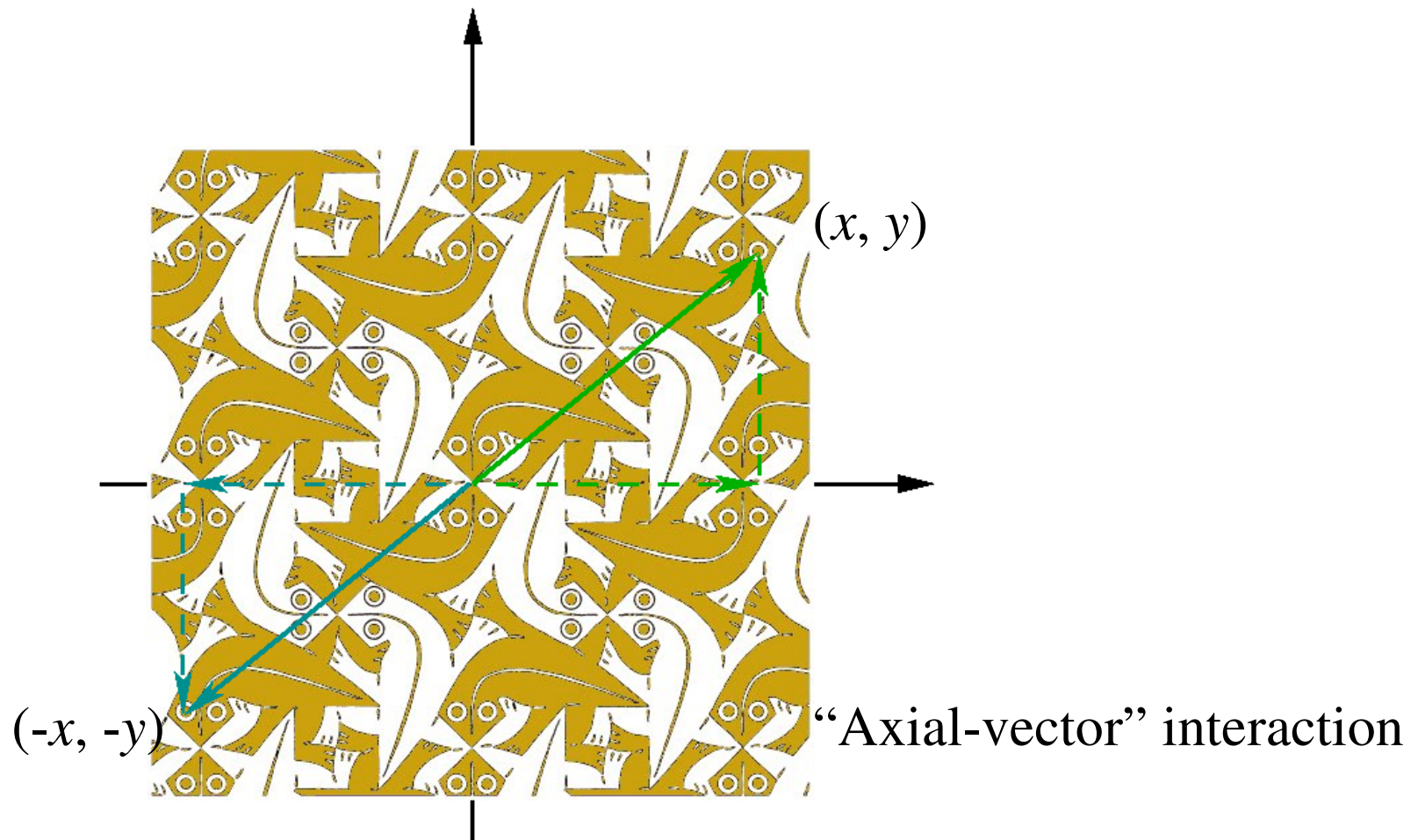
# History of parity

- 1786: Kant debates the nature of incongruent counterparts
- 1848: Pasteur observes optical rotation in chemical isomers
- 1924: Laporte introduces idea of parity conservation in quantum mechanics



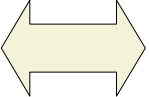
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# History of parity

- 1786: Kant debates the nature of incongruent counterparts
- 1848: Pasteur observes optical rotation in chemical isomers
- 1924: Laporte introduces idea of parity conservation in quantum mechanics

Intrinsic parity  helicity or “handedness”



# History of parity

- 1786: Kant debates the nature of incongruent counterparts
- 1848: Pasteur observes optical rotation in chemical isomers
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# History of parity

- 1786: Kant debates the nature of incongruent counterparts
- 1848: Pasteur observes optical rotation in chemical isomers
- 1924: Laporte introduces idea of parity conservation in quantum mechanics
- 1927: Wigner proves Maxwell's equations of electromagnetism conserve parity

⋮

- 1953: Experiments indicate weak interaction is (S,T)
- 1953: Dalitz points out “ $\theta\tau$  puzzle”:

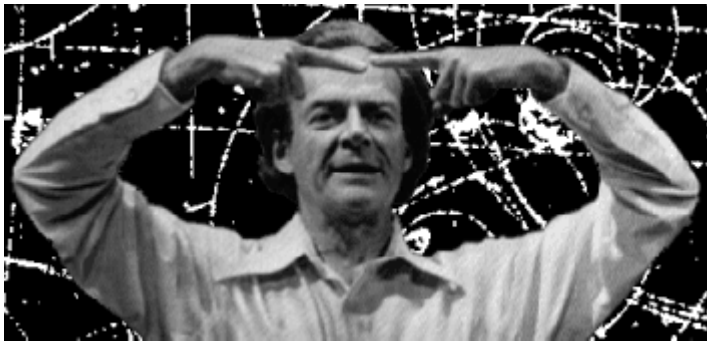
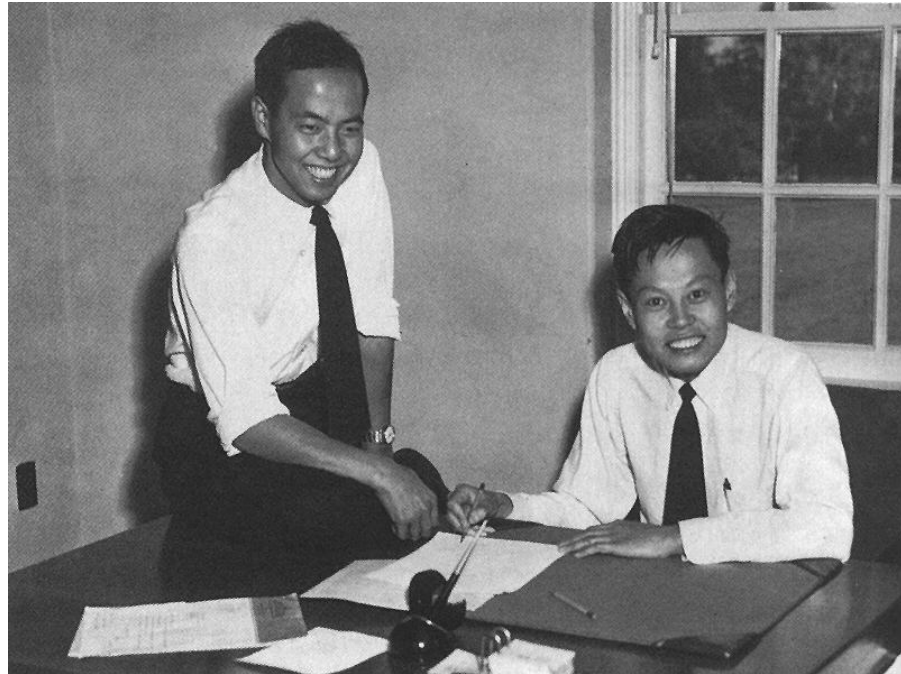
$$\theta \rightarrow \pi^0 \pi^+ \quad \text{vs} \quad \tau \rightarrow \pi^+ \pi^+ \pi^-$$

same half-life, same mass, same charge, ...

# Is parity always conserved?

Prompted Lee and Yang to note:

*“... existing experiments do indicate parity conservation in strong and electromagnetic interactions, but that for weak interactions ... parity conservation is so far only an extrapolated hypothesis, unsupported by experimental evidence.”*



Feynman bets parity stays conserved



# C.S. Wu's experiment

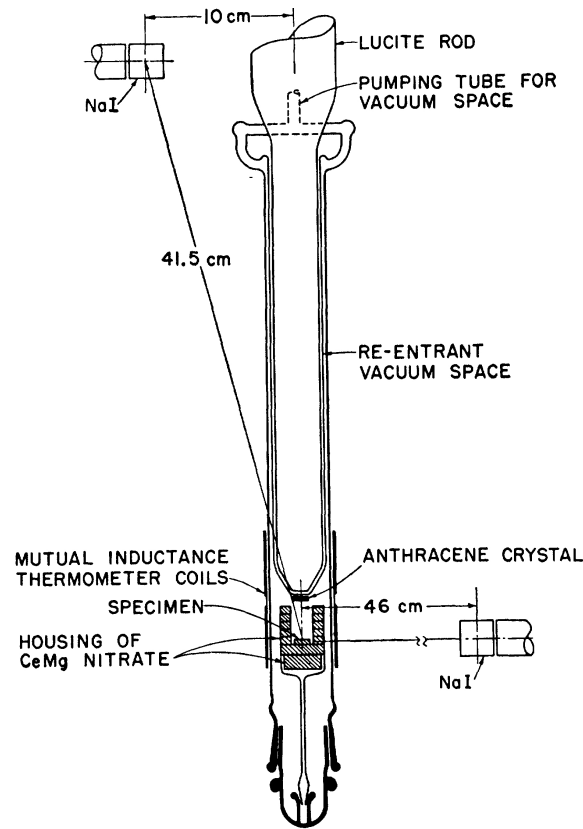
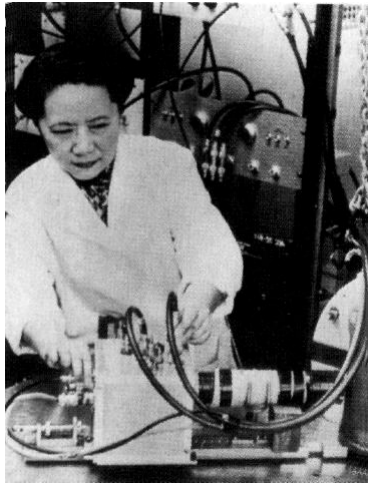
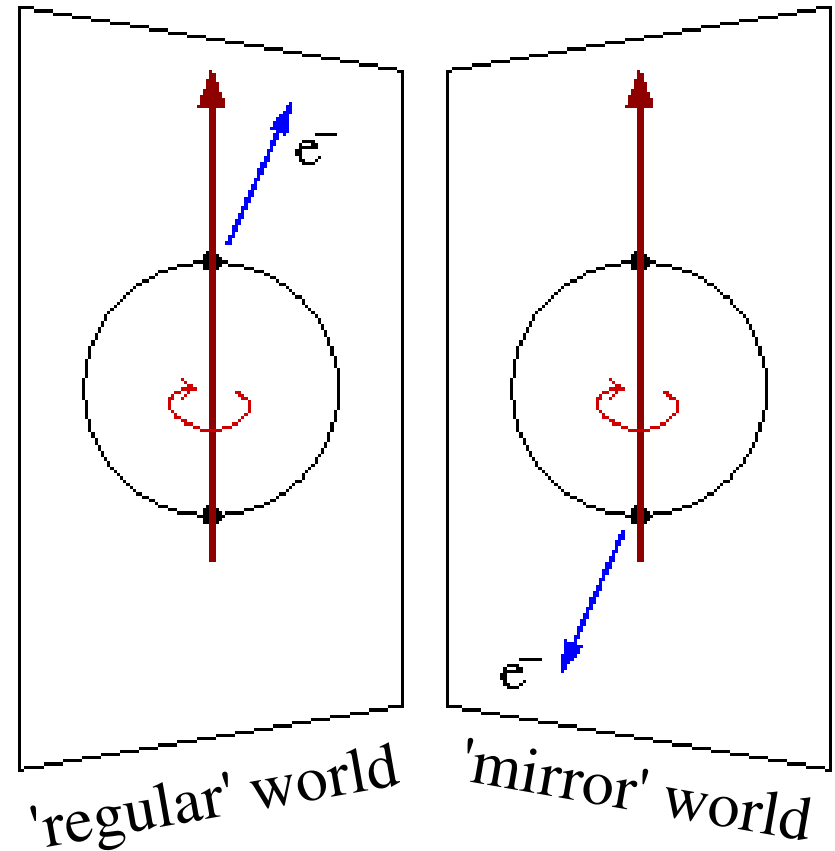


FIG. 1. Schematic drawing of the lower part of the cryostat.

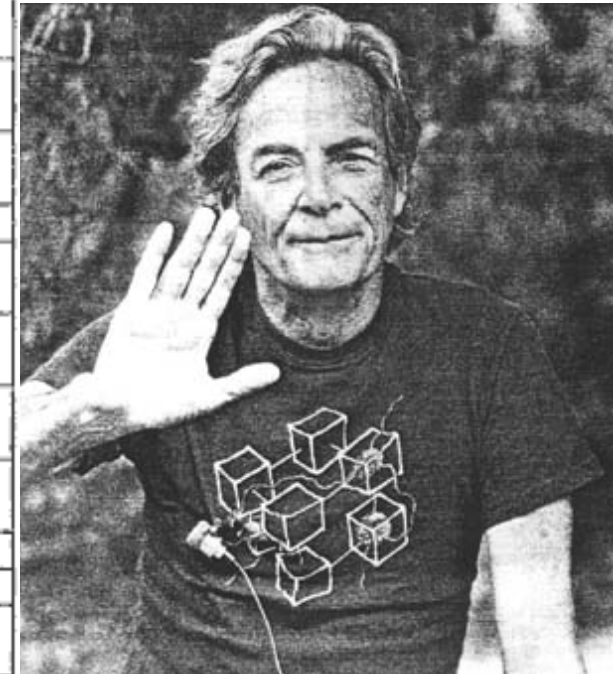
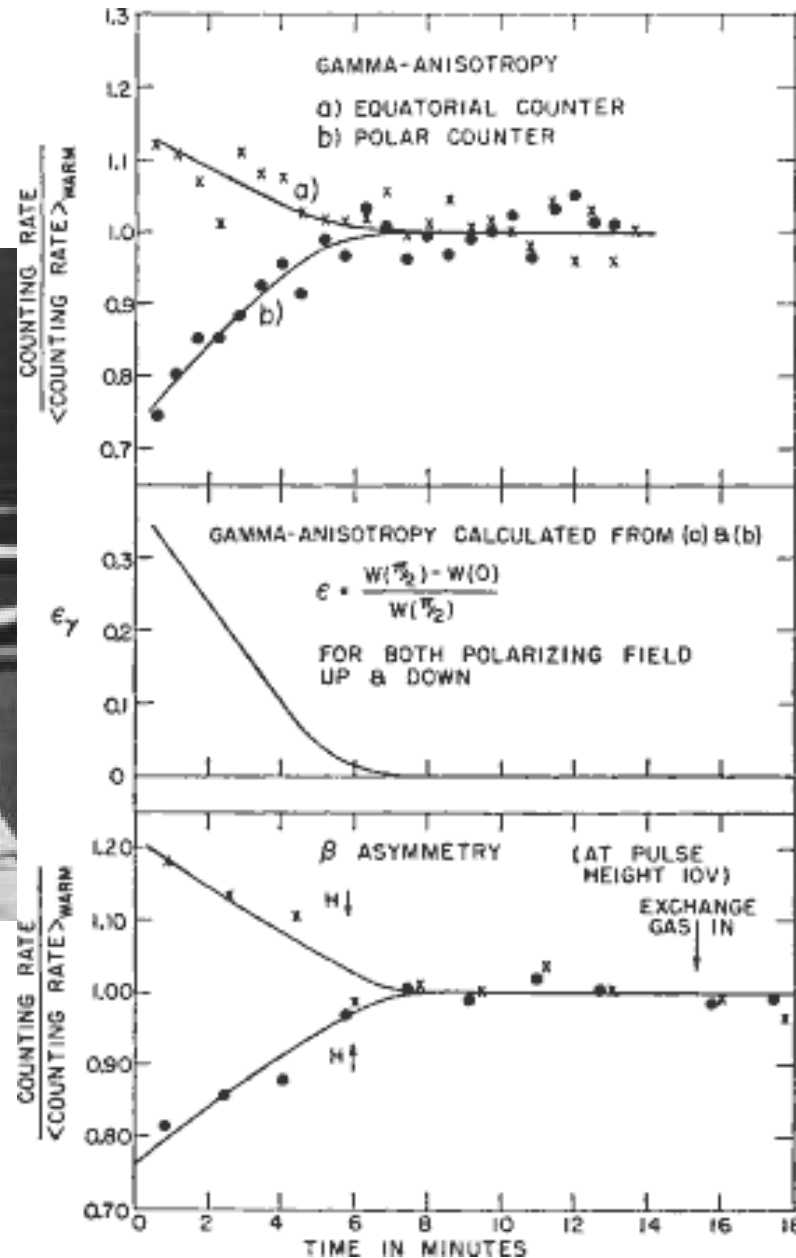


$e^-$  direction is a vector:  $\mathbf{p} = \Delta\mathbf{x}/\Delta t \rightarrow -\mathbf{p}$

*spin* is an axial-vector:  $\mathbf{J} = \mathbf{r} \times \mathbf{p} \rightarrow \mathbf{J}$

If there is a correlation between  $\mathbf{p}$  and  $\mathbf{J}$ , parity is not conserved!

# Feynman loses \$50



**Parity is NOT conserved in weak interactions!**

# Now the question is ...

The standard model of particle physics assumes the weak interaction is

$$V - A$$

which *maximally* violates parity (not  $V - 0.1A$ , for example)

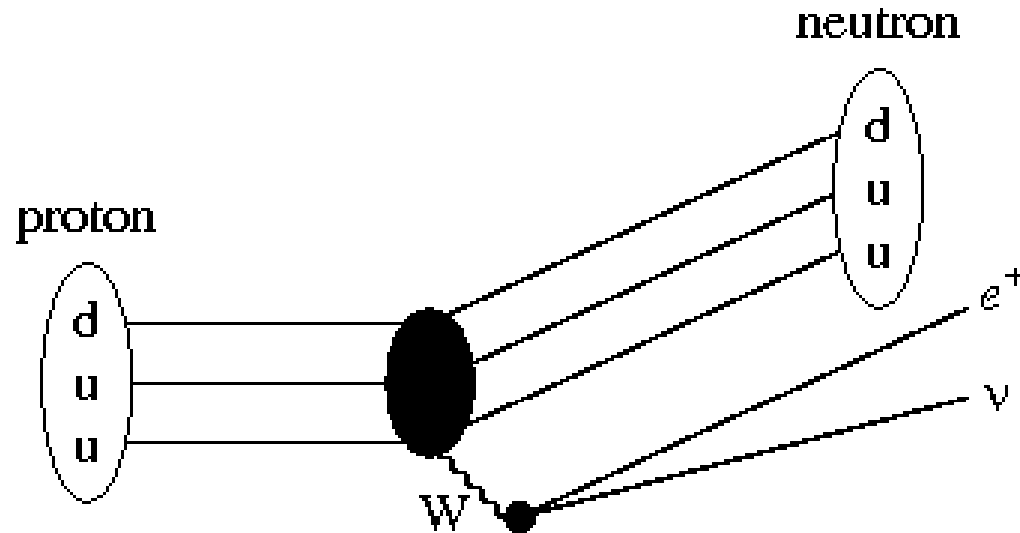
Are there any  $V + A$  components we just haven't seen yet?

Is Nature truly left-handed, or is it ambidextrous?

Why would it care whether a process occurred in the mirror world or not?

# Nuclear physics continues the search

Nuclear  $\beta$  decay:



Textbook assumptions:

- decay occurs from rest
- decay occurs from a point-source
- the particles escape without distortions
- the polarization is perfect

# Magneto-optical traps



Steven Chu



Claude Cohen-Tannoudji



William Philips

1997



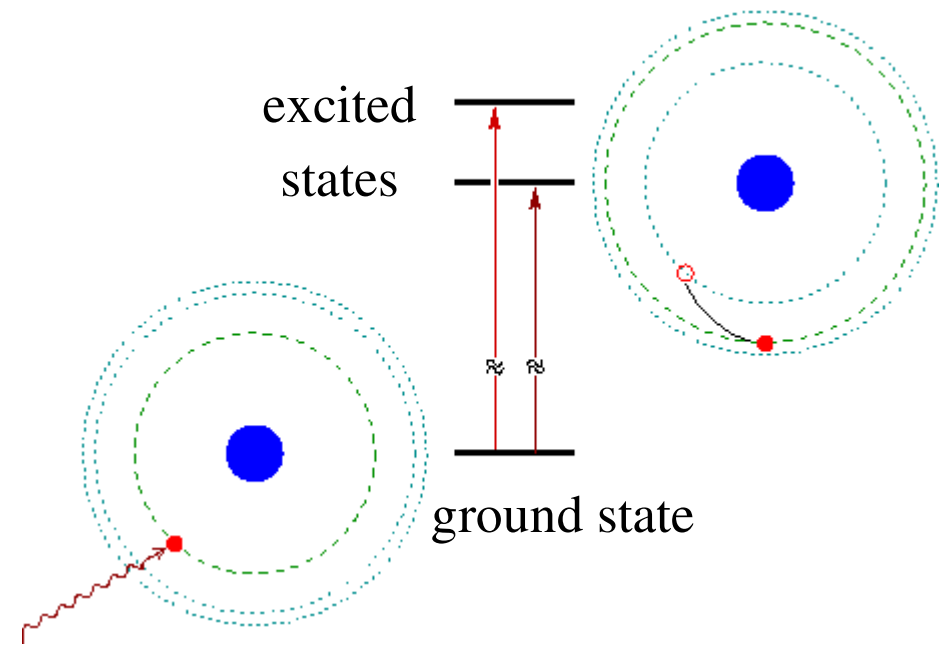
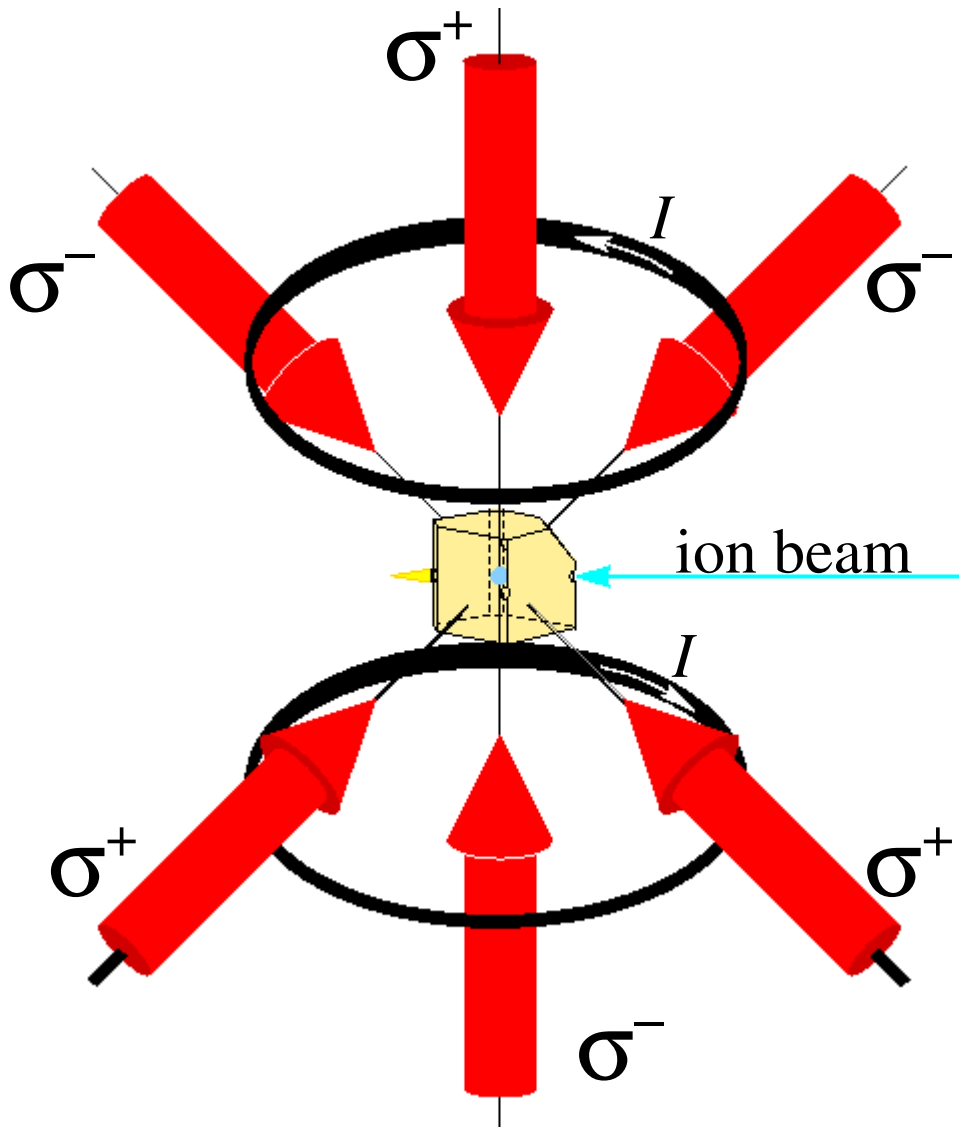
“For development of methods to cool and trap atoms with laser light”

Textbook assumptions:

- decay occurs from rest ✓
- decay occurs from a point-source ✓
- the particles escape without distortions ✓
- the polarization is perfect ?

# A vapour-cell MOT

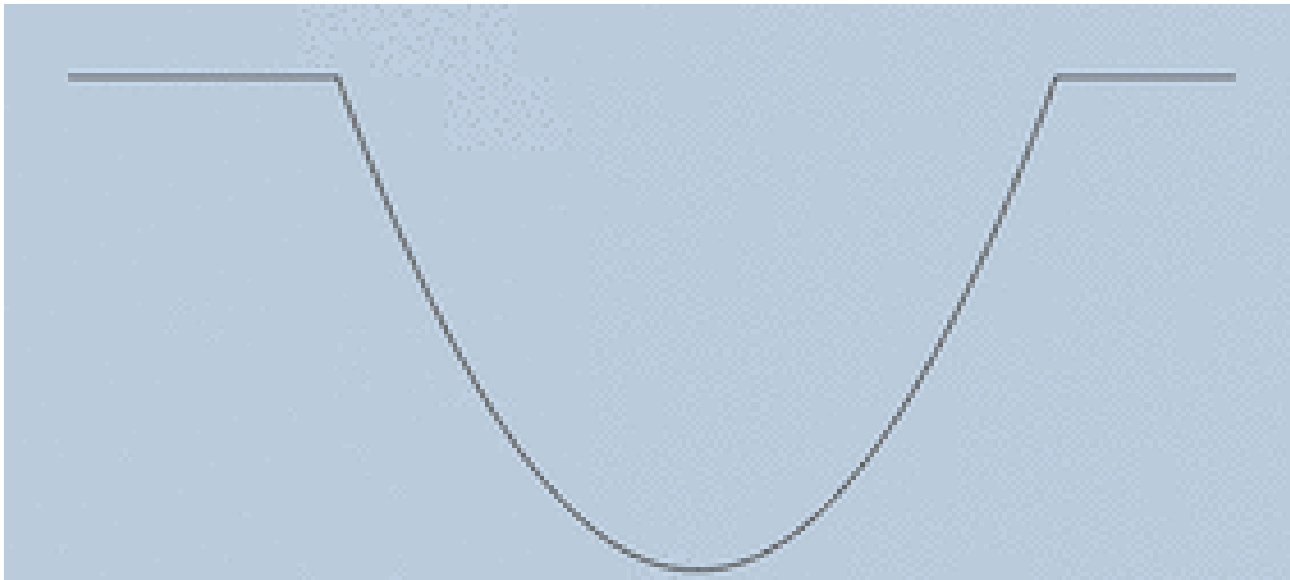
Laser excites atomic transitions:



# Basic idea behind *any* trap

**Speed**-dependent force: dampens the motion and slows particles down

**Position**-dependent force: defines where particles get trapped

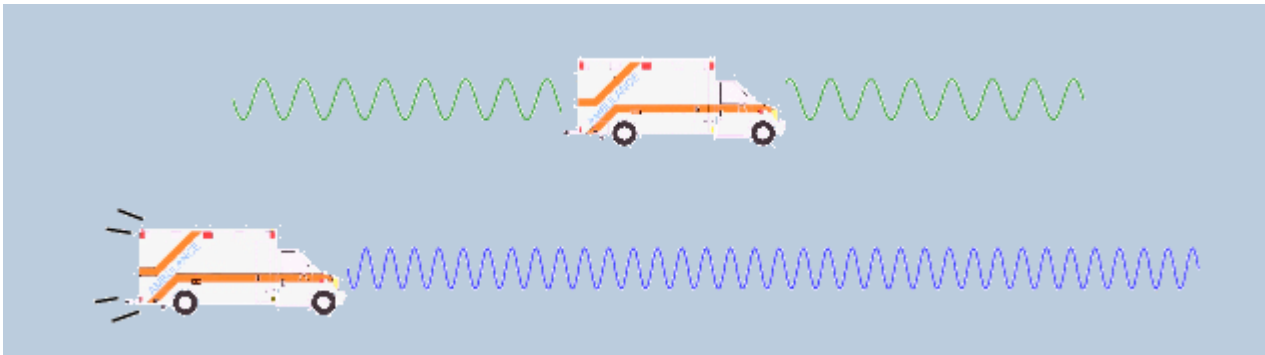


E.g.: Ball in a valley ... *with* friction

# How does a MOT work?

**Speed**-dependent force: the **Doppler effect**

**Position**-dependent force: **magnetic fields** make absorption rate depend on distance from centre



Lab frame:   

Atom's frame:   

The Doppler effect changes rate of absorbing laser beam

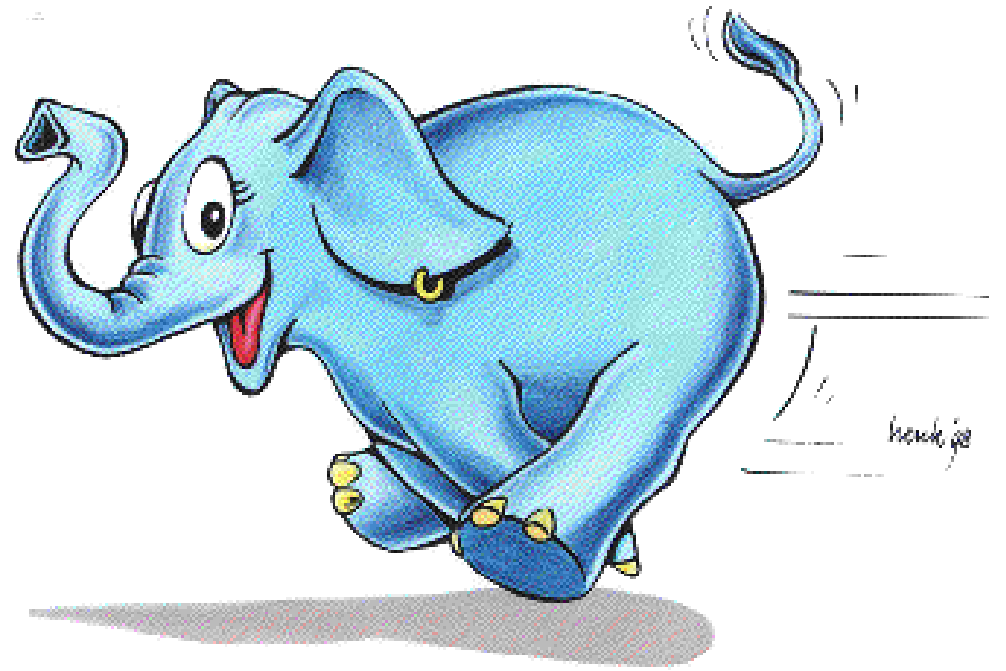


# Atom—photon interactions



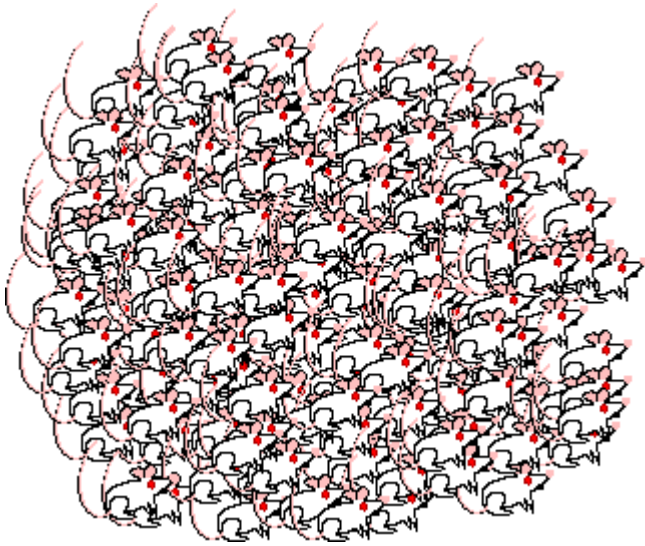
$$\hbar \vec{k} \sim 1.5 \text{ eV}/c$$

vs.

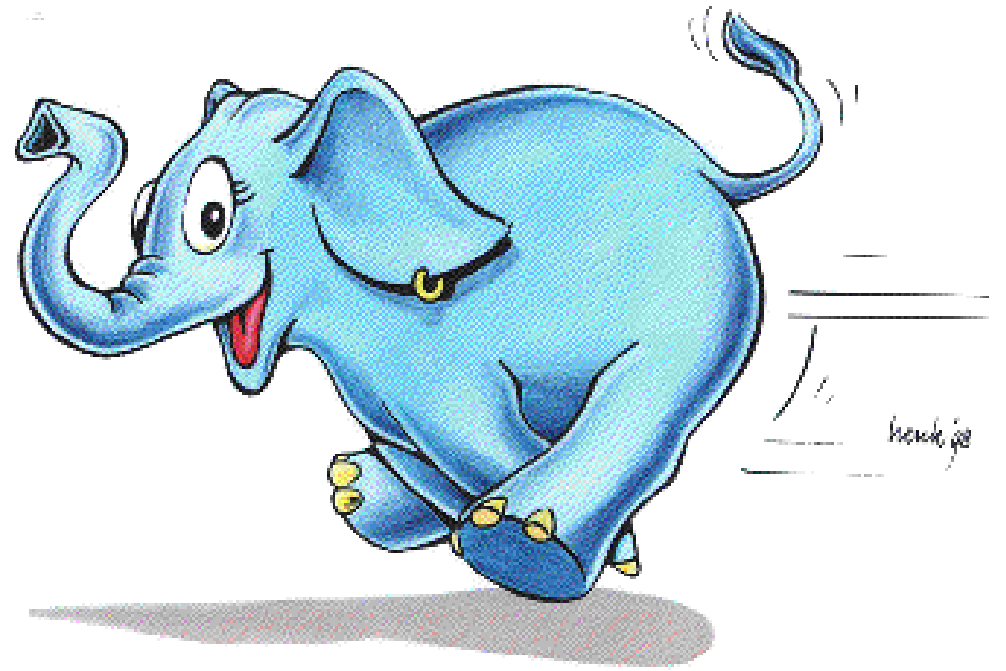


$$M \vec{v} \sim 45 \text{ keV}/c$$

# Atom—photon interactions

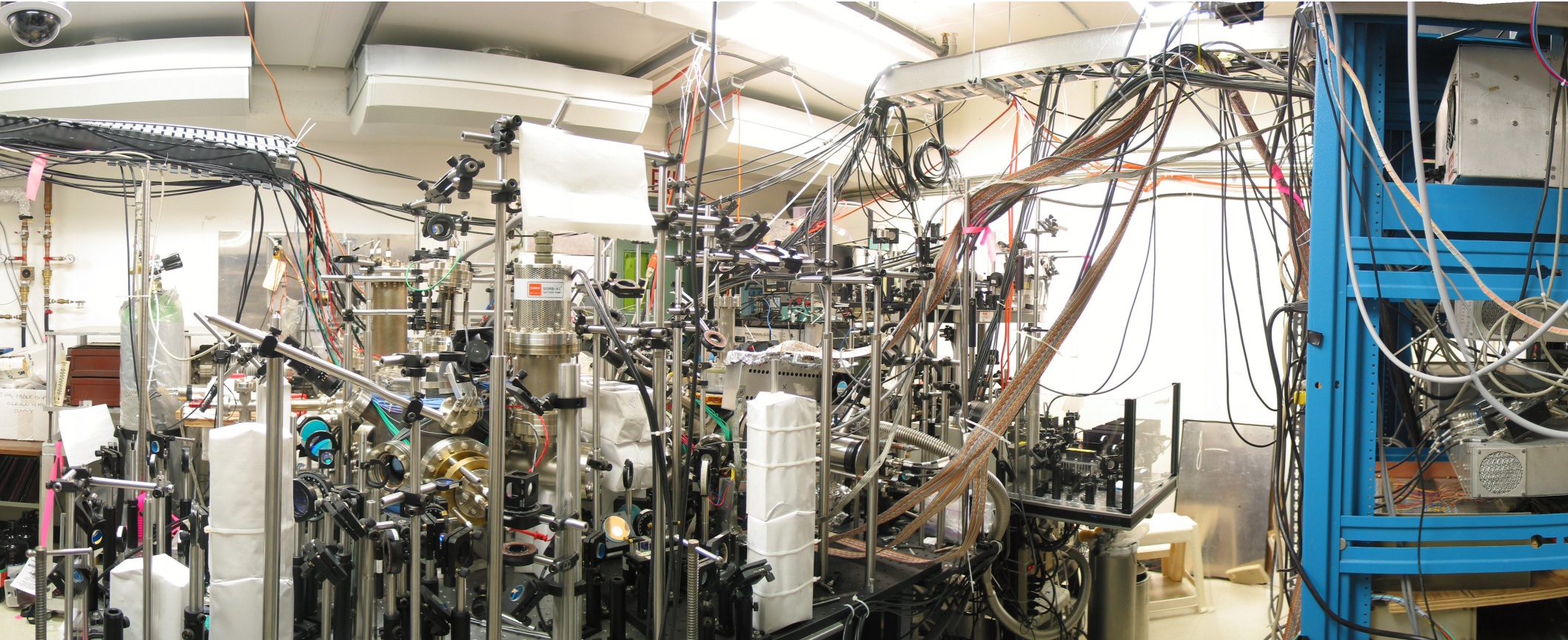
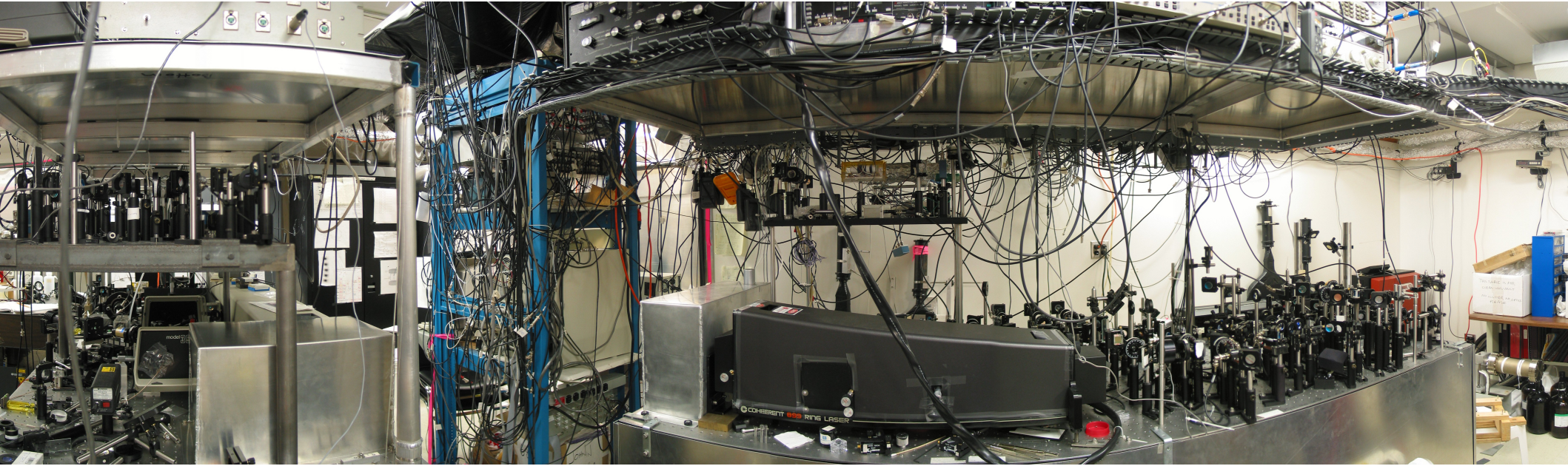


vs.

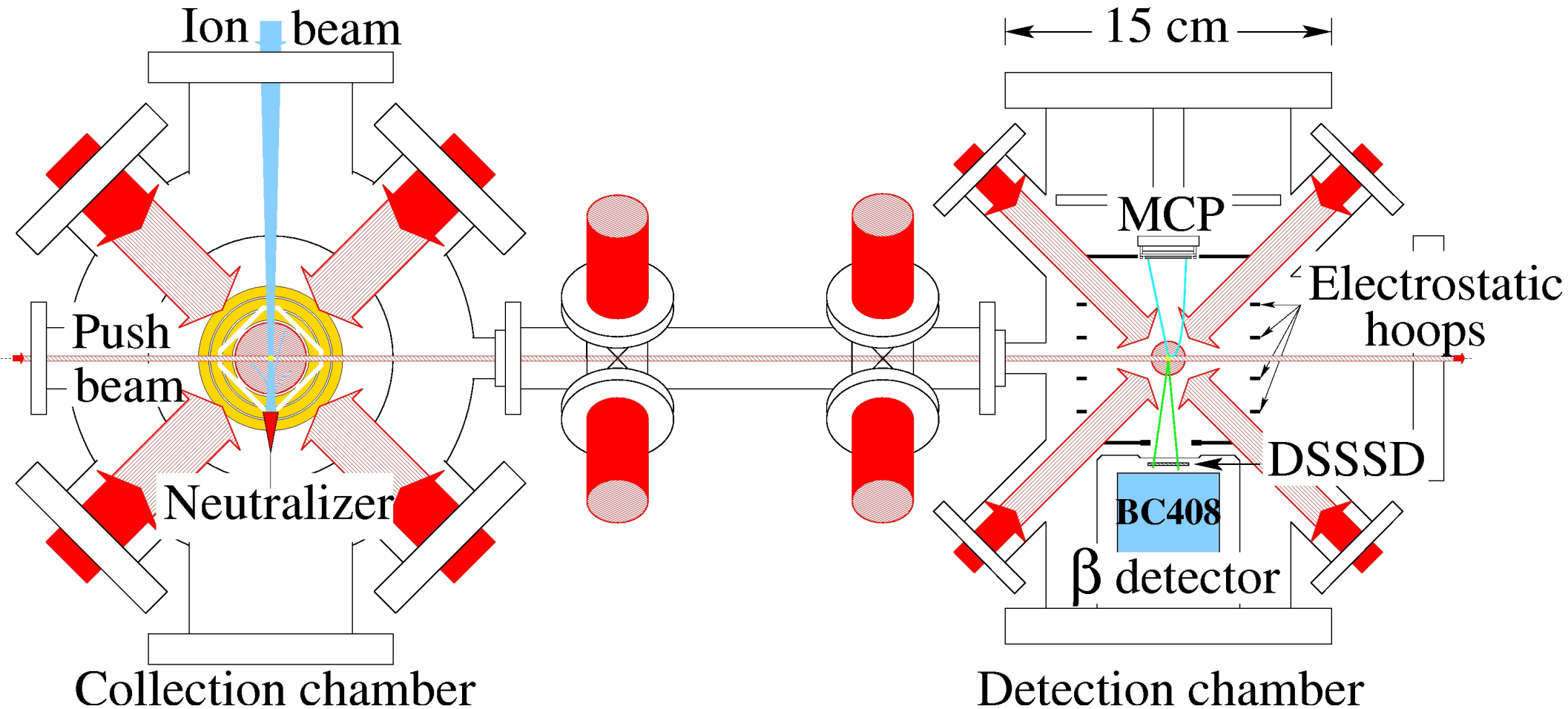


*Cycling transitions!!*

**Just in case you thought it was *easy* ...!!**



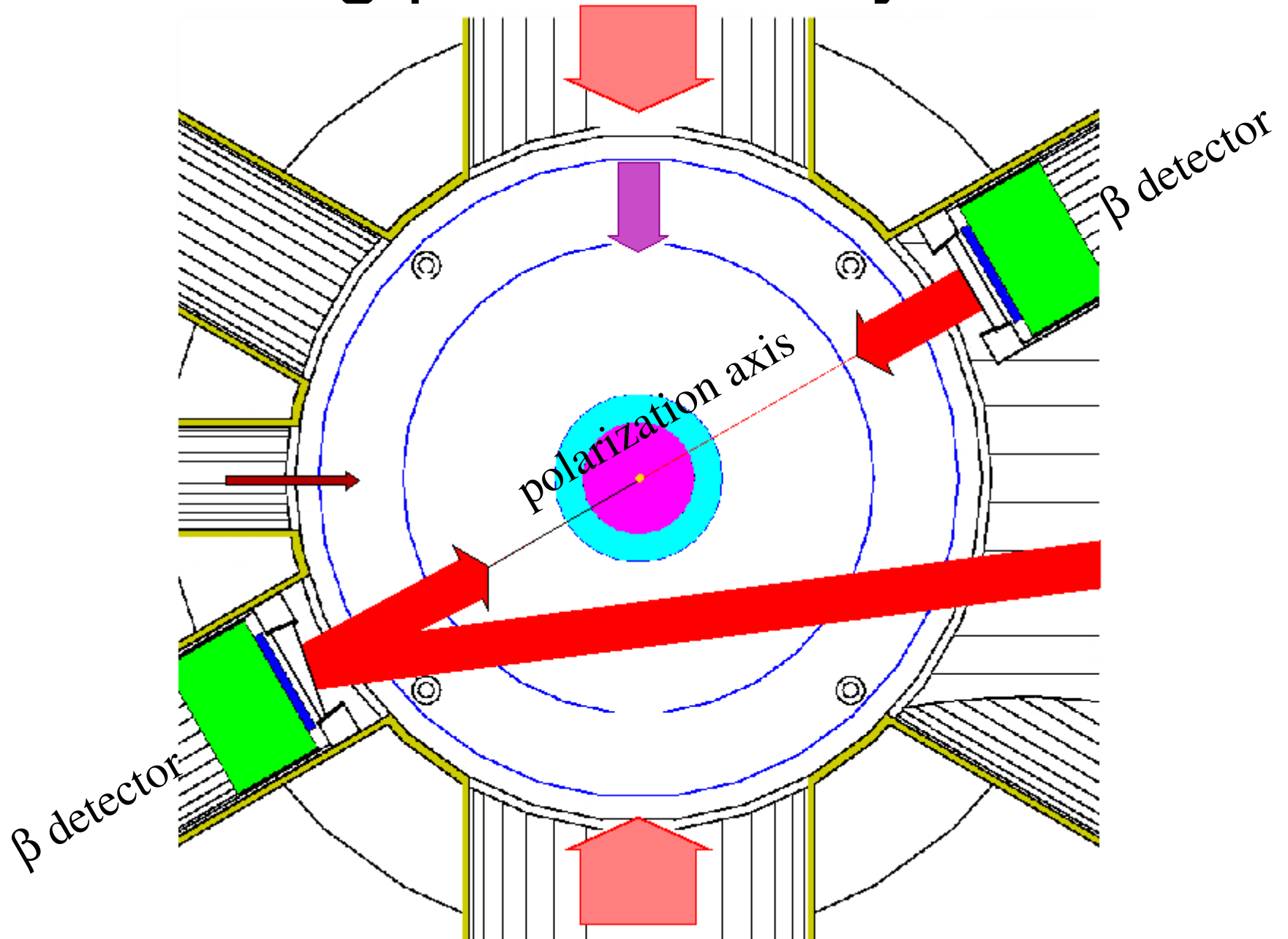
# A double-MOT system



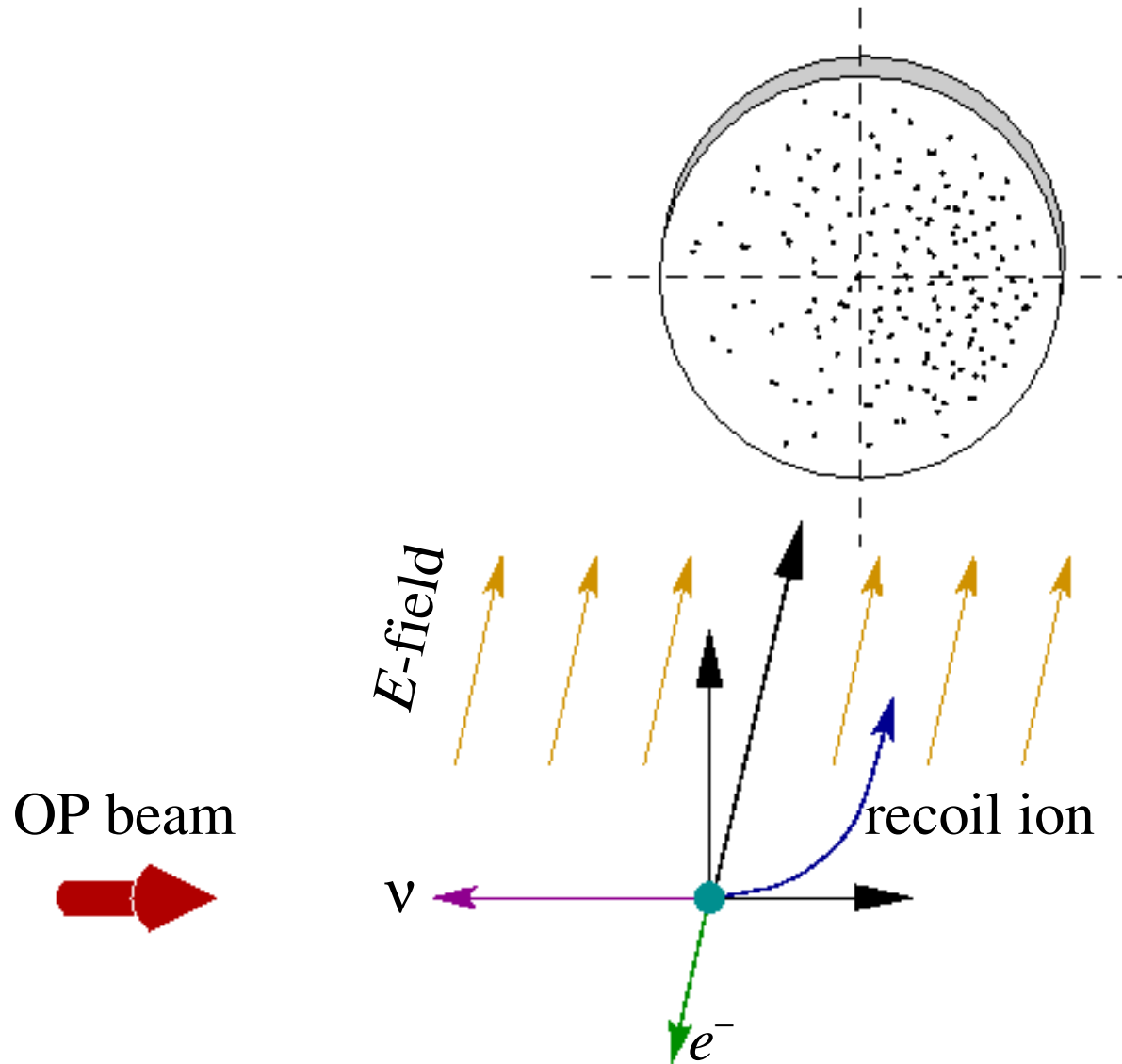
Traps provide a **backing-free**, **cold** ( $\sim 1\text{mK}$ ), **localized** ( $\sim 1\text{mm}^3$ ) source of **short-lived** radioactive atoms

Detect  $\vec{p}_e$  and  $\vec{p}_{recoil} \Rightarrow$  deduce  $\vec{p}_v!$

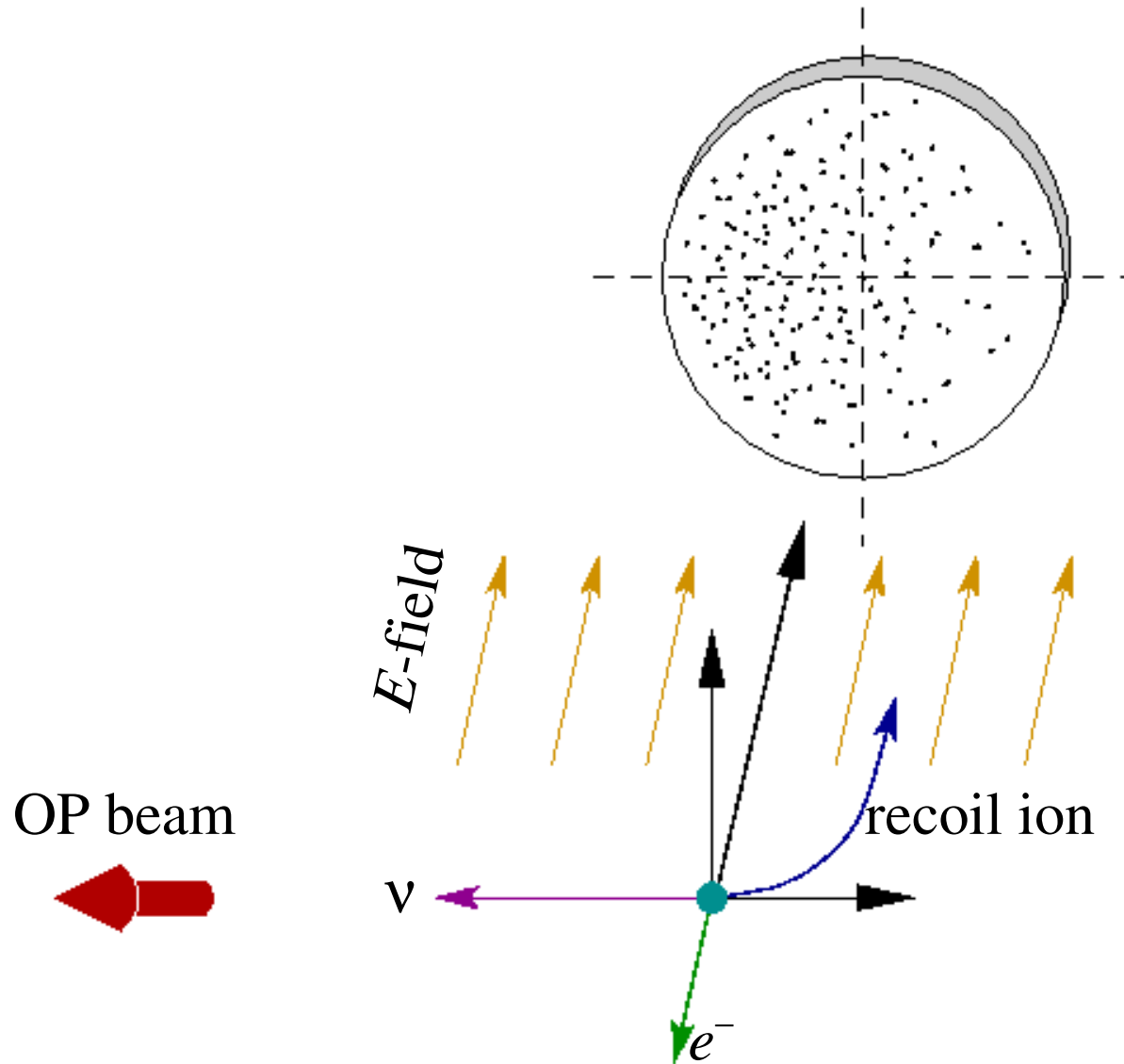
# Measuring polarized asymmetries



# The neutrino asymmetry

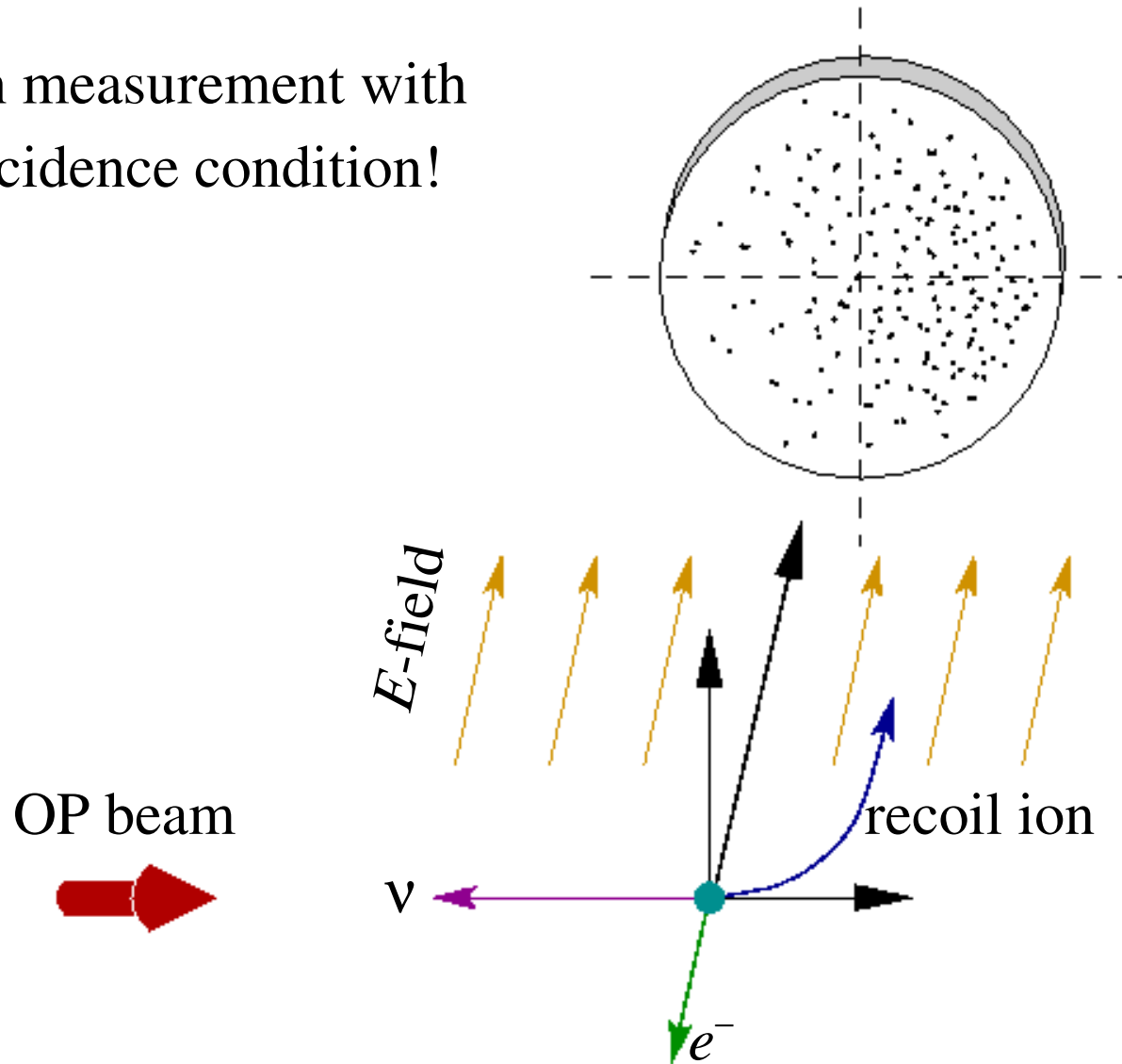


# The neutrino asymmetry



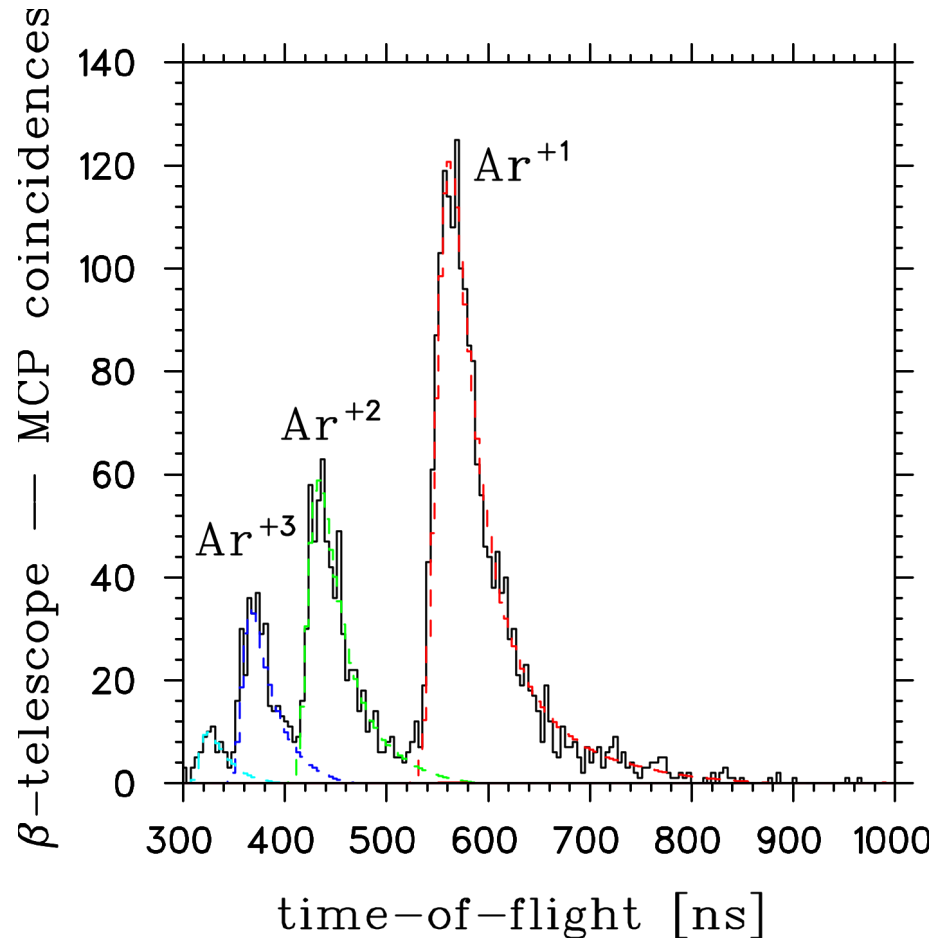
# The neutrino asymmetry

Clean measurement with  
coincidence condition!



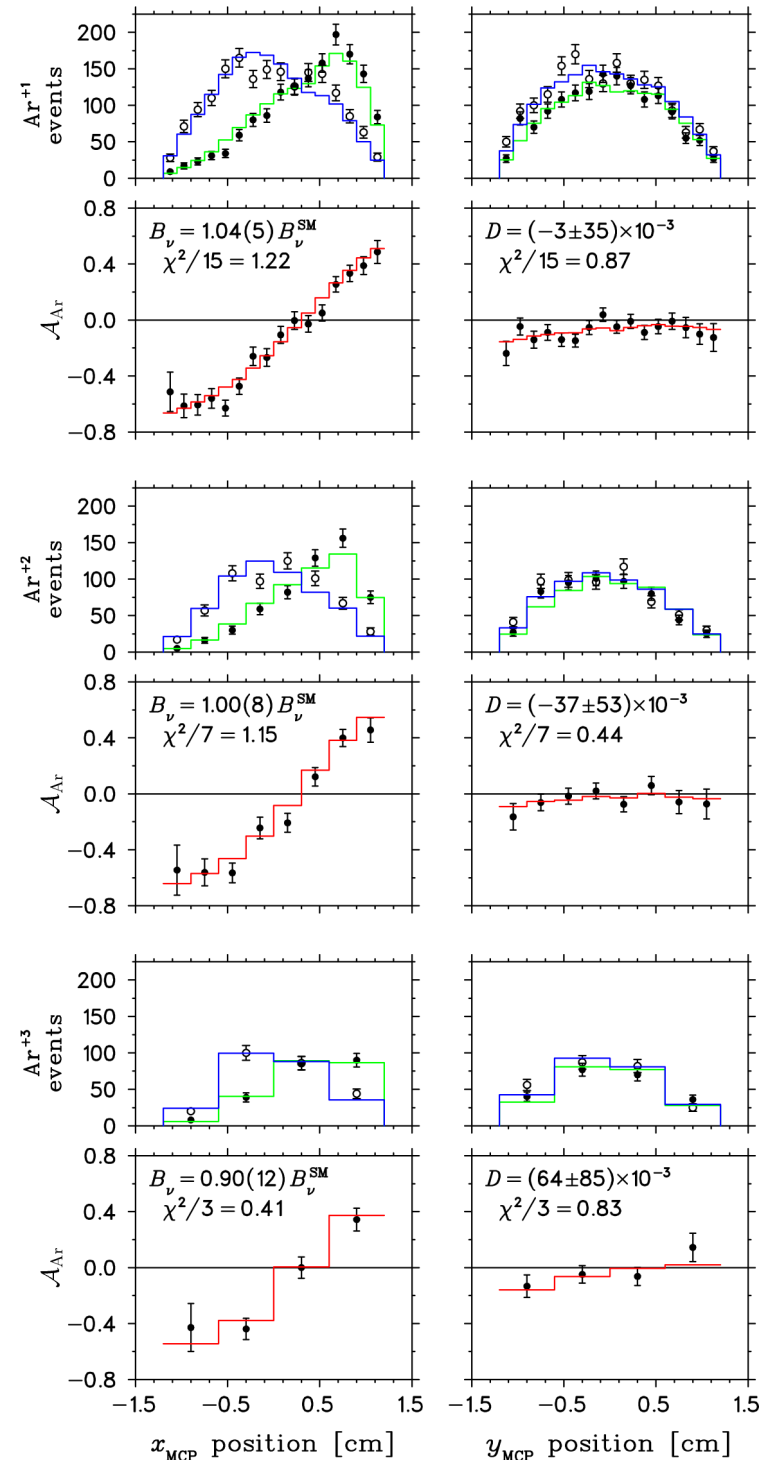


# Results



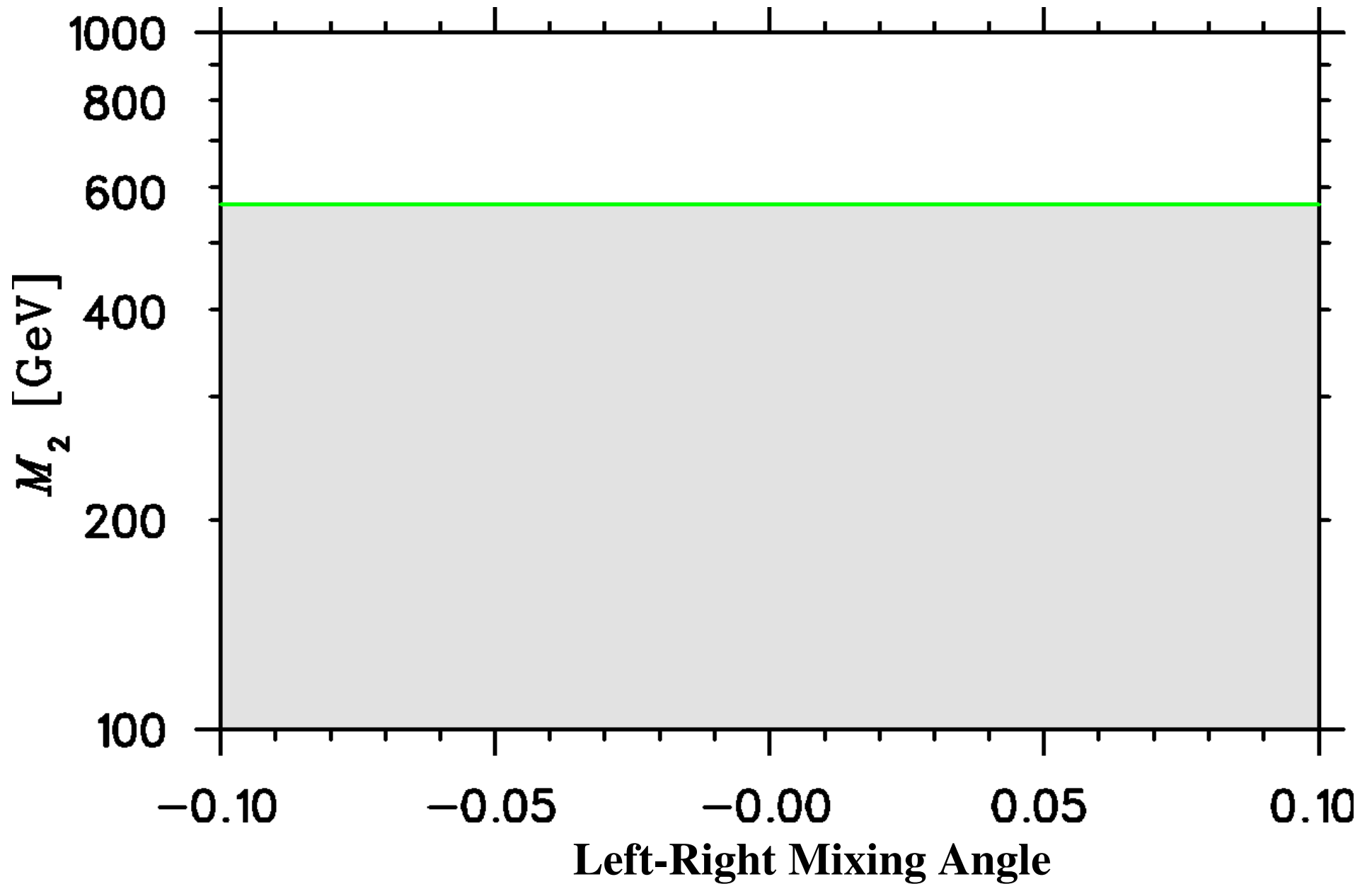
$$B_{\nu} = -0.755 \pm 0.020 \pm 0.013$$

This is about 20x better than Wu's experiment, but that was a long time ago ...



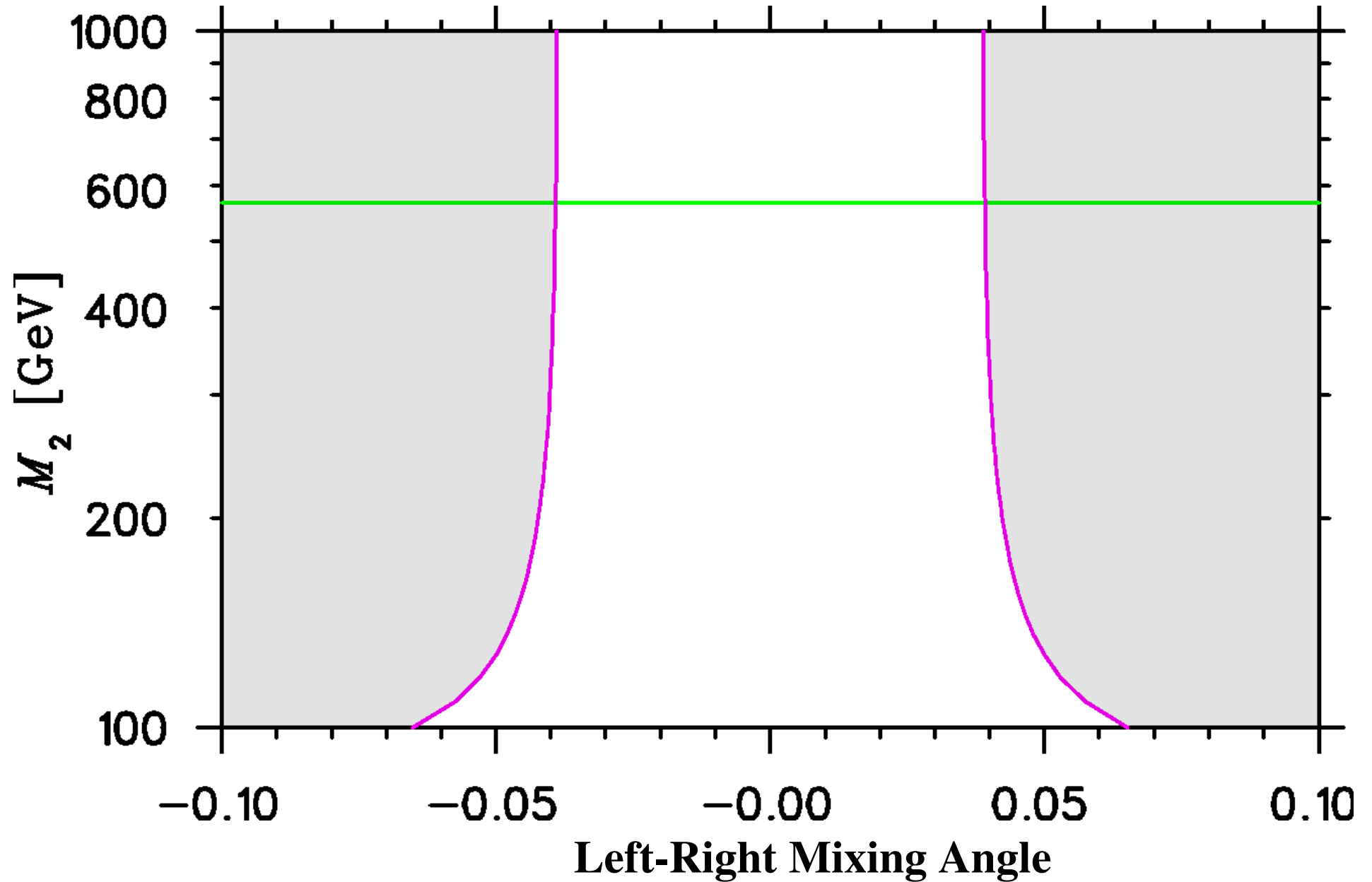
# Current limits

proton-proton colliders



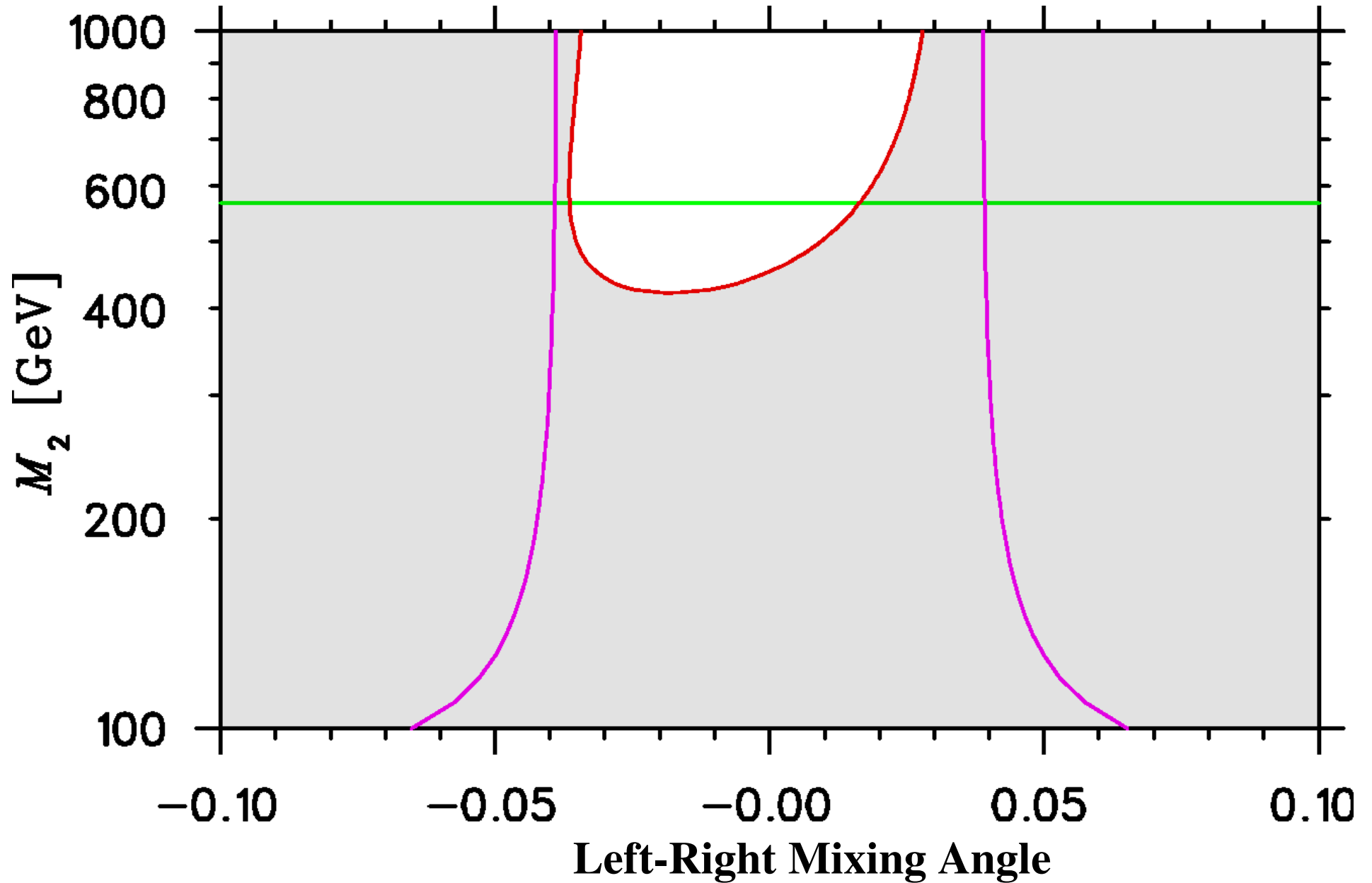
# Current limits

neutrino-nucleon scattering



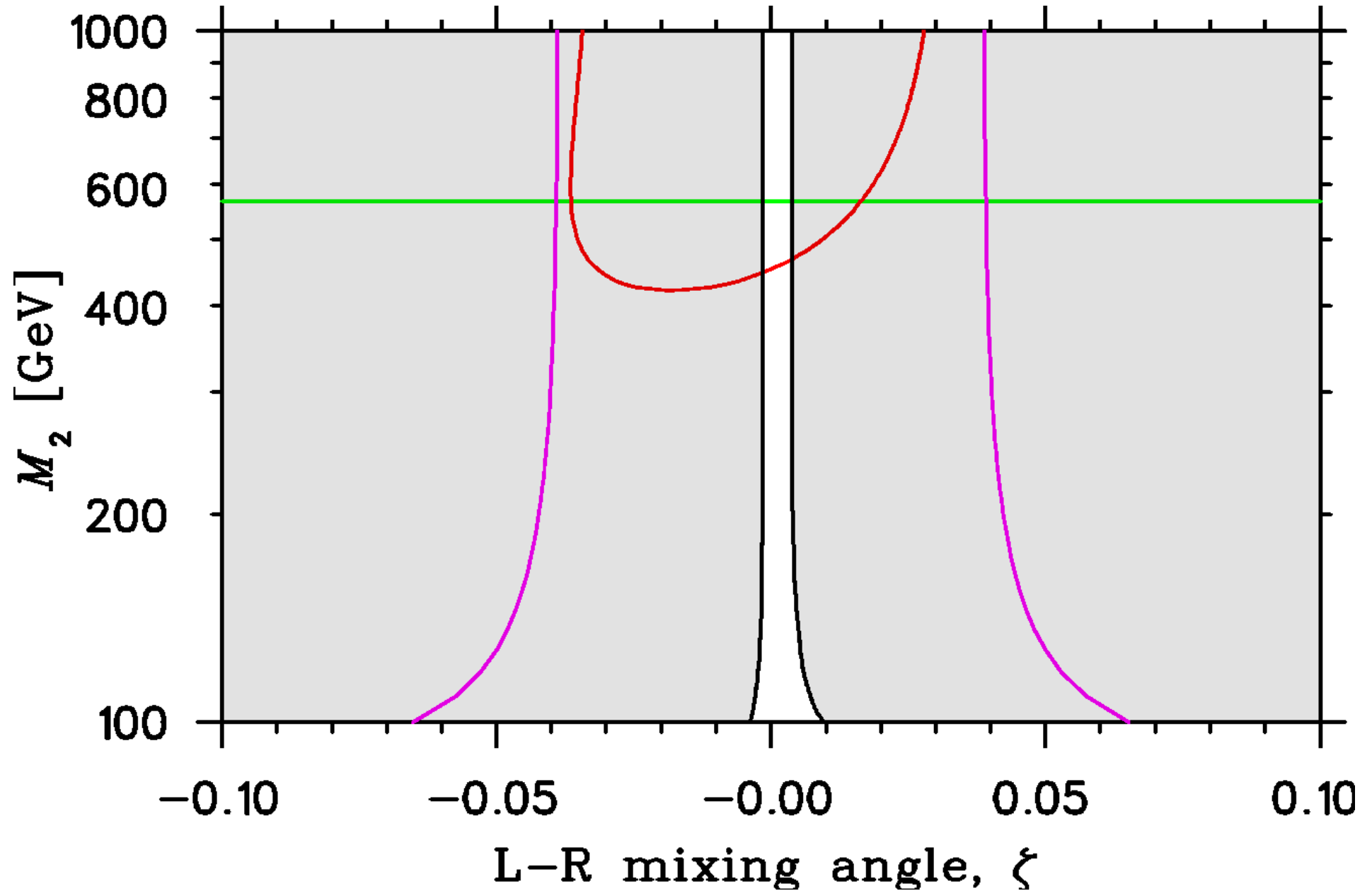
# Current limits

muon decay



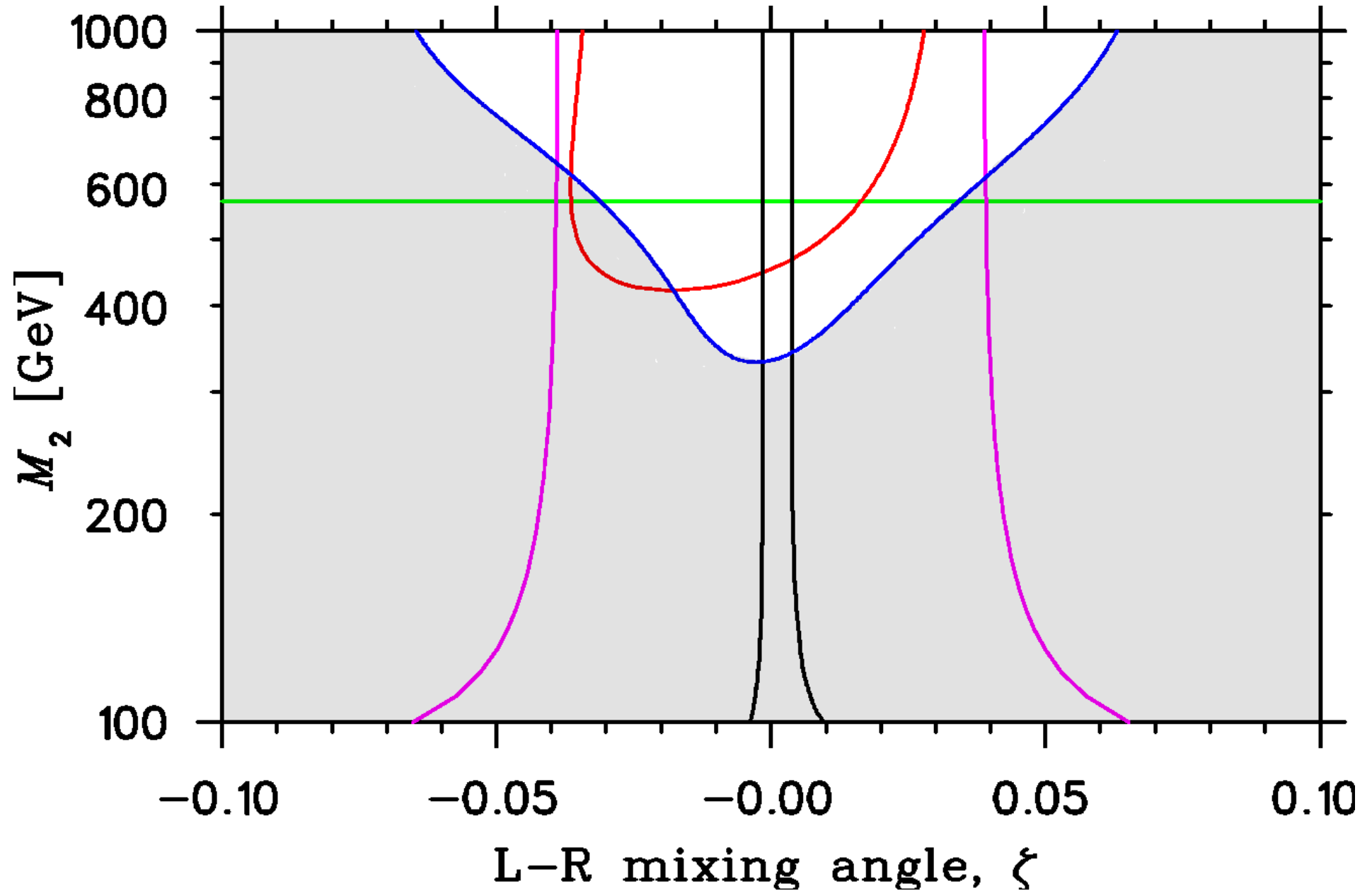
# Current limits

superallowed  $\beta$  decay



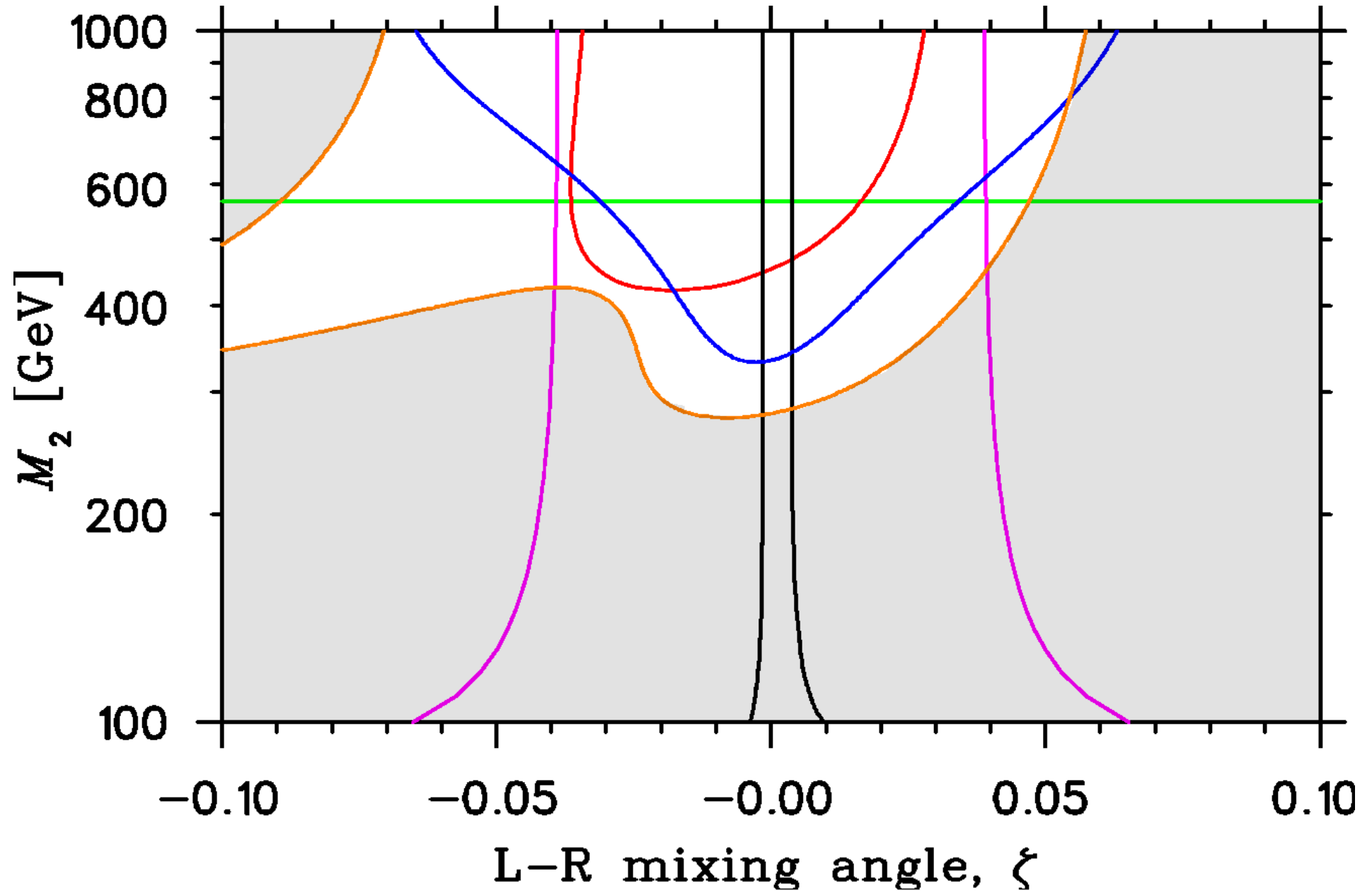
# Current limits

world average of  $\beta$  decay



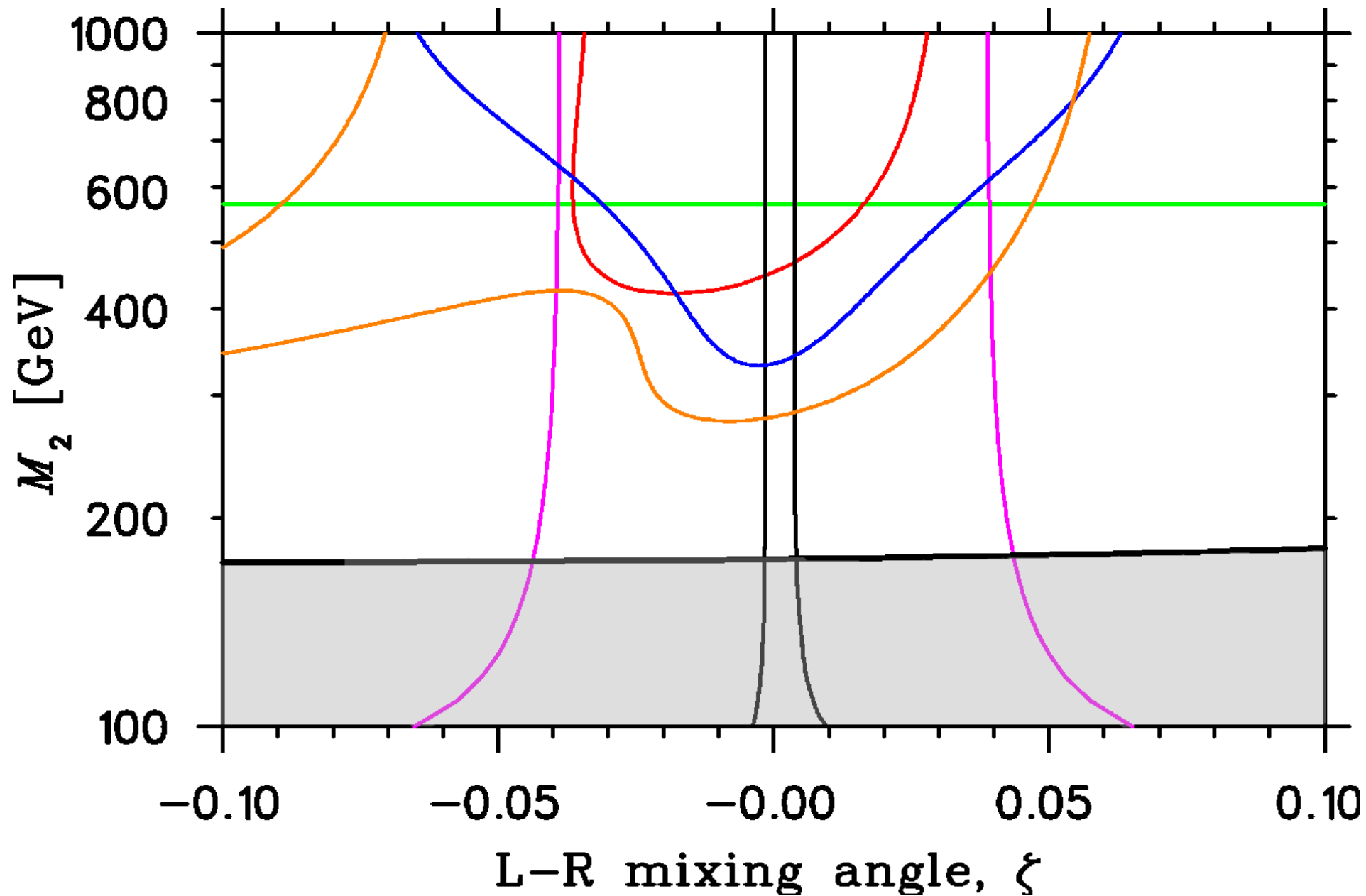
# Current limits

world average of neutron decay



# Current limits

result using trapped  $^{37}\text{K}$





# Current limits

expected results with improved  $^{37}\text{K}$  experiment

